

# Mark Scheme (Results) January 2007

GCE

## O Level Pure Mathematics (7362\_02)

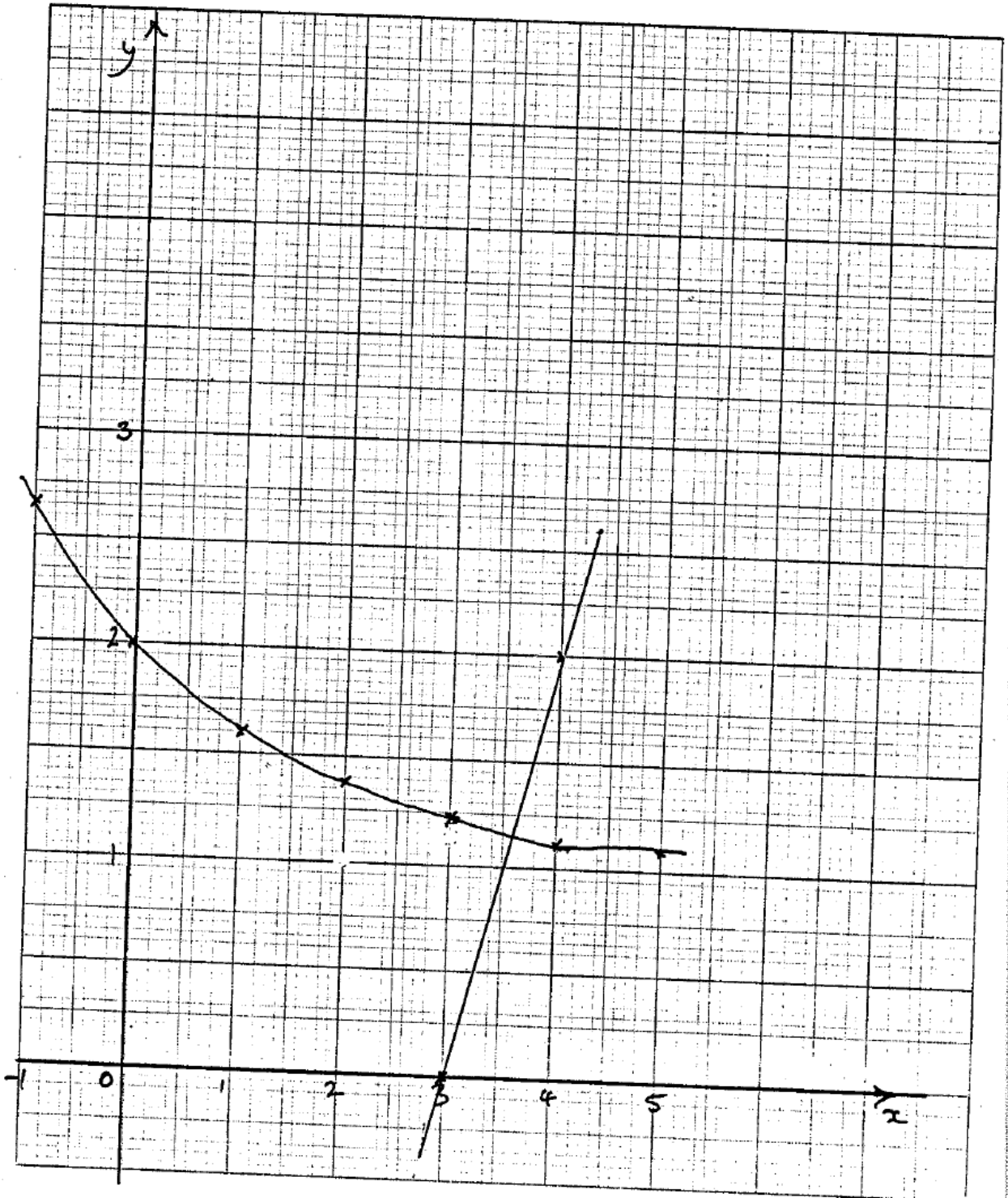
# Pure Mathematics 7362

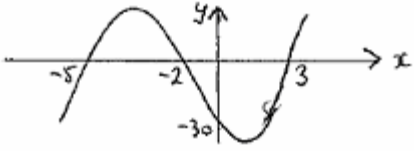
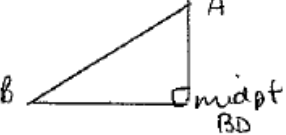
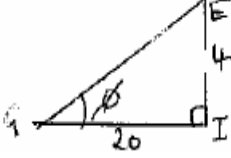
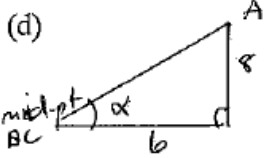
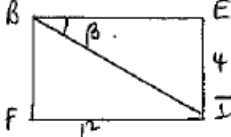
## Paper 2

