IMPERIAL COLLEGE LONDON

/ E4.03 AS5 SO10 /ISE4.3

DEPARTMENT OF ELECTRICAL AND ELECTRONIC ENGINEERING **EXAMINATIONS 2007**

MSc and EEE/ISE PART IV: MEng and ACGI

Corrected Copy

MOBILE RADIO COMMUNICATION

Tuesday, 1 May 10:00 am

Time allowed: 3:00 hours

There are FOUR questions on this paper.

Answer THREE questions.

All questions carry equal marks. The maximum mark for each subquestion is shown in brackets.

Any special instructions for invigilators and information for candidates are on page 1.

Examiners responsible

First Marker(s): M.K. Gurcan

Second Marker(s): K.K. Leung

The Questions

- 1. Answer the following subquestions.
 - (a) For the two-ray path-loss model, derive an approximate expression for the distance values below the critical distance, d_c , at which signal nulls occur.
 - (b) The following table lists a set of empirical path-loss measurements.

Distance from Transmitter	P_r/P_t
5 m	-60 dB
25 m	-80 dB
65 m	-105 dB
110 m	-115 dB
400 m	-135 dB
1000 m	-150 dB

Take 7=0.4248

where P_t and P_r are transmitted and received signal powers.

- i. Find the parameters of a simplified path-loss model, plus log normal [3] shadowing that best fit this data.
- ii. Find the path loss at 2000 m based on this model. [2]
- iii. Find the outage probability at a distance d assuming the received power at d due to path-loss alone is 10 dB above the required power for non-outage. [2]
- (c) Consider a two-path channel with impulse response

$$h(t) = \alpha_1 \delta(\tau) + \alpha_2 \delta(\tau - 22 \times 10^{-9} s).$$

Find the transmission delay τ , as well as α_1 and α_2 , assuming a free space path loss on each path, and a reflection coefficient of -1. Assume the transmitter and receiver are located 8 meters above the ground and the carrier frequency is 900 MHz.

- 2. Answer the following subquestions.
 - (a) For a Rayleigh fading channel with average power \bar{P}_r = 30dB, and Doppler frequency $f_D = 10$ Hz, compute the average fade duration for target fade values P_0 = 0 dB, P_0 = 15 dB, and P_0 = 30dB. [5]
 - (b) Consider the following two-ray channel scattering function obtained when applying a 900 MHz sinusoidal input to the channel:

$$S(\tau, \rho) = \begin{cases} \alpha_1 \delta(\tau) & \rho = 70\\ \alpha_2 \delta(\tau - 22 \times 10^{-9} \text{s}) & \rho = 49.5 \text{Hz}\\ 0 & \text{else,} \end{cases}$$

where α_1 and α_2 are determined by path loss, shadowing, and multipath fading. Assume the transmitter and receiver used to send and receive the sinusoidal signal are located 8 meters above the ground.

- i. Find the distance and velocity between the transmitter and receiver. [3]
- ii. For the distance computed in part i., is the path loss as a function of distance proportional to d^{-2} or d^{-4} ?
- iii. Does a 30 KHz voice signal transmitted over this channel experience flat [2] fading or frequency-selective fading?
- (c) Let a scattering function $S(\tau, \rho)$ be nonzero over $0 \le \tau \le 0.1$ ms and $-0.1 \le \rho \le 0.1$ Hz. Assume that the power of the scattering function is approximately uniform over the range where it is nonzero.
 - i. What is the multipath spread and the Doppler frequency spread of the [1] channel?
 - ii. If the input to this channel is two identical sinusoidal signals separated in time by Δt , what is the minimum value of Δf for which the channel response to the first sinusoidal signal is approximately independent of the channel response to the second sinusoidal signal?
 - iii. For two sinusoidal inputs to the channel $u_1(t) = \sin 2\pi f t$ and $u_2(t) = \sin 2\pi f (t + \Delta t)$, what is the minimum value of Δt for which the channel response to $u_1(t)$ is approximately independent of the channel response to $u_2(t)$?
 - iv. Will this channel exhibit flat fading or frequency-selective fading for a typical voice channel with a 3 KHz bandwidth? Examine the nature of fading for a cellular channel having a bandwidth of 30 KHz.

