

2011 Mathematics

Intermediate 1 Units 1, 2 & Applications Paper 2

Finalised Marking Instructions

© Scottish Qualifications Authority 2011

The information in this publication may be reproduced to support SQA qualifications only on a non-commercial basis. If it is to be used for any other purposes written permission must be obtained from SQA's NQ Delivery: Exam Operations team.

Where the publication includes materials from sources other than SQA (secondary copyright), this material should only be reproduced for the purposes of examination or assessment. If it needs to be reproduced for any other purpose it is the centre's responsibility to obtain the necessary copyright clearance. SQA's NQ Delivery: Exam Operations team may be able to direct you to the secondary sources.

These Marking Instructions have been prepared by Examination Teams for use by SQA Appointed Markers when marking External Course Assessments. This publication must not be reproduced for commercial or trade purposes.

Part One: General Marking Principles for Mathematics Intermediate 1 Units 1, 2 & 3 Paper 2

This information is provided to help you understand the general principles you must apply when marking candidate responses to questions in this Paper. These principles must be read in conjunction with the specific Marking Instructions for each question.

- 1. Marks for each candidate response must <u>always</u> be assigned in line with these general marking principles and the specific Marking Instructions for the relevant question. If a specific candidate response does not seem to be covered by either the principles or detailed Marking Instructions, and you are uncertain how to assess it, you must seek guidance from the Principal Assessor. You can do this by posting a question on the Marking Team forum. Alternatively, you can refer the issue directly to the Principal Assessor by completing a Principal Assessor Referral form and returning it with the script in the normal way.
- 2. Marking should always be positive ie, marks should be awarded for what is correct and not deducted for errors or omissions.
- **3.** Award one mark for each 'bullet' point shown in the Marking Instructions.
- 4. Working subsequent to an error must be followed through with the possibility of awarding all remaining marks for the subsequent working, provided the question has not been not simplified as a result of the error. In particular, the answer to one part of a question, even if incorrect, must be accepted as a basis for subsequent dependent parts of the question. Full marks in the dependent part(s) may be awarded provided the question has not been not simplified.
- 5. Solutions which seem unlikely to include anything of relevance must nevertheless be followed through. Candidates still have the opportunity of gaining one mark or more provided the solution satisfies the criteria for the marks.
- **6.** The following should not be penalised:
 - working subsequent to a correct answer (unless it provides firm evidence that the requirements of the question have not been met)
 - omission or misuse of units (unless marks have been specifically allocated for the purpose in the Marking Instructions)
 - bad form, eg sin $x^{\circ} = 0.5 = 30^{\circ}$
 - legitimate variation in numerical values/algebraic expressions
- 7. Full credit should only be given where the solution contains appropriate working. Where the correct answer may be obtained by inspection or mentally, credit may be given, but reference to this will be made in the Marking Instructions.
- 8. In general only give credit for answers if working is shown. A wrong answer without working receives no credit unless specifically mentioned in the Marking Instructions. The rubric on page one of the question paper states that 'full credit will be given only where the solution contains appropriate working'.
- 9. Sometimes the method to be used in a particular question is explicitly stated; no credit should be given where a candidate obtains the correct answer by an alternative method.
- **10.** Where the method to be used in a particular question is not explicitly stated, full credit must be given for alternative methods which produce the correct answer.

- 11. Do not penalise the same error twice in the same question.
- 12. Do not penalise a transcription error unless the question has been simplified as a result.
- Where a solution has been scored out and not replaced then provided the solution is legible marks should be awarded in line with the Marking Instructions for that question.
- 14. Where more than one solution is given, mark them all and award the least mark.
- 15. The symbols \checkmark and \times are used in the Marking Instructions to give guidance regarding the awarding of marks for specific candidate responses to some questions, eg 'award $2/4 \checkmark \times \times \checkmark$ ' indicates that the 1st & 4th marks should be awarded but the 2nd & 3rd marks should not.