1	$\cos \theta = \frac{4.6^2 + 5.3^2 - 6.5^2}{2 \times 4.6 \times 5.3}, \quad \theta = 81.7^\circ = 82^\circ$	M1A1,A1 (3)
2	$S_{10} = 5(2a + 9d) = 295, \quad S_8 = 4(2a + 7d) = 196$ $2a + 9d = 59$ $2a + 7d = 49$ $2d = 10 \quad d = 5$ $a = \frac{49 - 7 \times 5}{2} = 7$	M1,A1  M1A1 A1 (5)
3	$\log_3(5x + 12) + \log_3 x = 2 \quad \log_3[x(5x + 12)] = 2$ $5x^2 + 12x = 3^2, \quad 5x^2 + 12x - 9 = 0 \quad (5x - 3)(x + 3) = 0$ $x = \frac{3}{5} \quad (x = -3, \text{ not poss}).$	M1  M1,M1A1 A1 (5)
4	<p>(a) <math>\overrightarrow{OT} = (5\mathbf{i} + 12\mathbf{j})</math> (by ratio formula or vectors)</p> <p>(b) <math>\sqrt{5^2 + 12^2} = 13</math> unit vector <math>= \frac{1}{13}(5\mathbf{i} + 12\mathbf{j})</math></p>	M1A1A1  M1A1 (5)
5	<p>(a) <math>\cos 2\theta = \cos^2 \theta - \sin^2 \theta = \cos^2 \theta - (1 - \cos^2 \theta) = 2\cos^2 \theta - 1</math></p> <p>(b) <math>\text{Vol} = \int_0^{\frac{\pi}{8}} \pi \times 9 \cos^2 2x \, dx, = \frac{9}{2} \pi \int_0^{\frac{\pi}{8}} (\cos 4x + 1) \, dx</math>  <math>= \frac{9}{2} \pi \left[ \frac{1}{4} \sin 4x + x \right]_0^{\frac{\pi}{8}}, = \frac{9}{2} \pi \left[ \frac{1}{4} \sin \frac{\pi}{2} + \frac{\pi}{8} - 0 \right] = \frac{9}{16} \pi^2 + \frac{9}{8} \pi</math></p>	M1A1 M1,M1  M1A1, M1A1 (8)
6	<p>(a) <math>(x + 2)(7x - 4) = (3x)^2</math>  <math>7x^2 + 10x - 8 = 9x^2 \quad x^2 - 5x + 4 = 0, \quad (x - 1)(x - 4) = 0 \quad x = 4, \quad x = 1</math>  <math>x = 1</math> terms are 3,3,3 <math>\Rightarrow x = 4</math> and <math>a = 6</math></p> <p>(b) <math>r = \frac{12}{6} = 2</math></p> <p>(c) <math>S_{17} = \frac{6(2^{17} - 1)}{2 - 1} = 786426</math></p>	M1 A1,M1A1 A1  B1  M1A1  (8)