[2]

3. Answer the following subquestions.

- (a) Consider an additive white Gaussian noise (AWGN) channel with bandwidth 50 MHz, received power 10 mW, and a noise power spectral density (PSD) $N_0=2\times10^{-9}$ W/Hz. If the received signal power is doubled, by how much is the capacity increased? If the channel bandwidth is doubled, by how much is the capacity increased?
- [3] [3]

[3]

[3]

[4]

- (b) Consider a flat-fading channel where, for a fixed transmit power \bar{P} , the received signal-to-noise-ratio (SNR) is one of four values: $\gamma_1 = 30$ dB, $\gamma_2 = 20$ dB, $\gamma_3 = 10$ dB, and $\gamma_4 = 0$ dB. The probability associated with each state is $p_1 = 0.2$, $p_2 = 0.3$, $p_3 = 0.3$, and $p_4 = 0.2$ respectively. Assume both transmitter and receiver have Channel Side Information.
 - i. Find the optimal power control policy $P(\gamma_i)/\bar{P}$, $i=1,\cdots,4$, for this channel and its corresponding Shannon capacity per unit of bandwidth.
 - ii. Find the channel inversion power control policy for this channel and the associated zero-outage capacity per unit of bandwidth.
 - iii. Find the truncated channel inversion power control policy for this channel and the associated outage capacity per unit bandwidth and also the associated cutoff γ_0 for the following three different outage probabilities: $p_{out} = 0.1$, $p_{out} = 0.01$, and p_{out} corresponding to the value that achieves the maximum capacity with outage.
- (c) Consider two users simultaneously transmitting to a single receiver in an AWGN channel. Assume the users have equal received power of 10 mW and total noise at the receiver in the bandwidth of interest of 0.1 mW. The channel bandwidth for each user is 20 MHz.
 - i. Suppose that the receiver decodes one of the users' signal (signal 1) and the second user's signal acts as AWGN. What is the capacity of the channel associated with the decoded signal 1?
 - ii. Suppose that after decoding signal 1, the decoder re-encodes it and subtracts it from the received signal, what is the Shannon capacity of the second user's channel? [2]

4. Answer the following subquestions.

- (a) Consider the third generation wideband UTRA/FDD radio system and describe how the User Equipment, when it is first turned on, identifies the random access physical channel parameters using the following channels:
 - i. the Primary Synchronization Channel, [1]
 - ii. the Secondary Synchronization Channel, [1]
 - iii. the Pilot Channel, [1]
 - iv. the Primary Common Control Physical Channel (PCCPCH), [1]
 - v. the Secondary Common Control Physical Channel (SCCPCH).
- (b) In connection with the Global Systems Mobile (GSM) radio system, explain
 - i. the framing structure for the control channel, [1]
 - ii. how the logical control channels are multiplexed over the physical channel. [2]
 - iii. how the network switching subsystem is modified to handle packet transmission for use in the General Packet Radio Service (GPRS).
- (c) Consider a wideband direct sequence spread spectrum (WCDMA) system, where a total of Kspreading signature waveforms are used to spread the information data bits over the downlink. Assume that both transmitter and receiver have knowledge of both the channel gain, h_k , and the channel-SNR, $\frac{h_k}{\sigma^2}$, for each code where the term σ^2 is the noise variance. Given that the transmitter adjusts the transmission power P_k for each code k while maintaining a minimum SNIR requirement $\gamma_k^* \geq 0$ at the output of the receiver detector in accordance with the Perron-Frobenius theorem, produce an expression for the power P_k as a function of the inverse-channel-SNR.
- (d) Describe how the sum-capacity for random CDMA codes is upper bounded by the Welch-Bound-Equality limit. [3]
 - Explain how the iterative water filling and the discrete bit loading algorithms can be used to maximize the sum-capacity for random parallel codes in WCDMA systems.

