

Q.1-8 This question concerns the hamiltonian

$$\hat{H} = \hat{H}_1 + \hat{H}_2 + \hat{H}_3 + \hat{H}_4 + \hat{H}_5$$

that is used to predict the fine structure of the hydrogen atom. It consists of the five terms

$$\hat{H}_1 = \frac{\hat{\mathbf{p}} \cdot \hat{\mathbf{p}}}{2m}$$

$$\hat{H}_2 = -\frac{e^2}{4\pi\epsilon_0 r}$$

$$\hat{H}_3 = \frac{e^2 \hbar^2}{8\pi\epsilon_0 m^2 c^2 r^3} \hat{\mathbf{L}} \cdot \hat{\mathbf{S}}$$

$$\hat{H}_4 = -\frac{(\hat{\mathbf{p}} \cdot \hat{\mathbf{p}})^2}{8m^3 c^2}$$

and

$$\hat{H}_5 = \frac{e^2 \hbar^2}{8\pi\epsilon_0 m^2 c^2} \delta(x) \delta(y) \delta(z)$$

where $\hat{\mathbf{p}}$ is the momentum operator, $\hat{\mathbf{L}}$ is the orbital angular momentum operator, $\hat{\mathbf{S}}$ is the spin angular momentum operator and δ is the Dirac delta function.

- (i) Select the ONE option from the key that is the operator corresponding to a perturbation to the kinetic energy of the electron which takes into account some of the effects of special relativity. ☐
- (ii) Select the ONE option from the key that has zero expectation values for s -states ($l = 0$) of the hydrogen atom. ☐
- (iii) Select the ONE option from the key that has zero expectation values for all except s -states of the hydrogen atom. ☐

KEY for Q.1-8 (i) to (iii)

- A \hat{H}_1
B \hat{H}_2
C \hat{H}_3
D \hat{H}_4
E \hat{H}_5
-