UNIVERSITY OF BRADFORD

DERIVATIVES PRICING AND RISK MANAGEMENT (MSc)

MAN4258M

14th May 2014 **16:00 – 17:30 hours**

Main

This is a **CLOSED BOOK** examination

Available time: 1½ hour

You should attempt any **TWO** questions from the **FOUR** available. All questions are equally weighted.
You should answer every part of the question you attempt.

If you attempt more than two questions, then you will be awarded marks for your two highest scoring answers.

Marks are awarded for complete answers and not "just for the final result". A complete answer defines the notation, specifies the assumptions used, clearly explains the steps involved in the calculation, and provides a reasonable interpretation of the result, where relevant.

No programmable calculators are permitted.

Tables of the cumulative standard Normal distribution are appended.

Use the 30/360 day convention for all financial calculations.

You should attempt any TWO questions from the FOUR available.

Question 1

a. Describe the main characteristic features of a FRA (Forward Rate Agreement) having an implied loan period of 3 months.

[Weighting: 25%]

b. Describe the main characteristic features of a 3-month Euro-Dollar Futures contract.

[Weighting: 25%]

c. What are the critical differences between the FRA and the Euro-Dollar Futures contract at settlement.

[Weighting: 10%]

d. The following annualized spot interest rates are for various maturities are recorded:

Maturity	Spot rate
3 months	1.60%
6 months	1.80%
9 months	1.90%
12 months	2.00%
15 months	2.05%
18 months	2.10%

Using the 30/360 day convention, determine the annualized 12 month forward interest rate for a 3 month loan period.

[Weighting: 10%]

e. Using your result of part (d), determine the price for a 3-month Euro-Dollar Futures contract having a 12-month maturity.

[Weighting: 10%]

f. A firm negotiates a £100 million 3-month borrowing contract based on a 12×15 FRA. Using the rates recorded in part (d), determine the gain (loss) on this contract at settlement if the prevailing annualized 3-month spot interest rate at settlement is 2.4%.

[Weighting: 20%]

Question 2

a. Describe the main features of a plain vanilla interest rate swap.

[Weighting: 20%]

b. Explain why a firm concerned with interest rate exposure may be more willing to use an interest rate swap rather than separate FRA (Forward Rate Agreement) contracts.

[Weighting: 10%]

c. Swap contracts are subject to counter-party risk. Discuss the nature of this risk and the ways it can be mitigated and reduced in practice.

[Weighting: 10%]

d. The Kweli Investment Bank (KIB) negotiates a plain vanilla interest rate swap deal with one of its clients. KIB is the floating-rate payer, while the client is the fixed-rate payer. The swap contract based on a notional principal of £100 million has a maturity of 8 years, and cash flows are exchanged every 6 months of the contract, starting 6 months following the date of origination. The relevant zero-coupon bond prices for various maturities are recorded in the following table, where the notional principal is 100. Determine the swap rate as an annualized figure.

Maturity (Years)	Zero Coupon Bond Price
0.5	98.25
1.0	96.43
1.5	94.42
2.0	92.28
2.5	90.01
3.0	87.63
3.5	85.44
4.0	83.22
4.5	80.98
5.0	79.10
5.5	77.27
6.0	75.05
6.5	73.28
7.0	71.54
7.5	69.85
8.0	67.68

[Weighting: 30%]

e. 4 years after the date of origination, immediately following a cash flow exchange, KIB re-assesses its position to determine whether the bank has gained or lost money on the swap contract. The zero-coupon bond prices for various maturities prevailing at that time are recorded in the following table, where again the notional principal is 100. Determine whether or not the bank's swap value has gain, and the amount of that gain (loss). Explain why KIB has gained or lost on the swap contract.

Maturity (Years)	Zero Coupon Bond Price
0.5	98.06
1.0	96.06
1.5	94.02
2.0	91.92
2.5	89.79
3.0	87.38
3.5	84.30
4.0	80.72
4.5	76.93
5.0	73.68
5.5	70.36
6.0	67.39
6.5	64.42
7.0	62.27
7.5	60.20
8.0	58.20

[Weighting: 30%]

Question 3

a. Describe the main features of an option contract.

[Weighting: 20%]

b. Explain why American and European style option can have different prices. Which is more expensive, and why?

