

Mark Scheme (Results)

January 2008

GCE O Level

O Level Pure Mathematics (7362_01)

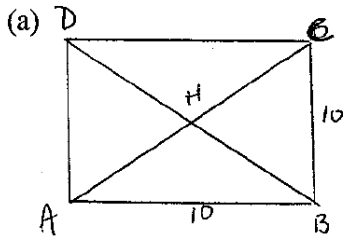
Pure Mathematics, 7362

Paper 1

Q.	Scheme	Marks
1	$\cos M = \frac{5^2 + 6.4^2 - 8.2^2}{2 \times 5 \times 6.4}, \quad M = 91.1^\circ$	M1A1,A1 (3)
2	$\sum_{r=7}^{50} (3r-5) = \frac{44}{2}(32+129) = 3542$	B1(44) M1A1 A1 (4)
3	(a) $\frac{dv}{dt} = -2 + 2t$, accel when $t=3$ is 4 m/s^2 (b) $\text{dist} = \int_0^4 (5-2t+t^2) dt = \left[5t - t^2 + \frac{1}{3}t^3\right]_0^4 = 20 - 16 + \frac{64}{3} = 25\frac{1}{3} \text{ m}$	M1A1,A1 M1A1,A1 (6)
4	(a) $\frac{dy}{dx} = 3e^{2x} + (3x-2) \times 2e^{2x}$ (b) $e^{2x} = \frac{y}{(3x-2)} \quad \frac{dy}{dx} = 3 \frac{y}{(3x-2)} + (3x-2) \times 2 \frac{y}{(3x-2)}$ $(3x-2) \frac{dy}{dx} = 3y + 6xy - 4y = (6x-1)y$	M1A1A1 M1A1 A1 (6)
5	(a) $V = \pi r^2 h = 50000\pi \quad r^2 h = 50000$ $A = 2\pi r h + \pi r^2 = 2\pi r \times \frac{50000}{r^2} + \pi r^2$ $= \left(\frac{100000}{r} + r^2\right) \pi$ (b) $\frac{dA}{dr} = (-100000r^{-2} + 2r) \pi$ $\frac{dA}{dr} = 0 \quad 2r = \frac{100000}{r^2}, \quad r^3 = 50000 \quad r = 36.84$ $\frac{d^2A}{dr^2} = (200000r^{-3} + 2) \pi > 0 \quad \therefore \text{minimum}$ $A_{\min} = 12791$	B1 M1,M1 A1 M1 M1,A1 M1A1, B1 (10)
6	(a) $\alpha + \beta = 2 \quad (\alpha + \beta) + \frac{1}{\alpha + \beta} = 2 + \frac{1}{2} = \frac{5}{2}$ $x^2 - \frac{5}{2}x + 1 = 0 \quad 2x^2 - 5x + 2 = 0$ (b) $\frac{\alpha + \beta}{\alpha} + \frac{\alpha + \beta}{\beta} = \frac{\alpha\beta + \beta^2 + \alpha^2 + \alpha\beta}{\alpha\beta} = \frac{(\alpha + \beta)^2}{\alpha\beta} = \frac{12}{p}$ Prod. $= \frac{(\alpha + \beta)^2}{\alpha\beta} = \frac{12}{p}$, Eqn. $x^2 - \frac{12}{p}x + \frac{12}{p} = 0$ (c) $x = 3: 9 - \frac{36}{p} + \frac{12}{p} = 0, \quad 9 = \frac{24}{p} \quad p = \frac{8}{3}$ (d) $\text{sum} = \frac{12}{p} = \frac{9}{2}$ other root $= \frac{9}{2} - 3 = \frac{3}{2}$	M1,A1 M1A1 M1A1 B1,B1 M1A1 M1A1 (12)

