CAMBRIDGE INTERNATIONAL EXAMINATIONS GCE Ordinary Level

MARK SCHEME for the October/November 2013 series

4037 ADDITIONAL MATHEMATICS

www.tiremepapers.com

4037/22

Paper 2, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the October/November 2013 series for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level components and some Ordinary Level components.



Page 2	Mark Scheme	Syllabus	Paper
	GCE O LEVEL – October/November 2013	4037	22

Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Accuracy mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol √^{*} implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.
 B2, 1, 0 means that the candidate can earn anything from 0 to 2.

	Page 3	Mark Scheme	Syllabus Paper			
		GCE O LEVEL – October/Novem	4037 22			
1	× ×	(x-1) + 6(x-1)	M1	Attempt to solve a three term quadratic		
	Cr	itical values –6 and 1	A1			
	-0	6 < <i>x</i> < 1	A1 [3]	Allow $x > -6$ AND $x < 1$ but not OR or a comma. Mark final answer.		
2	(4-	$\sqrt{5} - 2\Big)^2 = 80 - 16\sqrt{5} + 4$	M1	Attempt to expand, allow one error, must be in the form $a + b\sqrt{5}$.		
	M	ultiply top and bottom by $\sqrt{5} + 1$	M1	Must be attempt to expand top and bottom.		
	17	$\sqrt{5} + 1$	A1 A1 [4]	Allow A1 for $\frac{68\sqrt{5}+4}{c}$		
	Le	R $\sqrt{5}-2^2 = 80-16\sqrt{5}+4$ $\sqrt{5}-1(p\sqrt{5}+q) = 5p-q+\sqrt{5}(q-p)$ rading to $5p-q = 84, q-p = -16$ = 17 q = 1	M1 M1 A1 A1	Must get to a pair of simultaneous equations for this mark		
3	(i) $\frac{dy}{dk}$	$\frac{y}{k} = k \left(\frac{1}{4}x - 5\right)^7$ $= 2$	M1 A1 [2]			
	(ii) Us	dy dy dy with $y = 12$ and dy	M1	\checkmark on <i>k</i> needs both M marks		
	(II) US	we $\partial y = \frac{dy}{dx} \times \partial x$ with $x = 12$ and $\partial x = p$				
	-2	56 <i>p</i>	A1√ [^] [2]	\checkmark only for $-128kp$ and must be evaluated		
4	(i) 10		B1 [1]			
	(ii) –5		B 1	Not $\log_p 1-5$		
	(iii) log	$g_p XY = \log_p X + \log_p Y = 7$	[1] B1	Or $\log_{XY} p = \frac{1}{\log_p XY}$		
	$\frac{1}{7}$		B1√ [^] [2]	Do not allow just $\log_p X + \log_p Y = 7$ \checkmark^{h} on $\frac{1}{\log_p XY}$		

