

**The Handbook of Mathematics, Physics and  
Astronomy Data is provided**

KEELE UNIVERSITY

EXAMINATIONS, 2011/12

Level III

Monday 27<sup>th</sup> February 2012, 14.15-15:45

PHYSICS/ASTROPHYSICS

PHY-30023

PARTICLES, ACCELERATORS AND REACTOR PHYSICS

**Candidates should attempt to answer TWO questions.**

**NOT TO BE REMOVED FROM THE EXAMINATION HALL**

1. (a) Explain what is meant by *isospin* and *isospin multiplet* and quote the relevant quantum numbers for a proton and a neutron. [25]
- (b) State the Gell-Mann-Nishijima formula which applies to hadrons composed of down, up and strange quarks (and their antiquarks) only. Sketch a diagram of strangeness  $S$  versus  $T_3$ , the 3 axis isospin component quantum number, showing the positions of these three quarks and their anti-quarks. [15]
- (c) For each of the following spin 3/2 baryon multiplets; state the isospin quantum number  $T$  and use the formula of part (b) to determine the strangeness  $S$ .
- i.  $\Delta^{++} \Delta^+ \Delta^0 \Delta^-$  quartet. [5]
  - ii.  $\Sigma^{*+} \Sigma^{*0} \Sigma^{*-}$  triplet. [5]
  - iii.  $\Xi^{*0} \Xi^{*-}$  doublet. [5]
  - iv.  $\Omega^-$  singlet. [5]
- (d) Position all the particles of part (c) on an  $S$  vs  $T_3$  diagram and determine the quark structure of each. [40]

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2. (a) Discuss the conservation of baryon and lepton numbers, strangeness, charm and isospin for particles interacting via each of the electromagnetic, strong nuclear and weak nuclear interactions. [20]

- (b) Discuss the conservation of strangeness and lepton numbers for
- the decay of the strangeness  $S = 0$ ,  $\phi$  meson to the  $S = -1$ ,  $K^-$  meson and its antiparticle:



- the decay of the  $K^-$  particle:



- (c) The  $K^-$  has zero charm and does not contain top or bottom quarks. Determine
- its quark structure and [10]
  - its 3 axis component of isospin  $T_3$ . [5]
- (d) State and explain which field particle is involved in the decay of the  $K^-$  in part (b)ii. [5]
- (e) Write down and illustrate charge conservation, for each of the individual quarks in this  $K^-$  decay. [20]
- (f) Discuss why particle physics experiments tend to produce an abundance of mesons, but free quarks are not observed. [20]

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3. (a) Compare and contrast the operation of a *simple cyclotron*, *synchrocyclotron*, an *azimuthally varying field cyclotron* and a *synchrotron*. Your answer should include a discussion of the following points:

- acceleration and direction control mechanisms;
- relativistic effects;
- variation of key parameters, e.g., magnetic field, during operation;
- beam properties.

[60]

(b) By assuming that the orbital frequency for a particle of charge  $qe$  and relativistic total energy  $E$  in a magnetic field  $B$  is

$$f = \frac{qeBc^2}{2\pi E}$$

show that

$$f = \frac{c}{2\pi r}$$

for an electron synchrotron of radius  $r$ . [20]

(c) Electrons are extracted from an 80m radius synchrotron by a magnetic field of 0.7T. Calculate their energy in GeV. [10]

(d) Explain why the simple relationship of frequency to radius in part (b) does not apply for a proton synchrotron. [10]

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4. (a) Describe the different ways in which a neutron may interact with a nucleus on collision. [30]
- (b) The cross section for the  $^{59}\text{Co}(n,\gamma)^{60}\text{Co}$  reaction for thermal neutrons is 22 barns. Calculate the mass of  $^{59}\text{Co}$  to be placed in a thermal neutron flux of  $10^{14}\text{m}^{-2}\text{s}^{-1}$  in order to produce  $^{60}\text{Co}$  nuclei at a rate of  $10^{10}\text{s}^{-1}$ . (1 barn =  $10^{-28}\text{m}^2$ .) [15]
- (c) Explain what is meant by *neutron reproduction factor* in a nuclear reactor. [10]
- (d) The minimum volume of a cubic reactor is given by

$$V = \frac{161}{B^3}$$

where SI units are used and

$$B^2 = \frac{k_\infty - 1}{L^2}$$

for neutron diffusion length  $L$  and neutron reproduction factor  $k_\infty$  assuming an infinite assembly.

- i. Determine the length of the side of the cube for  $L = 0.4\text{ m}$  and  $k_\infty = 1.07$  [10]
- ii. Explain how the minimum volume of a spherical reactor compares with that of the cubic reactor and why. [10]
- iii. Explain how a realistic neutron reproduction factor  $k$  compares with  $k_\infty$  and why. [15]
- iv. Explain why it is advantageous to surround the core of a thermal fission reactor with graphite. [10]