## Special Information for Invigilators: none.

## Information for Candidates

VHDL language reference and course notes can be found in the booklet VHDL Exam Notes.

Unless otherwise specified assume VHDL 1993 compiler.

Library functions from the VHDL package utility_pack from the coursework may be used freely in your implementations.

## The Questions

## Question 1 is COMPULSORY

1. a)
(i) Determine the precise behaviours of processes P1 \& P2 in Figure 1.1, assuming that z is initially ' 0 '. Is P1 synthesisable?
(ii) You may assume that synthesis of a VHDL process depends only on its precise behaviour in simulation. State, giving reasons, whether P2 is synthesisable?
b) Figure 1.2 shows a random access memory entity ram with data output dout and control input write, address input addr and data input din. In ram what is the width of one memory location and the number of memory locations? Write a synthesisable architecture for entity ram implementing the function shown in Figure 1.2.
c) Calculate the ROBDD for the Boolean expression:

X xor Y xor $Z$ xor $W$
with variable order X, Y, Z, W
d) You may assume that $a, b, c, d$ in Figure 1.3 are all ' 0 ' at the start of simulation. Draw the first 20ns of the waveforms on these signals when driven by process P3, annotating each signal transition with its physical time and indicating the simulation $\Delta$ of the transition if this is not 0 .
e) Entity iobuff in Figure 1.4 has ports $z a, z b$ which are both inputs and (tri-state) clocked outputs. Its behaviour is described in Figure 1.5 where the notation $x_{i}$ denotes the value on signal $x$ during clock cycle $i$. Write an architecture for iobuff consistent with Figure 1.5.

```
P1:PR0CESS
BEGIN
    WAIT UNTIL clk'EVENT;
    z <= not z;
END PROCESS P1;
```

```
P2:PROCESS
BEGIN
    WAIT UNTIL clk'EVENT;
    IF clk='1' THEN
        z <= not z;
    END IF;
END PROCESS P2;
```

Figure 1.1

```
ENTITY ram IS
PORT(
            write, clk: IN std_logic;
            addr: IN std_logic_vector(3 DOWNTO 0);
            din: IN std_logic_vector(7 DOWNTO 0);
            dout: OUT std_logic_vector(7 DOWNTO 0)
);
END ram;
```

| write | Operation on next clock positive edge | Dout in current cycle |
| :--- | :--- | :--- |
| 1 | ramloc[addr] $:=$ din | ramloc[addr] |
| 0 | n/a | ramloc[addr] |

Figure 1.2

```
P3:PROCESS
    VARIABLE XV : std_logic;
BEGIN
    WAIT FOR 10 ns;
    XV := a;
    a <= not xv;
    b <= not a;
    WAIT FOR 0 ns;
    c <= b;
    d <= b AFTER 5 ns;
END PROCESS P3;
```

Figure 1.3

```
ENTITY iobuff IS
    PORT(dir,clk:IN std_logic;
            za,zb:INOUT std_logic
);
END iobuff;
```

Figure 1.4

| dir $_{n}$ | ${z a_{n}}^{z b_{n}}$ |  |
| :--- | :--- | :--- |
| 1 | $\mathrm{zb}_{\mathrm{n}-1}$ | High <br> impedance |
| 0 | High <br> impedance | $\mathrm{za}_{\mathrm{n}-1}$ |

Figure 1.5

## Students must answer TWO out of Questions 2-4.

2. Figure 2.2 shows an implementation of entity transpose in Figure 2.1. This uses a 16 word RAM tram to implement 4X4 matrix transposition. The circuit is synchronous with the negative edge of clk. The operation is initiated by a '1' on reset and controlled by finite state machine fsm with three states as in Figure 2.3. Note that the double vertical lines indicate where clock cycles have been omitted.

During state1, the16 matrix elements each of width 16 bits are input sequentially on din in row order and written to the RAM. In state2 the 16 matrix elements are output in column order. As this happens all 16 elements are summed in block alureg. In state3, lasting 1 cycle, the sum is output. The address inputs of tram are driven by a block amux which permutes address inputs in state 2 to implement the transposed element order. Block muxd selects the appropriate signal for dout.
a) Write appropriate VHDL to define type word as a 16 bit vector which can be used in entities instantiating transpose as well as the entity and architecture of transpose and tram.
b) The RAM tram is implemented as a separate entity. Write an appropriate entity declaration for tram. You do not need to write an architecture for tram.
c) Write an architecture for transpose which instantiates tram and implements blocks amux, muxd, fsm, alureg, and count.

```
ENTITY transpose IS
    PORT (
        clk, reset : IN STD_LOGIC;
        datain : IN word;
        dataout : OUT word
        );
END transpose;
```