[Weighting: 10%]

c. An asset paying a continuous dividend of 2% is currently priced at 100p, and its annual volatility is 32%. A binomial lattice having 4 equal steps is constructed for valuing a 6 month maturity option on the underlying asset, with an exercise price of 103p. The continuous risk-free rate is 6%. The price evolution for this asset, assuming no dividend is paid, is presented below as an array:

0	1	2	3	4
100.00	111.98	125.39	140.41	157.23
	89.30	100.00	111.98	125.39
		79.75	89.30	100.00
			71.22	79.75
				63.60

Find the values for the relevant risk-neutral probabilities.

[Weighting: 10%]

d. The derivation of the American call option values is partly presented in the following array:

0	1	2	3	4
			37.83	54.23
	2.64	5.38	10.98	22.39
		0.00	0.00	0.00
			0.00	0.00
				0.00

Complete the missing entries and identify the American call option premium at origination. Is the call exercised early? If so, when?

[Weighting: 30%]

e. The derivation of the American put option values is partly presented in the following array:

0	1	2	3	4
	4.20	0.76	0.00	0.00
		7.62	1.51	0.00
			13.70	3.00
			31.78	23.25
				39.40

Complete the missing entries and identify the American put option premium at origination. Is the put exercised early? If so, when?

[Weighting: 30%]

Question 4

Discuss each of the following terms:

a. Geometric Brownian motion process for describing asset prices.

[Weighting: 20%]

b. Self-financing, dynamic, replicating portfolio.

[Weighting: 20%]

c. Collar contract, or buying a call and selling a put on the same asset with identical maturity dates, but at different exercise prices.

[Weighting: 20%]

d. Delta hedging.

[Weighting: 20%]

e. Binary option.

[Weighting: 20%]

