





**Special Instructions for Invigilators:** None

**Information for candidates:**

1. a) Assume that a receiver is located at a distance  $d_0 = 1$  km from a base station transmitting at a power of 10 W. If the carrier frequency is 900 MHz, free space propagation is assumed and the transmitter and receiver gains are  $G_T = 1$ , and  $G_R = 2$  respectively, at the receiver antenna find

- i) the free-space power,  $P_{FSR}(d_0)$ , and [3]  
 ii) the magnitude of the electric field,  $E_{FSR}(d_0)$ . [2]

- b) Assume that in a mobile radio system, the area-mean-power,  $P_{am}(R_1)$ , at the cell boundary is  $6.57 \times 10^{-11}$  W, and  $R_1 = 6$  km. The interference signal power,  $6 P_{am}(D)$ , in the radio cell is constant and equal to  $9.1 \times 10^{-13}$  W. A mobile user is located  $R_2$  km away from the base station and the received signal is subjected to randomly fluctuating shadowing losses as the mobile moves. The standard deviation,  $\sigma$ , of the log-normal shadowing loss is  $\sigma = 3$  dB. The probability that the local-mean-power,  $P_{lm}(R_2)$ , will exceed a certain value  $\gamma$  is calculated from the cumulative distribution function using

$$\Pr(P_{lm}(R_2) > \gamma) = 1 - \frac{1}{2\sqrt{\pi}} \exp \left\{ - \left( \frac{10 \log_{10} \frac{P_{am}(R_2)}{\gamma}}{\sigma \sqrt{2}} \right)^2 \right\}.$$

Find the maximum transmitter-receiver separation,  $R_2$ , that will ensure that a local-mean-power to interference-power ratio of 13 dB is provided for 95% of the time. [4]

- c) Assume that in a narrow-band mobile radio system, the shadowing loss is 0 dB and the mobile is  $R_1$  metres away from the base station and is moving at a steady speed of  $v$  m/s and receiving a signal with wavelength  $\lambda$  metres.

- i) Describe how the statistical time varying nature of the received signal envelope can be expressed using the Rayleigh fading probability density function (PDF). [3]  
 ii) Show how the actual signal power,  $P_i(R_1)$ , can be related to the area mean power,  $P_{am}(R_1)$ , and the Rayleigh fading amplitude  $R$ . [3]

*Question continued over*

- d) A narrow-band mobile radio system, subject to Rayleigh fading, uses differential binary phase-shift-keying modulation. As a function of the signal-to-noise ratio,  $X_a$ , the bit error probability,  $P_e(X_a)$ , is given by  $P_e(X_a) = \frac{1}{2} \exp(-X_a)$ . Show that the bit-error-probability is given by  $P_e(X_R) = \frac{1}{2 + 2X_R}$  as a function of wanted-signal-area-mean power to total-interference-signal-power ratio,  $X_R$ . [5]

2. a) Describe
- i) how the performance of a slotted Aloha multiple access scheme is stabilised by controlling the re-transmission probabilities of back-logged users, [2]
  - ii) why it is necessary to estimate the number of backlogged users in order to stabilise slotted Aloha systems, and [2]
  - iii) how the offered load-drift,  $dG$ , given by  $dG = \frac{dn - G ds}{S_{k+1}}$  can be used to stabilise a slotted Aloha system at the optimum offered load. Assume that  $N_k$  and  $S_k$  respectively are the real and estimated numbers of backlogged users and that  $G_k = \frac{N_k}{S_k}$ . Assume also that the terms  $dn$  and  $ds$  correspond to the real and estimated drifts respectively. [3]
- b) Assume that the joint-drift,  $dj$ , is related to the offered-load-drift by  $dj = S_{k+1} dG$ . State the limiting values of the joint drift equation  $dj(G)$  for  $G = 0$  and  $G = \infty$ . Comment on the results if the control parameter  $u_c$  (i.e the number of corrections applied to the estimated number of users when there is a collision), satisfies the condition  $u_c > \lambda$ . [5]
- c) If the joint drift equation  $dj(G) = 0$  has three roots, discuss under what condition the largest root might result in an unstable Aloha system. Comment on the real number of users in the system for this case. [4]
- d) In a mobile radio system a circular radio cell of radius 450m is used. There are 1600 mobile users in an area of 20000  $m^2$  and 12 percent of the mobile users are active during a one hour period. Determine
- i) the call arrival rate per second for the access control scheme, and [2]
  - ii) the call arrival rate per slot, assuming a slotted Aloha system with packet duration of 100 ms is used. [2]

This page is intentionally left blank.

