

CHE-2F4Y
NUCLEAR MAGNETIC RESONANCE
SPECTROSCOPY

Course outline

1. Basic principles
2. Chemical shifts
3. Spin-spin coupling
4. Chemical exchange
5. Fundamentals of pulsed NMR
6. Nuclear spin relaxation

Nuclear Magnetic Resonance

Originally demonstrated in 1946

- Groups of Purcell and Bloch.

The Nobel prize in 1995 was won by R Ernst for his contributions to the development of NMR.

The Nobel prize in 2002 was won by K Wüthrich for his work in protein structure determination by NMR.

NMR is *the* method for analysing synthetic reactions

Idea of magnetic energy levels

- Pauli in 1924 to explain the atomic hyperfine structure

Magnetic **R**esonance **I**maging (MRI)

2005 Nobel Prize for

Physiology and Medicine

Professors Lauterbur and Mansfield

Fundamentals

Quantisation of angular momentum.

Nucleus has spin

- spin angular momentum

- **Nuclear**

Total angular momentum ***P*** can only have discrete values.

$$P = \hbar \sqrt{I(I+1)}$$

I, spin quantum number

- allowed angular momentum

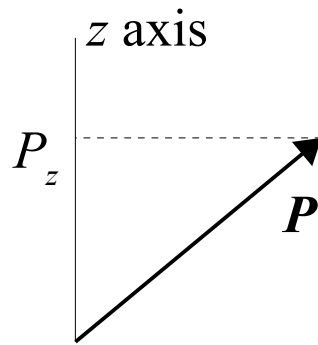
\hbar is $h/2\pi$

h is Planck's constant = 1.0544×10^{-34} Js

Energy is also quantised.

Angular momentum is a vector property.

- must state its direction as well as the magnitude.
- define the projection of the vector onto a *z* axis



Quantise in the z direction
 - magnetic quantum number, m_I .

$$P_z = \hbar m_I$$

Allowed values for m_I
 $I, I-1, I-2, \dots, -I$

In total $2I + 1$

Examples

$$I = 4$$

Allowed $m_I = +4, +3, +2, +1, 0, -1, -2, -3, -4$

I can also be half integral, for example $I = 3/2$.

Same conditions apply to m_I

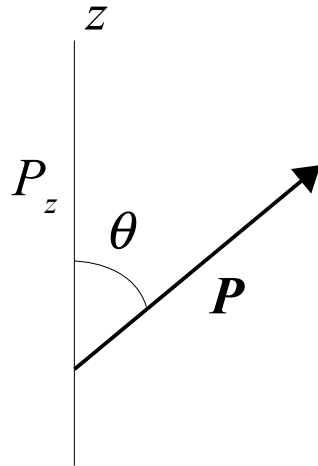
$$m_I = +3/2, +1/2, -1/2, -3/2.$$

Most useful nucleus for NMR, the proton, ^1H
 which has $I = 1/2$

$$\text{so } m_I = +1/2, -1/2.$$

If $m_I = 1/2$

Magnitude of the angular momentum P is $\frac{\sqrt{3}}{2} \hbar$



$$\begin{aligned}\cos \theta &= \frac{m_I}{\sqrt{I(I+1)}} \\ &= \frac{1}{\sqrt{3}} \\ \theta &= 54.7^\circ\end{aligned}$$

Degenerate in the absence of a magnetic field

Notice

- direction of the angular momentum vector is only defined in the z axis.
- any direction allowed in the x and y axes.
- in an ensemble with many spins the average value of the x and y components of the angular momentum will be zero.

Nuclear spin

What determines the spin of a given nucleus?

Both the proton and the neutron have spin $I=1/2$.

1. Odd mass number: Half integral spin
e.g. ^1H , ^{13}C , ^{15}N , $I=1/2$
and ^{23}Na , $I=3/2$
2. Even mass number/
even charge number: Zero spin
e.g. ^{12}C , ^{16}O
3. Even mass number/
odd charge number: Integral spin
e.g. ^2H , ^{14}N

Consequence

Common nuclei no NMR properties

^{12}C is 99% abundant and ^{16}O is 99.9%.

Quadrupolar nuclei

$I > 1/2$ possess a quadrupole moment



Nuclear magnetic states associated with quadrupolar nuclei tend to have shorter lifetimes

- broader lines
- “no” scalar coupling : Not observable indirectly

Consequently they are not readily studied and for most purposes can be regarded as non-magnetic

Emphasis in these lectures will be on spin-1/2 nuclei.

Magnetic moment

A nucleus possess a charge and is “spinning” it will “generate” a magnetic field.

- Magnetic

This is expressed by:

$$\mu = k P$$

k is a collection of fundamental constants

$$k = \frac{g_N \mu_N}{\hbar} \quad \text{with} \quad \mu_N = \frac{eh}{4\pi m_p}$$

$$\mu_N = 5.05 \times 10^{-27} \text{ JT}^{-1}$$

μ_N is the nuclear magneton

g_N is the nuclear g-factor

Notation common to both nuclear and electron spin resonance. But usually in NMR the magnetogyric ratio, γ , is used.

So $k = \gamma$

(UNITS $\text{rad T}^{-1}\text{s}^{-1}$ with the applied field B in Tesla)

Total magnetic moment

$$\mu = \gamma P$$

since

$$P = \hbar \sqrt{I(I+1)}$$

$$\mu = \gamma \hbar \sqrt{I(I+1)}$$

In the case of the projection onto the z axis

$$\mu_z = \gamma \hbar m_I$$