Table of the cumulative standard Normal distribution N(x) for x ≤ 0

	0.00	-0.01	-0.02	-0.03	-0.04	-0.05	-0.06	-0.07	-0.08	-0.09
0.0	0.50000	0.49601	0.49202	0.48803	0.48405	0.48006	0.47608	0.47210	0.46812	0.46414
-0.1	0.46017	0.45620	0.45224	0.44828	0.44433	0.44038	0.43644	0.43251	0.42858	0.42465
-0.2	0.42074	0.41683	0.41294	0.40905	0.40517	0.40129	0.39743	0.39358	0.38974	0.38591
-0.3	0.38209	0.37828	0.37448	0.37070	0.36693	0.36317	0.35942	0.35569	0.35197	0.34827
-0.4	0.34458	0.34090	0.33724	0.33360	0.32997	0.32636	0.32276	0.31918	0.31561	0.31207
-0.5	0.30854	0.30503	0.30153	0.29806	0.29460	0.29116	0.28774	0.28434	0.28096	0.27760
-0.6	0.27425	0.27093	0.26763	0.26435	0.26109	0.25785	0.25463	0.25143	0.24825	0.24510
-0.7	0.24196	0.23885	0.23576	0.23270	0.22965	0.22663	0.22363	0.22065	0.21770	0.21476
-0.8	0.21186	0.20897	0.20611	0.20327	0.20045	0.19766	0.19489	0.19215	0.18943	0.18673
-0.9	0.18406	0.18141	0.17879	0.17619	0.17361	0.17106	0.16853	0.16602	0.16354	0.16109
-1.0	0.15866	0.15625	0.15386	0.15151	0.14917	0.14686	0.14457	0.14231	0.14007	0.13786
-1.1	0.13567	0.13350	0.13136	0.12924	0.12714	0.12507	0.12302	0.12100	0.11900	0.11702
-1.2	0.11507	0.11314	0.11123	0.10935	0.10749	0.10565	0.10383	0.10204	0.10027	0.09853
-1.3	0.09680	0.09510	0.09342	0.09176	0.09012	0.08851	0.08691	0.08534	0.08379	0.08226
-1.4	0.08076	0.07927	0.07780	0.07636	0.07493	0.07353	0.07215	0.07078	0.06944	0.06811
-1.5	0.06681	0.06552	0.06426	0.06301	0.06178	0.06057	0.05938	0.05821	0.05705	0.05592
-1.6	0.05480	0.05370	0.05262	0.05155	0.05050	0.04947	0.04846	0.04746	0.04648	0.04551
-1.7	0.04457	0.04363	0.04272	0.04182	0.04093	0.04006	0.03920	0.03836	0.03754	0.03673
-1.8	0.03593	0.03515	0.03438	0.03362	0.03288	0.03216	0.03144	0.03074	0.03005	0.02938
-1.9	0.02872	0.02807	0.02743	0.02680	0.02619	0.02559	0.02500	0.02442	0.02385	0.02330
-2.0	0.02275	0.02222	0.02169	0.02118	0.02068	0.02018	0.01970	0.01923	0.01876	0.01831
-2.1	0.01786	0.01743	0.01700	0.01659	0.01618	0.01578	0.01539	0.01500	0.01463	0.01426
-2.2	0.01390	0.01355	0.01321	0.01287	0.01255	0.01222	0.01191	0.01160	0.01130	0.01101
-2.3	0.01072	0.01044	0.01017	0.00990	0.00964	0.00939	0.00914	0.00889	0.00866	0.00842
-2.4	0.00820	0.00798	0.00776	0.00755	0.00734	0.00714	0.00695	0.00676	0.00657	0.00639
-2.5	0.00621	0.00604	0.00587	0.00570	0.00554	0.00539	0.00523	0.00508	0.00494	0.00480
-2.6	0.00466	0.00453	0.00440	0.00427	0.00415	0.00402	0.00391	0.00379	0.00368	0.00357
-2.7	0.00347	0.00336	0.00326	0.00317	0.00307	0.00298	0.00289	0.00280	0.00272	0.00264
-2.8	0.00256	0.00248	0.00240	0.00233	0.00226	0.00219	0.00212	0.00205	0.00199	0.00193
-2.9	0.00187	0.00181	0.00175	0.00169	0.00164	0.00159	0.00154	0.00149	0.00144	0.00139
-3.0	0.00135	0.00131	0.00126	0.00122	0.00118	0.00114	0.00111	0.00107	0.00104	0.00100
-3.1	0.00097	0.00094	0.00090	0.00087	0.00084	0.00082	0.00079	0.00076	0.00074	0.00071
-3.2	0.00069	0.00066	0.00064	0.00062	0.00060	0.00058	0.00056	0.00054	0.00052	0.00050
-3.3	0.00048	0.00047	0.00045	0.00043	0.00042	0.00040	0.00039	0.00038	0.00036	0.00035
-3.4	0.00034	0.00032	0.00031	0.00030	0.00029	0.00028	0.00027	0.00026	0.00025	0.00024
-3.5	0.00023	0.00022	0.00022	0.00021	0.00020	0.00019	0.00019	0.00018	0.00017	0.00017
-3.6	0.00016	0.00015	0.00015	0.00014	0.00014	0.00013	0.00013	0.00012	0.00012	0.00011
-3.7	0.00011	0.00010	0.00010	0.00010	0.00009	0.00009	0.00008	0.00008	0.00008	0.00008
-3.8	0.00007	0.00007	0.00007	0.00006	0.00006	0.00006	0.00006	0.00005	0.00005	0.00005
-3.9	0.00005	0.00005	0.00004	0.00004	0.00004	0.00004	0.00004	0.00004	0.00003	0.00003
-4.0	0.00003	0.00003	0.00003	0.00003	0.00003	0.00003	0.00002	0.00002	0.00002	0.00002