7	<p>(a) $(5x-9)(12x+4) = (7x-3)^2$ $60x^2 - 88x - 36 = 49x^2 - 42x + 9$ $11x^2 - 46x - 45 = 0$ $(11x+9)(x-5) = 0 \quad x = \frac{-9}{11} \quad x = 5$</p> <p>(b) $x = 5 \quad 16, 32, 64 \quad r = 2$</p> <p>(c) $a = \frac{16}{r^2} = 4$</p> <p>(d) $S_{12} = \frac{4(2^{12}-1)}{1} = 16380$</p>	<p>M1</p> <p>A1 M1A1A1</p> <p>M1A1 M1A1</p> <p>M1A1 (11)</p>
8	<p>(a) $f'(x) = 3x^2 - 4x - 4 \quad f(x) = x^3 - 2x^2 - 4x + c$ thro' (1, 0) $0 = 1 - 2 - 4 + c \quad c = 5$ $\therefore f(x) = x^3 - 2x^2 - 4x + 5$</p> <p>(b) $3x^2 - 4x - 4 = 0 \quad (3x+2)(x-2) = 0 \quad x = \frac{-2}{3} \quad x = 2$ P is $(\frac{-2}{3}, 6\frac{13}{27}) \quad Q$ is $(2, -3)$</p> <p>(c) (i) tang. at P: $y = 6\frac{13}{27}$ (ii) normal at Q: $x = 2$</p> <p>(d) $\int_{\frac{-2}{3}}^1 (x^3 - 2x^2 - 4x + 5) dx = \left[\frac{1}{4}x^4 - \frac{2}{3}x^3 - 2x^2 + 5x \right]_{\frac{-2}{3}}^1$ $= \left(\frac{1}{4} - \frac{2}{3} - 2 + 5 \right) - \left(\frac{1}{4} \times \frac{16}{81} + \frac{2}{3} \times \frac{8}{27} - 2 \times \frac{4}{9} - 5 \times \frac{2}{3} \right) = 6\frac{1813}{324}$ $\int_2^{\frac{-2}{3}} (x^3 - 2x^2 - 4x + 5) dx = 4 - \frac{16}{3} - 8 + 10 - \left(\frac{1}{4} - \frac{2}{3} - 2 + 5 \right) = -1\frac{11}{12}$ Reqd. area $= 6\frac{13}{27} \times 2\frac{2}{3} + 1\frac{11}{12} - 6\frac{1813}{324} = 12\frac{22}{81}$</p>	<p>M1A1 B1</p> <p>M1 A1A1 B1 ✓ B1 ✓</p> <p>M1A1 ✓</p> <p>M1</p> <p>M1 B1, M1A1</p> <p>(15)</p>
9	<p>(a) $\cos 2\theta = \cos^2 \theta - \sin^2 \theta = \cos^2 \theta - (1 - \cos^2 \theta) = 2\cos^2 \theta - 1$</p> <p>(b) $\sin 2\theta = \sin \theta \cos \theta + \sin \theta \cos \theta = 2\sin \theta \cos \theta$</p> <p>(c) $\cos 3\theta = \cos(2\theta + \theta) = \cos 2\theta \cos \theta - \sin 2\theta \sin \theta$ $= (2\cos^2 \theta - 1)\cos \theta - 2\sin^2 \theta \cos \theta$ $= 2\cos^3 \theta - \cos \theta - 2(1 - \cos^2 \theta)\cos \theta = 4\cos^3 \theta - 3\cos \theta$</p> <p>(d) $9\cos \theta - 12\cos^3 \theta = 2 \quad -3(4\cos^3 \theta - 3\cos \theta) = 2$ $-3\cos 3\theta = 2 \quad \cos 3\theta = -\frac{2}{3} \quad 3\theta = 2.3005, 3.9826, 8.$ $\theta = 0.767, 1.33, 2.86$</p> <p>(e) $\int_0^{\frac{\pi}{2}} (3\cos^3 \theta + 2\sin \theta) d\theta = \int_0^{\frac{\pi}{2}} \frac{3}{4}(\cos 3\theta + 3\cos \theta) + 2\sin \theta d\theta$ $= \left[\frac{3}{4} \left(\frac{1}{3} \sin 3\theta + 3\sin \theta \right) - 2\cos \theta \right]_0^{\frac{\pi}{2}}$ $= \frac{3}{4} \left(\frac{1}{3} \times (-1) + 3 - 0 \right) - 0 + 2 = 4$</p>	<p>M1A1</p> <p>B1 M1</p> <p>M1 M1A1</p> <p>M1</p> <p>M1 A2, 1, 0</p> <p>M1</p> <p>M1A1 M1A1 (16)</p>

10



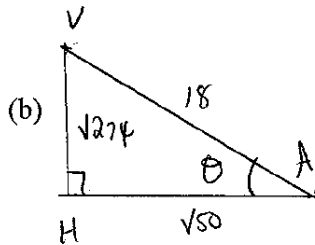
$$HB^2 = \frac{1}{4}(10^2 + 10^2) = \frac{200}{4} = 50$$

$$VH^2 = 18^2 - 50$$

$$VH = \sqrt{274} = 16.6 \text{ cm}$$

M1

M1A1

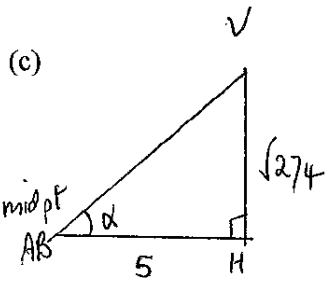


$$\cos \theta = \frac{\sqrt{50}}{18}$$

$$\theta = 66.86\dots = 66.9^\circ$$

M1A1

A1

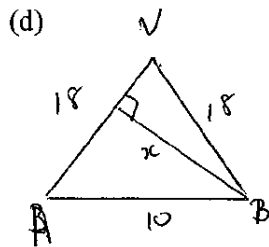


$$\tan \alpha = \frac{\sqrt{274}}{5}$$

$$\alpha = 73.19\dots = 73.2^\circ$$

M1A1

A1

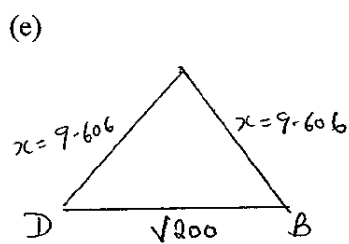


$$\sin\left(\frac{1}{2} \angle AVB\right) = \frac{x}{18} \quad \angle AVB = 32.255$$

$$\sin \angle AVB = \frac{x}{18} \quad x = 9.606\dots = 9.61 \text{ cm}$$

M1A1

M1A1



$$\sin \frac{1}{2} \phi = \frac{\frac{1}{2} \sqrt{200}}{9.606}$$

$$\frac{1}{2} \phi = 47.4^\circ$$

$$\phi = 94.8^\circ$$

M1A1

A1

A1 (17)