Figure 2.1
reset (not shown) controls


Figure 2.2


Figure 2.3
3. Figure 3.1 illustrates a hardware engine to compute the Mandelbrot fractals which implements repeatedly two complex number iterations each of the form:

$$
\begin{align*}
& z_{r}^{\prime}:=\operatorname{round}\left\{\left(z_{r} * z_{r}-z_{i}^{*} z_{i}\right) * 2^{-n}\right\}+c_{r}  \tag{3.1}\\
& z_{i}^{\prime}:=\operatorname{round}\left\{2 z_{i}^{*} z_{r}^{*} * 2^{-n}\right\}+c_{i}
\end{align*}
$$

where $z_{i}, c_{i}, z_{r}, c_{r}$ are two's complement $m$-bit signed integers representing imaginary and real parts of (fixed point) complex numbers $z$ and $c$ respectively, and $z^{\prime}$ is the new value of $z$. The function round implements rounding to the nearest signed integer.
a) A fixed-point signed vector $x(m-1: 0)$ with $n$ fractional bits ( $n<m$ ) may be rounded to the nearest fixed-point integer by adding bit $x(n-1)$ onto $x$ at bit index n , and setting the bottom $n$ bits to 0 . Write a VHDL function:

## FUNCTION roundn(n: INTEGER; x: SIGNED) RETURN SIGNED;

which rounds a signed fixed point vector $x$ to the nearest integer.
b) Figure 3.1 shows hardware to implement Equation (3.1). The multiplier blocks compute products $z_{i}{ }^{*} z_{i}, z_{i}{ }^{*} z_{r}, z_{r}{ }^{*} z_{r}$, which are held in REG1. The block COUNT is a one bit counter. Block $A S R$ computes the new values $z_{i}^{\prime}, z_{r}^{\prime}$ from these products and the complex constant $c$, which is output from multiplexer MUX. Supposing complex inputs $c a$ and $c b$ are constant, determine the output of REG2 for the first four clock cycles after reset. Hence explain how the circuit computes Equation (3.1).
c) Define a VHDL type complex which implements a complex number as an array of two signed vectors, each of length $m$, where $m$ is a constant.
d) You may assume that the VHDL operator :
*: signed $\times$ signed $\rightarrow$ signed
synthesises signed multipliers. The length of the result is the sum of the lengths of the two operands. Using the * operator and previous answers from this question write a VHDL architecture for the entity in Figure 3.2 which implements Figure 3.1.


Figure 3.1

```
ENTITY mandelbrot IS
    GENERIC( n : INTEGER); -- precision
    PORT(
        ca, cb : IN complex;
        z : OUT complex;
        reset, clk: IN std_logic;
        casel: OUT std_logic -- '1' when ca is selected
        );
END mandelbrot;
```

Figure 3.2
(a) Explain how in VHDL constant expressions are synthesised differently from signals whose value may change:
(i) as indexes of arrays
(ii) as operands of logical operators.

Specify three distinct contexts in which VHDL identifiers can represent constant expressions.
(b) Figure 4.1 shows VHDL entity and architecture permute which has $k$ bit input $a$ and output $b$. Precisely what hardware will this synthesise if
(i) $k=2, m=1$
(ii) $k=4, m=2$
(c) Entity switch in Figure 4.3 uses multiple permute blocks all with $k=2, m=1$. It connects $2^{n}$ inputs $a$ to $2^{n}$ outputs $b$ and is made up of $n$ layers labelled 0 to $n-1$ each containing $2^{n-1}$ copies of permute with identical $p$ input as illustrated in Figure 4.2, where the dots indicate repeated blocks which have been omitted. Between layers $q$ and $q+1$ there is an array of $2^{n}$ signals $x(q)$. You are given synthesisable functions $\mathbf{x 0}(\mathbf{q}, \mathbf{i})$ and $\mathbf{x 1}(\mathbf{q}, \mathbf{i})$ which determine the connections of the permute blocks. In layer $q$, the $i$ ith copy of permute ( $i=$ $0, \ldots, 2^{\mathrm{n}-1}$ ) is connected as in Figure 4.4.

Using one or more FOR GENERATE loops, complete architecture synth in Figure 4.3 using synthesisable code.

|  | index 0 | index 1 |
| :---: | :---: | :---: |
| xin | $x(q)(x 0(q, i))$ | $x(q)(x 1(q, i))$ |
| xout | $x(q+1)(x 0(q, i))$ | $x(q+1)(x 1(q, i))$ |

Figure 4.4

```
ENTITY permute IS
GENERIC(k,m:INTEGER);
PORT (
        p : IN std_logic_vector(m-1 DOWNTO 0);
        xin : IN std_logic_vector(k-1 DOWNTO 0);
        xout : OUT std_logic_vector(k-1 DOWNTO 0)
    );
END permute;
ARCHITECTURE behave OF permute IS BEGIN
        G1: FOR i IN k DOWNTO 1 GENERATE
        xout(i-1) <= xin((i*(conv_integer(unsigned((p)))+1) mod k+1)-1);
        END GENERATE G1;
END behave;
```

Figure 4.1


Figure 4.2

```
ENTITY switch IS
    GENERIC(n: INTEGER);
    PORT( a: IN std_logic_vector(2**n-1 DOWNTO 0);
        b: OUT std_logic_vector(2**n-1 DOWNTO 0);
        sel: IN std_logic_vector(n-1 DOWNT0 0) );
END switch;
ARCHITECTURE synth OF switch IS
    TYPE grid IS ARRAY (0 TO n+1) OF std_logic_vector(2**n-1 DOWNTO 0);
    SIGNAL x: grid;
BEGIN
END synth;
```

Figure 4.3