7	<p>(a) mid-point is <math>(1\frac{1}{2}, 4\frac{1}{2})</math>  <math>\text{grad } AB = \frac{5-4}{5+2} = \frac{1}{7}</math>, <math>\text{grad perp.} = -7</math>  <math>\text{eqn. perp bisector: } y - 4\frac{1}{2} = -7(x - 1\frac{1}{2}), \quad y + 7x = 15</math></p> <p>(b) perp bisector of <math>AC: x = 2</math></p> <p>(c) centre of circle where perp bisectors cross</p> <p>(i) centre is <math>(2, 1)</math></p> <p>(ii) radius <math>= \sqrt{(4^2 + 3^2)} = 5</math></p>	<p>B1 M1,A1</p> <p>M1,A1 B1</p> <p>M1 A1</p> <p>M1A1 (10)</p>																
8	<p>(a)</p> <table border="1" data-bbox="316 683 1059 763"> <tbody> <tr> <td>x</td> <td>-1</td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> </tr> <tr> <td>y</td> <td><b>2.65</b></td> <td>2</td> <td>1.61</td> <td><b>1.37</b></td> <td>1.22</td> <td>1.14</td> <td><b>1.08</b></td> </tr> </tbody> </table> <p>(b) Graph</p> <p>(c) <math>e^{-\frac{1}{2}x} + 1 = 1.8, \quad x = 0.45</math></p> <p>(d) <math>x = -2 \ln(2x - 7) \quad -\frac{1}{2}x = \ln(2x - 7) \quad e^{-\frac{1}{2}x} + 1 = 2x - 7 + 1</math>  <math>\text{Draw } y = 2x - 6. \quad x = 3.6</math></p>	x	-1	0	1	2	3	4	5	y	<b>2.65</b>	2	1.61	<b>1.37</b>	1.22	1.14	<b>1.08</b>	<p>B2,1,0</p> <p>G2 M1A1</p> <p>M1A1 M1A1 (10)</p>
x	-1	0	1	2	3	4	5											
y	<b>2.65</b>	2	1.61	<b>1.37</b>	1.22	1.14	<b>1.08</b>											
9	<p>(a) <math>\alpha\beta = \frac{3}{2}, \quad x^2 - (\frac{9}{4} + \frac{4}{9})x + 1 = 0</math>  <math>36x^2 - 97x + 36 = 0</math></p> <p>(b) <math>\alpha^2 + \beta^2 = (\alpha + \beta)^2 - 2\alpha\beta = (-\frac{p}{2})^2 - 2 \times \frac{3}{2} = \frac{p^2}{4} - 3</math>  <math>x^2 - (\frac{p^2}{4} - 3)x + \frac{9}{4} = 0</math></p> <p>(c) <math>\alpha^2 = 3 \quad \alpha^2\beta^2 = \frac{9}{4} \quad \beta^2 = \frac{3}{4}</math></p> <p>(d) <math>\frac{p^2}{4} - 3 = 3 + \frac{3}{4} \quad \frac{p^2}{4} = \frac{27}{4} \quad p^2 = 27 \quad p = \pm\sqrt{27} \quad (\pm 5.2)</math></p>	<p>M1M1 A1</p> <p>M1A1 B1(<u>AB</u>)<sup>2</sup> M1A1</p> <p>M1A1</p> <p>M1M1A1 (13)</p>																

Examining body	Jan 2007 Paper 2	Centre number			
Candidate name	No 8	Candidate number			
Paper reference		Question number		Sheet number	



10	<p>(a) <math>-125 + 25p + 55 + q = 0</math>  <math>25p + q = 70</math>  <math>27 + 9p - 33 = 0</math>  <math>9p + q = 6</math></p> <p>(b) <math>16p = 64</math> <math>p = 4</math> <math>q = -30</math></p> <p>(c) <math>x^3 + 4x^2 - 11x - 30 = (x+5)(x-3)(x+2)</math></p> <p>(d)</p>  <p>(e) <math>y = x^3 + 4x^2 - 11x - 30</math> <math>\frac{dy}{dx} = 3x^2 + 8x - 11</math>  At min. <math>(3x+11)(x-1) = 0</math> min. at <math>(1, -36)</math>  Tgt: <math>y = -36</math> meets curve where <math>x^3 + 4x^2 - 11x - 30 = -36</math>  <math>x^3 + 4x^2 - 11x + 6 = 0</math> <math>(x-1)(x-1)(x+6) = 0</math> <math>x = -6</math> ie at</p>	<p>M1A1</p> <p>A1</p> <p>M1A1A1</p> <p>B1 G1 G1 G1</p> <p>M1 M1A1 M1</p> <p>M1A1 (16)</p>
11	<p>(a) (i) <math>GE^2 = 12^2 + 16^2 + 4^2 = 416</math> <math>GE = 20.4</math></p> <p>(ii)</p>  <p><math>BD = 20</math>  <math>AB^2 = 64 + 100</math> <math>AB = 12.8</math></p> <p>(b)</p>  <p><math>\tan \phi = \frac{4}{20}</math> <math>\phi = 11.3^\circ</math></p> <p>(c) <math>\tan \theta = \frac{8}{20} \times 2 = \frac{4}{5}</math> <math>\theta = 38.7^\circ</math></p> <p>(d)</p>  <p><math>\tan \alpha = \frac{8}{6}</math> (<math>\alpha = 53.13^\circ</math>)  <math>\tan \beta = \frac{4}{12}</math> (<math>\beta = 18.43^\circ</math>)  reqd. angle <math>= 71.56^\circ = 71.6^\circ</math></p> 	<p>M1A1A1</p> <p>B1 M1A1</p> <p>M1A1 Ö A1</p> <p>M1A1 Ö A1</p> <p>M1A1 M1A1</p> <p>A1 (17)</p>