[4]

[4]

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Paper Code 4.03 [1643 5010 ASS

K.K. LEUNG Second Examiner

Question

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Marks allocations in right margin

$$\begin{array}{l} (a) & \text{Signac NULLS occur when } \Delta \beta = (2n+1)\pi \\ & \frac{2\pi}{\lambda} \left[\sqrt{(h_{\xi}+h_{r})^{2}+d^{2}} - \sqrt{(h_{\xi}-h_{r})^{2}+d^{2}} = \pi(2n+1) \right] \\ & \frac{2\pi}{\lambda} \left[\sqrt{(h_{\xi}+h_{r})^{2}+d^{2}} - \sqrt{(h_{\xi}-h_{r})^{2}+d^{2}} = \frac{\lambda}{2}(2n+1) \right] \\ & \sqrt{(h_{\xi}+h_{r})^{2}+d^{2}} - \sqrt{(h_{\xi}-h_{r})^{2}+d^{2}} = \frac{\lambda}{2}(2n+1) \\ & \text{Let } m = (2n+1) \\ & \sqrt{(h_{\xi}+h_{r})^{2}+d^{2}} = m\frac{\lambda}{2} + \sqrt{(h_{\xi}-h_{r})^{2}+d^{2}} \\ & \text{Square both sides} \\ & (h_{\xi}+h_{r})^{2} + d^{2} = m^{2}\frac{\lambda^{2}}{4} + (h_{\xi}-h_{r})^{2} + d^{2} + m\lambda\sqrt{(h_{\xi}-h_{r})^{2}+d^{2}} \\ & \times = (h_{\xi}+h_{r})^{2}, \quad \forall = (h_{\xi}-h_{r})^{2}, \quad \times - \forall = 4h_{\xi}h_{r} \\ & \times = m^{2}\frac{\lambda^{2}}{4} + y + m\lambda\sqrt{\forall + d^{2}} \\ & \Rightarrow d = \sqrt{\left[\frac{1}{m\lambda}(x-m^{2}\frac{\lambda^{2}}{4}-y)\right]^{2}-y} \\ & d = \sqrt{\left[\frac{4h_{\xi}h_{r}}{(2n+1)\lambda} - \frac{(2n+1)\lambda}{4}\right]^{2} - \left(h_{\xi}-h_{r}\right)^{2}, \quad n \in \mathbb{Z}$$

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d-1

$$\frac{P_r}{P_t}dB = 10 \log_{10} k - 10 Y \log_{10} \frac{d}{d_0}$$
using least squares we get
$$10 \log_{10} k = -29.42 dB$$

li

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Receiver power can be assumed to be Goussian with voriance of 2

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1.C
$$h(c) = x, S(t-7) + x_2 S(t-(2+0.22/45))$$
 $G_r = G_c = 1$
 $h_{x} = h_r = 8m$
 $f_c = 900 \text{ MHz}, \quad \lambda = C/f_c = 1/2, \quad \lambda = -1$
 $belay spread = \frac{x+x'-L}{C} = 0.022 \times 10^6 \text{ s}$
 $\Rightarrow 2\sqrt{8^2+(\frac{d}{2})^2} - d = 0.022 \times 10^6 \text{ s}$
 $\Rightarrow d = 16.1 \text{ m}$
 $\therefore \quad \tau = \frac{d}{c} = 53.67 \text{ n s}$
 $x = (\frac{\lambda}{4\pi}) \frac{(G_L)^2}{L} = 2.71 \times 10^6$
 $x = (\frac{\lambda}{4\pi}) \frac{(R.G_r)}{X+X'} = 1.37 \times 10^6$