Part Two: Mathematics Intermediate 1: Paper 2, Units 1, 2 and Applications

Question	Expected Answer/s	Max Mark	Additional Guidance
1	 Ans: 50 minutes o¹ find number of calories per minute: 160 ÷ 20 = 8 o² find time: 400 ÷ 8 = 50 	2	1. Correct answer without working award 2/2 2. Alternative strategies (a) •¹ 20 ÷ 160 = 0·125 •² 0·125 × 400 = 50 (b) •¹ 400 ÷ 160 = 2·5 •² 2·5 × 20 = 50 (c) •¹•² eg 160 20 160 20 80 10 400 50 [In this case award 1/2 for correct strategy with one error.]
2	Ans: £1129·92 • 1 find monthly payment: 47.08 • 2 find total payment: $47.08 \times 24 = 1129.92$	2	1. Correct answer without working award 2/2 2. Some common answers (no working necessary) (a) 2129.92 [1129.92 + 1000] award 1/2 (b) 129.92 [1129.92 - 1000] award 1/2 (c) 94.16 [47.08 × 2] award 1/2 (d) 1047.08 [47.08 + 1000] award 1/2 (e) 952.92 [1000 - 47.08] award 1/2

Questio	on Expected Answer/s	Max Mark	Additional Guidance	
Question 3	Ans: 150 cm ² • 1 know how to find total area of rectangular faces: 5 × 7 + 8 × 7 · 5 × 7 or equivalent • 2 know how to find area of a triangular face: ½ × 8 × 3 • 3 calculate total surface area: 150	Mark 3	 Correct answer without working award 3/3 The final mark can only be awarded for the addition of 5 calculations, except in notes 3 and 4 below. Where both triangles are calculated correctly as 1 rectangle, calculation leading to 150 award 3/3 Where both triangles are calculated as 1 rectangle calculation using incorrect sides then working can be followed through to award the final mark only in the following cases. 	
			(a) 147 [3 × 7 + 126] award 2/3 (b) 141 [3 × 5 + 126] award 2/3 (c) 135 [3 × 3 + 126] award 2/3	

Qu	estio	Expected Answer/s	Max Mark	Additional Guidance
4	a b	Ans: 1 hour 15 minutes •¹ interpret graph: 1 hour 15 minutes (or equivalent) Ans: 80 mph	3	
		• know how to find speed: $S = {}^{D}/{}_{T}$ • interpret graph: $D = 300$, $T = 3h45m$ • calculate speed: $300 \div 3.75 = 80$		 Correct answer without working award 3/3 Some common answers (no working necessary, rounding or truncation is acceptable) (a) 300 ÷ 3·45 = 87, 86(·9)

Question	Expected Answer/s	Max Mark	Additional Guidance
5	Ans: £210 • 1 find cost of letters (per shirt) $4 \times 0.15 = 60$ (p) • 2 find cost of 25 shirts $25 \times (9 + 0.60) = 240$ • 3 find discounted cost $0.125 \times 240 = 210$	3	1. Correct answer without working award 3/3 2. Common answers, working must be shown (a) 8.40 [87.5% of 9.60] award 2/3 (b) 236.25 [12 letters × 15p] award 2/3 (c) 196.87 (.88) [87.5% of 225] award 2/3 (d) 225.60 [225 + 60p] award 1/3 (e) 197.40 [87.5% of 225.60] award 2/3 3. For award of the final mark answers must be rounded or truncated to the nearest penny.
6	Ans: 18 minutes • 1 know how to find volume of tank: $90 \times 60 \times 50$ • 2 know how to find volume in litres: $(90 \times 60 \times 50) \div 1000$ • 3 know how to find time: $[(90 \times 60 \times 50) \div 1000] \div 15$ • 4 calculate $[(\text{volume}) \div 1000] \div 15 = 18$	4	 Correct answer with no working award 4/4 Some common answers (working must be shown) (a) 270000 ÷ 15 ÷ 60 = 300 ✓×✓× award 2/4 (b) 270000 ÷ 1000 ÷ 60 = 4.5 ✓✓×× award 2/4 (c) [(90 + 60 + 50) ÷ 1000] ÷ 15 = 0.013 ×✓✓✓ award 3/4