	Page 4		Mark Scheme		Syllabus	Paper
			GCE O LEVEL – October/Nove	4037	22	
5			y = 5 oe	B1		
			2y = 5 oe	B 1		
		Solve	their linear simultaneous equations	M1	Each in two variable quadratic as far as <i>x</i>	
		<i>x</i> = 3	or $y = -0.5$	A1,A1√ [≜] [5]		or <i>y</i>
		OR f	rom log	B1		
		0.602	2x - 2.408y = 3.01	B 1		
			4x + 0.954y = 2.386			
			rom ln	B 1		
			5x - 5.545y = 6.931 7x + 2.197y = 5.493	B 1		
			$M1A1A1\sqrt[4]{}$ follows as before			
6	(a) (i)	-8 or	20	B 1	± 40 implies $\pm 2 \times 2$	0 or +160
		160	(x^3) isw	B1	hence B1	ion
		-100	(x) ISW	[2]	OK if seen in expans	31011
	(ii)	$60(x^2)$,	B1	Can be implied	
		(i) +-	$\frac{1}{2}$ (their 60)	M1		
		-130		A1 [3]		
	(b)	$16x^2$	$+32x+24+\frac{8}{x}+\frac{1}{x^2}$ oe	B3,2,1,0	Terms must be evalu B2 for 4 terms correct	ct.
				[3]	B1 for 2 or 3 terms c ISW once expansion	
7	(i)	$l = \frac{32}{2}$	$\frac{500}{r^2}$	B1	allow $lx^2 = 3500$	
		•	$\times 4x + 2x + 2l$	B1	RHS 3 terms e.g. 12	$x + 2x + 2\left(\frac{3500}{x^2}\right)$
					or better	```
			itute for <i>l</i> and correctly reach			
		L = 1	$4x + \frac{7000}{x^2}$	DB1ag [3]	Dependent on both p	previous B marks
	(ii)		$14 - \frac{14000}{x^3}$	M1A1	M1 either power red A1 both terms correc	
		Equa	te $\frac{dL}{dr}$ to 0 and solve	DM1	Must get $x^n =$	
		x = 10 $L = 2$	0	A1	Both values	
			$=\frac{42000}{x^4}$ and minimum stated	B1 [5]	Or use of gradient ei turning point.	ther side of

Page 5		Mark Scheme					Syllabus	Paper		
			GCE O LEVEL – October/November 2013					4037	22	
8	(i)	x^2					B1 [1]	Implied by axes or v May be seen in (ii)	alues in a table.	
	(ii)	Plot -	$\frac{y}{x}$ agair	st x^2 w	vith linea	r scales		Must be linear scale	s	
		x^2	4	16	36	64	B1	At least 3 correct points	ints plotted and	
		$\frac{y}{x}$	4.8	9.6	17.5	29	B1 [2]	Line must be ruled a least 2 correct points		
	(iii)		gradies 4 ± 0.02				M1	Condone use of corr table/graph to find g		
			$.2 \pm 0.4$	<u>~</u>			A1 B1 [3]	equation. Values rea must be correct.		
	(iv)	Read	$\frac{y}{x} = 12$.5			M1	Obtaining $(x^2) = 22$	to 24 from graph	
		or sul	substitute in formula					As far as $x^2 = +ve c$	constant	
		4.8					A1 [2]	4.7 to 4.9 ignore -4.8 or 0		
9		12vsi 12(vc 12vc	s composin $\alpha = 4$ cos $\alpha + 1$ cos $\alpha = 4$ e for v o 39.6	$\begin{pmatrix} 0 \\ .8 \end{pmatrix} = 70 \\ 8.4$			M1 A1 A1 M1A1 DM1 A1 A1 [8]	Allow 0.691 radians		
		$y = 7$ $D^{2} = 0$ $D = 0$ $V = -1$	$x = \frac{x}{10 - 21.6}$ $x = \frac{40^2 + 4}{52.8}$ $\frac{D}{12}$ 5.23 $x = \frac{40}{48.4}$	5 = 48.4	D y 942.56)	→ ↓ ↓ ↓ ↓	B1 B1 M1 A1 DM1 A1 M1 A1	5.23 or better Allow 0.691 radians	3	
							[8]		,	