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2.0

$$C = \sqrt{10^{\frac{P_0 - P_1}{10}}} =$$

$$C = \sqrt{\frac{(P_0 - P_1)}{10^{-10}}} = \frac{C = \sqrt{10^{-3}} = 0.03/17 \quad f_0 = 0.000}{C = \sqrt{10^{-13}} = 0.1778 \quad f_0 = 15.00}$$

$$P_0 = 0 dBm$$
, $\overline{t}_2 = \frac{e^2 - 1}{\ell f_B \sqrt{2\pi}} = 0.00135$

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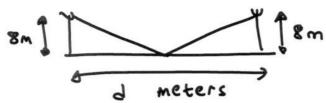
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2.6

$$S(\gamma,\ell) = \begin{cases} x, S(\gamma) & \ell = 70 \text{ Hz} \\ x_2 S(\gamma - 0.022 \mu) & \ell = 49.5 \text{ Hz} \\ 0 & \text{else} \end{cases}$$

The antenna set up is



From the figure, the distance travalled by the Los ray is d and the distance travalled by the first multipath component is

Given this set up, we can plot the arrival of the LOS ray and the multipath ray that bounces of the ground on a time axis as Shown in the above diagram. So we have

$$2\sqrt{\left(\frac{d}{2}\right)^{2}+8^{2}}-d=0.022\times10^{3}\times3\times10^{8}$$

$$=>4\left(\frac{d^{2}}{4}+8^{2}\right)=6.6+d^{2}+2d(6.6)$$

$$=>d=16.1 \text{ m}.$$

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MODEL ANSWER and MARKING SCHEME Confidential Paper Code 4.03 M. K. GULCAN First Examiner Question 2. Page 6 out of 6 K.K. LEUNG **Second Examiner** Marks allocations in right margin Ouestion labels in left margin 2-b Jed fn= 1 ws(+)/> u= f, //ws(+). For the LOS ray, \$=0 and for the multipath component, \$=45°. We can use either of these rays and the corresponding for value to get v= 23.33 m/s. dc = 768 m. Since d<<dc, power four-off is proportional to d'? Tm = 0.022 Ms, B = 0.33 Ms. Since TMCC BI, we have feat fading.

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Question 2.6 Page

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Tm ~ Oil msec = 100 usec B1 2 0.1 HZ Answers based on the or of are fine too. Notice, that based on the choice of either Tm, / or of, the remaining answers will be different too. BC = 1 = 10 KHZ. Sf>10 kHz for u, Luz Lii (At) = 10 S LU 3 KILL B => flat 30 KHZ> B_ => frequency selective. 15(2,p)

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3,9

Noise = 50 x10 x 2 x10 = 0.1 w

Signal = 0.01 W

SNR = 0.01/0.1 = 0.1

C= 50x log (1+0.1) = 6.8752 Mbps Doubling power C=50 xlog, (1+0.2)

Pnew= 20 mW, C= 13.1517 (for XCCL, log(HX)2X)

capacity increase = 13.1517 - 6.8752 = 6.2765 Mbps

B= 100 NHz, Notice that both the bandwists noise power will increase. So C= 7mbps

-11/____

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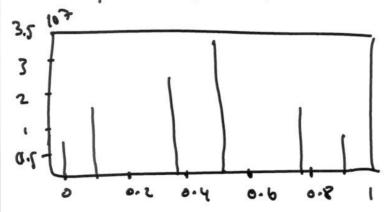
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Marks allocations in right margin

We suppose that all channel states are used

$$\frac{1}{V_0} = 1 + \sum_{i=1}^{4} \frac{1}{V_i} P_i \implies V_0 = 0.8109$$

$$\frac{\overline{P}}{\overline{P}} = \frac{R^0}{\Gamma} - \frac{R^0}{\Gamma}$$



$$\frac{P(Y)}{3} = \begin{cases} 1.2322 & Y = Y_1 \\ 1.2322 & Y = Y_2 \\ 1.1332 & Y = Y_4 \end{cases}$$
0.2332 $Y = Y_4$