Table of the cumulative standard Normal distribution N(x) for x ≥ 0

	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.50000	0.50399	0.50798	0.51197	0.51595	0.51994	0.52392	0.52790	0.53188	0.53586
0.1	0.53983	0.54380	0.54776	0.55172	0.55567	0.55962	0.56356	0.56749	0.57142	0.57535
0.2	0.57926	0.58317	0.58706	0.59095	0.59483	0.59871	0.60257	0.60642	0.61026	0.61409
0.3	0.61791	0.62172	0.62552	0.62930	0.63307	0.63683	0.64058	0.64431	0.64803	0.65173
0.4	0.65542	0.65910	0.66276	0.66640	0.67003	0.67364	0.67724	0.68082	0.68439	0.68793
0.5	0.69146	0.69497	0.69847	0.70194	0.70540	0.70884	0.71226	0.71566	0.71904	0.72240
0.6	0.72575	0.72907	0.73237	0.73565	0.73891	0.74215	0.74537	0.74857	0.75175	0.75490
0.7	0.75804	0.76115	0.76424	0.76730	0.77035	0.77337	0.77637	0.77935	0.78230	0.78524
0.8	0.78814	0.79103	0.79389	0.79673	0.79955	0.80234	0.80511	0.80785	0.81057	0.81327
0.9	0.81594	0.81859	0.82121	0.82381	0.82639	0.82894	0.83147	0.83398	0.83646	0.83891
1.0	0.84134	0.84375	0.84614	0.84849	0.85083	0.85314	0.85543	0.85769	0.85993	0.86214
1.1	0.86433	0.86650	0.86864	0.87076	0.87286	0.87493	0.87698	0.87900	0.88100	0.88298
1.2	0.88493	0.88686	0.88877	0.89065	0.89251	0.89435	0.89617	0.89796	0.89973	0.90147
1.3	0.90320	0.90490	0.90658	0.90824	0.90988	0.91149	0.91309	0.91466	0.91621	0.91774
1.4	0.91924	0.92073	0.92220	0.92364	0.92507	0.92647	0.92785	0.92922	0.93056	0.93189
1.5	0.93319	0.93448	0.93574	0.93699	0.93822	0.93943	0.94062	0.94179	0.94295	0.94408
1.6	0.94520	0.94630	0.94738	0.94845	0.94950	0.95053	0.95154	0.95254	0.95352	0.95449
1.7	0.95543	0.95637	0.95728	0.95818	0.95907	0.95994	0.96080	0.96164	0.96246	0.96327
1.8	0.96407	0.96485	0.96562	0.96638	0.96712	0.96784	0.96856	0.96926	0.96995	0.97062
1.9	0.97128	0.97193	0.97257	0.97320	0.97381	0.97441	0.97500	0.97558	0.97615	0.97670
2.0	0.97725	0.97778	0.97831	0.97882	0.97932	0.97982	0.98030	0.98077	0.98124	0.98169
2.1	0.98214	0.98257	0.98300	0.98341	0.98382	0.98422	0.98461	0.98500	0.98537	0.98574
2.2	0.98610	0.98645	0.98679	0.98713	0.98745	0.98778	0.98809	0.98840	0.98870	0.98899
2.3	0.98928	0.98956	0.98983	0.99010	0.99036	0.99061	0.99086	0.99111	0.99134	0.99158
2.4	0.99180	0.99202	0.99224	0.99245	0.99266	0.99286	0.99305	0.99324	0.99343	0.99361
2.5	0.99379	0.99396	0.99413	0.99430	0.99446	0.99461	0.99477	0.99492	0.99506	0.99520
2.6	0.99534	0.99547	0.99560	0.99573	0.99585	0.99598	0.99609	0.99621	0.99632	0.99643
2.7	0.99653	0.99664	0.99674	0.99683	0.99693	0.99702	0.99711	0.99720	0.99728	0.99736
2.8	0.99744	0.99752	0.99760	0.99767	0.99774	0.99781	0.99788	0.99795	0.99801	0.99807
2.9	0.99813	0.99819	0.99825	0.99831	0.99836	0.99841	0.99846	0.99851	0.99856	0.99861
3.0	0.99865	0.99869	0.99874	0.99878	0.99882	0.99886	0.99889	0.99893	0.99896	0.99900
3.1	0.99903	0.99906	0.99910	0.99913	0.99916	0.99918	0.99921	0.99924	0.99926	0.99929
3.2	0.99931	0.99934	0.99936	0.99938	0.99940	0.99942	0.99944	0.99946	0.99948	0.99950
3.3	0.99952	0.99953	0.99955	0.99957	0.99958	0.99960	0.99961	0.99962	0.99964	0.99965
3.4	0.99966	0.99968	0.99969	0.99970	0.99971	0.99972	0.99973	0.99974	0.99975	0.99976
3.5	0.99977	0.99978	0.99978	0.99979	0.99980	0.99981	0.99981	0.99982	0.99983	0.99983
3.6	0.99984	0.99985	0.99985	0.99986	0.99986	0.99987	0.99987	0.99988	0.99988	0.99989
3.7	0.99989	0.99990	0.99990	0.99990	0.99991	0.99991	0.99992	0.99992	0.99992	0.99992
3.8	0.99993	0.99993	0.99993	0.99994	0.99994	0.99994	0.99994	0.99995	0.99995	0.99995
3.9	0.99995	0.99995	0.99996	0.99996	0.99996	0.99996	0.99996	0.99996	0.99997	0.99997
4.0	0.99997	0.99997	0.99997	0.99997	0.99997	0.99997	0.99998	0.99998	0.99998	0.99998