3. a) Explain
- i) why equalisers are required in wideband radio transmission systems, and [2]
  - ii) how the equaliser coefficients are calculated using training sequences employed in a GSM radio system. You may assume that the channel introduces intersymbol interference and suffers from additive white Gaussian noise. [2]
- b) Discuss the advantages and disadvantages of using
- i) *linear equalisers*, [2]
  - ii) *decision feedback equalisers* and [2]
  - iii) *maximum likelihood sequence detectors*. [2]
- in wideband mobile radio systems.
- c) The cell radius of a mobile radio system is  $R_1 = 1000$  m. When a narrow-band radio system is used the system operates with the required signal-to-noise ratio  $X_R(R_1) = 875$  and provides 20 simultaneous conversations in each cell. The narrow-band system will be replaced with a wide-band system that is time-shared between eight users and covers eight times the transmission bandwidth of the narrow-band system. Both the wide-band and the narrow-band systems have the same transmitter powers, the same transmitter and receiver antenna gains of unity, and the same desired signal-to-noise ratios  $X_D(R_2) = 13$  dB. Assuming that the wideband system achieves the desired signal-to-noise ratio at  $R_2 = 970$  m when the equaliser gain,  $c_0$ , is 0.8 find
- i) the total number of channels available with the narrow-band system, [2]
  - ii) the number of simultaneous conversations the wide-band system can provide for the same total number of physical channels. [3]

*Question continued over*



- d) In a wide-band mobile radio system, the base-station transmits uncorrelated data signals. A channel, with an impulse response  $\mathbf{h} = [0.845 \ 0.507 \ 0.169]^T$ , introduces intersymbol interference for the received signal. The ratio of area-mean-power-to-total-interference-power is equal to 13 dB at the cell boundary. A minimum-mean-square-error decision-feedback-equaliser (DFE) is used to equalise the received signal. The equaliser feedforward and feedback coefficients are  $\mathbf{c} = [-0.0094 \ 0.0477 \ 1.081]^T$  and  $\mathbf{b} = [-0.5561 \ -0.1827]^T$  respectively. Find the signal-to-noise ratio at the output of the equaliser and the corresponding equaliser gain  $c_0$ .

- 4) a) In connection with the Global Systems Mobile (GSM) radio system, describe
- i) the framing structure for the control channels, [2]
  - ii) how the network switching subsystem is modified to handle packet transmission for use in the General Packet Radio Service (GPRS). [2]
- b) Describe how new sets of logical channels are used as part of GPRS in the phase-two GSM specifications in the case of
- i) the packet common control channel, [1]
  - ii) the packet broadcast control channel, [1]
  - iii) the packet data traffic channel. [1]
- c) For the third generation wideband UTRA/FDD radio system, outline
- i) the orthogonal variable spreading factor codes, [1]
  - ii) the physical layer structure, paying particular attention to:
    - how the uplink modulation and scrambling are organised to minimise the audible interference from the terminal transmission, [2]
    - the transport channels:
      - ◆ the dedicated transport channel, [1]
      - ◆ the downlink shared common transport channel. [1]
  - iii) The downlink frame structure, paying particular attention to the DPCCH / DPDCH structure. [2]
  - iv) the downlink multiplexing and channel coding, paying particular attention to
    - the transport block concatenation, [1]
    - the downlink channel coding, [1]
    - the frame equalisation, [1]
    - the interleaving, [1]
    - the radio frame segmentation, [1]
    - the rate matching. [1]