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$$\sigma = \frac{1}{E[\frac{1}{8}]} = 4.2882$$

$$\frac{P(8i)}{=} = \frac{5}{12}$$

$$\frac{P(r)}{\overline{P}} = \begin{cases} 0.0043 & 8 = 8_1 \\ 0.0029 & 8 = 8_2 \\ 0.4288 & 8 = 8_4 \end{cases}$$

$$\frac{P(r)}{P} = \begin{cases} 0.0043 & 8 = 8_1 \\ 0.0029 & 8 = 8_2 \end{cases}$$

3.6

To have Pout=0.1 or 0.01 we will have to use all the sub-channels as leaving any of these will result in a Port of at least 0.2 .. truncated channel power control policy and associated spectral efficiency are the same as zero-outage case in part b. To have put that maximizes C with truncated channel inversion, we get

max = 4.1462 bps/Hz, Pout=0.5

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$$\frac{C_7}{B} = (0.3 + 0.2) \times \log_2 \left(1 + \frac{1}{0.2} + \frac{0.3}{10^2} \right)$$

$$= 0.5 \log_2 \left(1 + \frac{1}{0.0032} \right)$$

$$Y_{1} = 10$$
 $P_{2} = 0.2$
 $Y_{2} = 10$
 $P_{3} = 0.3$
 $Y_{3} = 10$
 $P_{3} = 0.3$
 $Y_{4} = 1$
 $P_{4} = 0.4$

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4.0	i) book work. primary synchronization channel is used to get slot timing information li) secondary synchronization channel is used to get frame timing information.
	iii) Pilot channel is used to get primary scrambling code information.
	iv) Primary Common broad coust channel is used to pet the Channela zation codes for the random access channel.
	v) Secondary control chanel is used to transfer information over forward access und random access ununels.
4.6	ii) each frame consists of 8 slots.
/	51 frames is a multiframe
	26 multi frames is a super frame.
	(i) Each multi frame is organized as
	follows
	11 frequency correction channel
	(1 Synchronization channel
	channels 4 Broadast channels
	10 Synchronization channel channels 4 Broadast channels 4 Paping channels
	above arrangement is repeated five times.
	1.00

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Second Examiner K.K. LEUNG Question 4.1 Page 14 out of 16

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Hill WBE

$$k \leq \log_2(1+V_k) = \frac{1}{2}\log_2(1+\frac{V_k}{N})$$
 $k \geq \log_2(1+V_k) = \frac{1}{2}\log_2(1+\frac{V_k}{N})$
 $k \geq \log_2(1+\frac{V_k}{N})$
 $k \leq \log_2(1+\frac{V_k}{N})$
 k

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Discrete bit looking. 4.4 SNRs on each Sub-channel QK = [QKXI] , where QK = 1 log (1+ 8k) Yk=[8kx1], where Yk=6(2-1) γ_{k2} h_k ρ_k (w_i, ζ_i)² + σ² (ω_iω_i) equating two sur equations lead to G (2 -1) = hk Pk (wic Sk)2

\[
\begin{align*}
\lefth{h_{ic} P_{i} \left(\omega_{ic} S_{ic} \right)^{2} + v^{2} \left(\omega_{ic} \omega_ Re organise equation. (Z-F) P= U fu,j = [FKxk] = { (22ak) (wiss) Uk = 026(220k - 1) WK WK

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4.1

P= (1-+)-1 u everta giztupation

E(Q)=TP=T(I-P) 4 incremental energy

2(Q) = 2(Q+B,+V,)- 2(A) S = 2 2 11

Algoritum

SESTEM (Q) if SCE, then.

Q(Q+(Br+1-Brm) VM

else

break.

ent white

Ret 8.

I enia de