Question	Expected Answer/s	Max Mark	Additional Guidance
7 a	Ans: 3698 •¹ find 'Liberal' angle: 43 •² know how to find number of Liberal votes: •³/₃₀₀ × 30960 or •³ 30960/₃₀₀ × 43 or 43 ÷ (360 ÷ 30960) •³ find number of Liberal votes: 3698	3	 Correct answer without working award 3/3 27262 [317/360 × 30960] award 2/3 × ✓ ✓ (no working necessary) A common answer (working must be shown) 43% of 30960 = 13312(·8), 13313 award 1/3 ✓ × × Do not award third mark where premature rounding results in wrong answer eg 43/360 × 30960 = 0·12 × 30960 = 3715(·2) award 2/3 ✓ ✓ ×
7 b	Ans: In the by-election more voted SNP fewer voted Labour more voted Liberal •¹ state any one of the above differences •² state another one of the above differences	2	 Disregard invalid statements. eg SNP increased ✓ Labour decreased ✓ Liberal decreased × award 2/2 Disregard incorrect numerical references. eg SNP gained 70° Labour lost 90° award 2/2 Some common answers (a) Labour lost votes to SNP award 2/2 (b) In 2005 Labour had much more than SNP, but in 2008 they were close to each other.

Question	Expected Answer/s	Max Mark	Additional Guidance
8	Ans: £994·39 or £994·40 •¹ calculate 800 × 1·33 correctly: 1064 •² know to calculate 1064 ÷ 1·07: •³ divide correctly and round to nearest (appropriate) penny: 994·39 or 994·40	3	 Correct answer without working award 3/3 The third mark is only available where the answer to the division has to be rounded or truncated to the nearest penny For £994.4
9	 Ans: 7.5 m 1 correct form of Pythagoras Theorem: 4.5² + 2.4² 2 calculate sum (or difference) of squares: 26.01 3 calculate the square root of a calculated value: 5.1 4 calculate height: 5.1 + 2.4 = 7.5 	4	 Correct answer without working award 4/4 Some common answers (working must be shown) (a) 6·2() [√(4·5² - 2·4²) + 2·4)] x√√√ award 3/4 (b) 3·8() [√(4·5² - 2·4²)] x√√x award 2/4 Example of alternative strategy involving trigonometry a° = tan⁻¹(²·4/4·5) = 28.07° cos28·07° = 5·1 height = 5·1 + 2·4 = 7·5 Do not penalise inadvertent use of radians or grads if trigonometry is used Mark 4 can be awarded for adding 2.4 on to a previously calculated value

Que	stion	Exp	pected Answer/s	Max Mark	Additional Guidance
10		Ans	s: £35	3	
		•1•2	know how to calculate interest: $^{7.5}/_{100} \times 1400 \times ^4/_{12}$ (award 1 for $^{7.5}/_{100} \times 1400$ or $^4/_{12} \times ^{7.5}/_{100}$ or $^4/_{12} \times 1400$) carry out percentage and fraction calculations correctly: 35		 Correct answer without working award 3/3 If answer is 1435 [1400 + 35] (no working necessary) (a) award 3/3 if candidate states that interest is 35 (b) award 2/3 if candidate does not state that interest is 35 Acceptable answers for partial credit (no working necessary) (a) 105 [7·5% of 1400] award 1/3 (b) 2·5 [⁴/₁₂ × 7·5] award 1/3 (c) 466·67 or 466·66 [⁴/₁₂ × 1400] award 1/3 (d) 420 [105 × 4] award 1/3 The following common wrong answers illustrate where the 3rd mark is available to candidates, working must be shown. (a) 1400 × ¹¹⁰⁰/7·5 × ⁴/1² = 6222.22 × √ (note: answer must be rounded or truncated to nearest penny) (b) 1400 ÷ 7.5 × ⁴/1² = 62.22 × √x (c) 1400 × ^{7.5}/₁₀₀ × ¹²/₄ = 315

Question Exp	oected Answer/s	Max Mark	Additional Guidance
•1	find current Saturday pay: $7 \times 1.5 \times 8 = 84$ find current pay: $4 \times 7 \times 8 + \text{Saturday pay} = 308$ find new pay: $5 \times 7 \times 8.75 = 306.25$ state conclusion: £1.75 worse off	4	 Correct answer without working award 4/4 Evidence for the award of second mark Accept 224 + 28 (7 × 0.5 × 8) = 252 Do not accept (a) 24 + 12 (1.5 × 8) = 236 (b) 224 + 10.5(1.5 × 7) = 245.5(0) (c) (224 × 1.5) = 336 Where the wrong number of days has been used (a) Where only 1 day has been used, follow through working with the possibility of awarding 2/4. eg Current = 7 × 1.5 × 8 = 84