Page 6	Mark Scheme		Syllabus	Paper
	GCE O LEVEL – October/November 2013			22
$v = \frac{1}{2}$ $\tan \delta$ $V^{2} = \frac{1}{2}$ $V = \frac{1}{2}$ $\frac{\sin \beta}{1}$	$\frac{v}{V}$ $\frac{k}{V}$ $\frac{1.8}{70}$ $\sqrt{40^2 + 70^2} (= 80.6)$ $\sqrt{40^2 + 70^2} (= 6.72)$ $\frac{12}{12} (= 6.72)$ $r = \frac{4}{7} \rightarrow (\delta = 29.74) \text{ oe}$ $1.8^2 + 6.72^2 - 2 \times 1.8 \times 6.72 \cos 29.74$	B1 B1 B1 M1 A1 M1 A1	Or $\tan(90 - \delta) = \frac{7}{4}$ Allow 0.172 radians	
$\alpha = 2$	$29.74 + \beta = 39.6$	A1	Allow 0.691 radians	
		[8]		
x = 1 $\tan \delta$ $D^{2} =$ V = ($z = \frac{B}{D}$ $\frac{\delta}{21.6}$ $\sqrt{40^2 + 70^2} (= 80.6)$ $.8 \times 12 = 21.6$ $\frac{4}{7} \rightarrow (\delta = 29.74) \text{ oe}$ $21.6^2 + 80.6^2 - 2.21.6.80.6 \cos 29.74$ $62.8/12) = 5.23$	B1 B1 M1 A1	This method has extra this point the M mark equation in D but the A value of V .	is for an
21	$\frac{3}{6}.6 = \frac{\sin 29.74}{62}.8$			
$\beta = 2$	9.8(3) or 9.8(2)	A1	Allow 0.172 radians	
	$29.74 + \beta = 39.6$	A1 [8]	Allow 0.691 radians	

	Page 7	Mark Scheme	Syllabus Paper	
		GCE O LEVEL – October/Novem	4037 22	
			T	I.
10	()	$AB^{2} = 12^{2} + 12^{2} - 2 \times 12 \times 12 \times \cos 1.4$ 15.4 to 15.5 $\theta = 2\pi - 1.4 (= 4.88)$	M1 A1 B1	$AB = 2 \times 12 \sin 0.7$ May be implied May be implied
		Use $s = r\theta (= 58.6)$ 74.1	M1 A1 [5]	12×4.9 or better oe
		(Sector) $\frac{1}{2} \times 12^2 \times (2\pi - 1.4) (= 352)$ or $\pi \times 12^2 - \frac{1}{2} \times 12^2 \times 1.4$	M1	May be implied .
		(Triangle) = $\frac{1}{2} \times 12 \times 12 \times \sin 1.4 (= 70.9 \text{ or } 71)$	M1	
		Area of major sector + Area of triangle 422 or 423	M1 A1 [4]	May be implied
11		$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{1}{3}\mathrm{e}^{\frac{1}{3}x}$	B1	
		$m = \frac{1}{3}e^3$	M1	For insertion of $x = 9$ into their $\frac{dy}{dx}$. 6.7 or better if correct.
		$y - e^3 = \frac{1}{3}e^3(x - 9)$	DM1	Using their evaluated <i>m</i> to find eqn y = 6.7x - 40.2 or better if correct.
		$\operatorname{At} Q y = 0, x = 6$	A1 [4]	Accept value that rounds to 6.0 to 2sf
	(ii)	Area triangle $1.5e^3$ or 30.1	B1	
		$\int e^{\frac{1}{3}x} dx = 3e^{\frac{1}{3}x} \text{ oe}$	B1	
		Uses limits of 0 and 9 in integrated function.	M1	\pm must see both values inserted if incorrect answer
		$3e^3 - 3$ or 57.3 Area under curve subtract area of triangle $1.5e^3 - 3$ or 27.1	A1 M1 A1	Condone 27.2 if obtained from
			[6]	57.3 – 30.1.

	Page 8	8	Mark Scheme		Syllabus	Paper
			GCE O LEVEL – October/Nov	ember 2013	4037	22
12	(a)	cosec	$x = \frac{1}{\sin x}$ inserted into equation	B1		
		tan x	$=-\frac{2}{7}$	DB1		
		164.1 344.1	,	B1 B1√ [≜] [4]	One correct value. \checkmark on $180 + (164.1)$ M tanx = Condone164 and 344 Deduct 1 mark for ex	4
	(b)	Find y 0.898	1) = 0.79or 2.34 y using radians (or 0.9 or 0.90) 4.04 and 4.81(45)	B1 M1 A1 A1 A1 [5]	Allow 0.8, 2.3 or 45 Add 1 then divide by angle One correct value Another correct valu Final two values Deduct 1 mark for ex	2 on a correct