Que	estion	Expected Answer/s	Max Mark	Additional Guidance	
12	a	Ans: 7 •¹ identify Q ₁ and Q ₃ : 15 and 22 •² calculate interquartile range: 7	2	 Correct answer without working award 2/2 The second mark is available for correctly subtracting any pair of numbers from the Craigtown boxplot. eg 26 – 12 = 14 (range) award 1/2 Some common answers (working must be shown) (a) ½ (22 – 15) = 3.5 (SIQR) award 1/2 (b) 23 – 18 = 5 (Scottsburgh IQR) award 1/2 	
	b	Ans: Scottsburgh has a higher median and a smaller interquartile range •¹ interpret boxplot: Scottsburgh has a higher median •² interpret boxplot: Scottsburgh has a smaller interquartile range	2	 Award of 1st mark (a) accept eg (i) Scottsburgh is 21 and Craigtown is 18 (ii) Scottsburgh's box is higher (b) do not accept eg Scottburgh's boxplot is higher Award of 2nd mark (a) accept eg Scottsburgh's box is smaller (b) do not accept eg Scottsburgh's boxplot is smaller 	

Question	Expected Answer/s	Max Mark	Additional Guidance
13	Ans: 36% (See Note 1) •¹ find loss: 45 •² know to express loss as a fraction of 125: ⁴⁵ / ₁₂₅ •³ know to multiply fraction by 100: ⁴⁵ / ₁₂₅ × 100 •⁴ carry out all calculations correctly: 36	4	1. Correct answer without working award 2/4 Be aware 45/ ₁₀₀ × 80 = 36 award 2/4 √××√ When the only working is 45 and 36 award 2/4 √××√ 2. 4th mark is only available for calculations of the form 4/5 × c where a,b,c = calculated loss or 125 or 80 or 100. 3. Some common answers (working must be shown) (a) (i) 56(·25) [45/ ₈₀ × 100] award 3/4 √×√√ (ii) 56(·25) [45/ ₁₀₀ × 125] award 2/4 √××√ When the only working is 45 and 56(·25) award 2/4 √×√√ (b) 64 [80/ ₁₂₅ × 100] award 3/4 ×√√√ (c) 178, 177(·7) [80/ ₄₅ × 100] award 3/4 ×√√√ (d) 156(·25) [125/ ₈₀ × 100] award 2/4 ××√√ (e) 100 [80/ ₁₀₀ × 125 or 125/ ₁₀₀ × 80] award 1/4 ×××√

Question	Expected Answer/s	Max Mark	Additional Guidance
14	 Ans: 5·2 cm² Iknow to calculate area of semicircle: ½ πr² substitute correct radius into formula: ½ × π × 1·4² know to add area of triangle to area of semi-circle: ½ × π × 1·4² + ½ × 2·8 × 1·5 carry out all calculations correctly: 3·07 + 2·1 = 5·17 (must include a circle calculation followed by an addition) round to one decimal place: 5·2 	5	 Correct answer without working award 0/5 Some common answers (working must be shown) (a) 8·3 [π × 1·4² + ½ × 2·8 × 1·5] award 4/5 × √ √ (b) 7·3 [½ × π × 1·4² + 2·8 × 1·5] award 4/5 √ √ √ (c) 14·4 [½ × π × 2·8² + ½ × 2·8 × 1·5] award 4/5 √ √ √ (d) 6·5 [½ × π × 2·8 + ½ × 2·8 × 1·5] award 4/5 × √ √ √ (e) 4·3 [½ × π × 1·4 + ½ × 2·8 × 1·5] award 3/5 × √ × √ (f) 3·1 [½ × π × 1·4²] award 3/5 √ √ × × √ (g) 6·2 [π × 1·4²] award 2/5 × √ × × √ (h) 4·4 [½ × π × 2·8] award 2/5 × √ × × √ (i) 8·8 [π × 2·8] award 2/5 × √ × × √ (j) 2·2 [½ × π × 1·4] award 1/5 × × × × √ 3. (a) 5th mark is only available where the final answer or answer to circle calculation requires rounding. (b) Where premature rounding leads to incorrect answer, a maximum of 4/5 is available eg triangle = (½ × 1·4 × 1·5) × 2 = 1·05 × 2 = 1·1 × 2 total area = 2·2 + 3·1 = 5·3

TOTAL MARKS FOR PAPER 2 50

> TOTAL MARKS FOR PAPER 1 & 2 80

[END OF MARKING INSTRUCTIONS]