

QUESTION 1			
1.1	1.1.1	$3(2x^2 - 5) = x$ $6x^2 - x - 15 = 0$ $(2x + 3)(3x - 5) = 0$ $x = -1\frac{1}{2} \text{ or } x = 1\frac{2}{3}$	<p>✓ standard form ✓ factorising</p> <p>✓✓ answer</p> <p>[4]</p>
	1.1.2	$3x^2 + x - 5 = 0$ $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $x = \frac{-1 \pm \sqrt{1 - 4(3)(-5)}}{2(3)}$ $= \frac{-1 \pm \sqrt{61}}{6}$ $x = \frac{-1 + 7,81}{6} \text{ or } x = \frac{-1 - 7,81}{6}$ $x = \frac{6,81}{6} \text{ or } x = \frac{-8,81}{6}$ $x = 1,14 \text{ or } x = -1,47$	<p>✓ formula ✓ substitution</p> <p>✓ simplification $\sqrt{61} = 7,810$</p> <p>✓✓ x- values</p> <p>[5]</p>
	1.1.3	$\sqrt{x} - 1 = 5$ $\sqrt{x} = 6$ $x = 36$	<p>✓ transposing -1 ✓ answer</p> <p>[2]</p>

1.2		$x^2 - 2xy + y^2 - 9 = 0 \dots (1)$ $x - 2y = 1$ $x = 1 + 2y \dots (2)$ <p><i>sub (2) in (1)</i></p> $(1 + 2y)^2 - 2y(1 + 2y) + y^2 - 9 = 0$ $1 + 4y + 4y^2 - 2y - 4y^2 + y^2 - 9 = 0$ $y^2 + 2y - 8 = 0$ $(y + 4)(y - 2) = 0$ $y = -4 \text{ or } y = 2$ $x = 1 + 2(-4); x = 1 + 2(2)$ $x = -7; x = 5$ <p><i>ALTERNATIVE SOLUTION:</i></p> $x = 2y + 1 \dots (1)$ $(x - y)^2 = 9 \dots (2)$ $x - y = 3 \text{ or } -3$ $(2y + 1) - y = 3 \text{ or } (2y + 1) - y = -3$ $2y + 1 - y = 3 \text{ or } 2y + 1 - y = -3$ $y = 2 \text{ or } y = -4$ $x = 3 + 2 \text{ or } x = -3 - 4$ $x = 5 \text{ or } x = -7$	<p>[8]</p> <p>[8]</p> <p>[19]</p>	<p>✓ making x the subject of the formula in linear equation</p> <p>✓ correct substitution</p> <p>✓ simplification</p> <p>✓ standard form</p> <p>✓ factorisation</p> <p>✓ y-values</p> <p>✓ ✓ x-values</p> <p>✓ factorising quadratic equation</p> <p>✓ ✓ simplifying quadratic equation</p> <p>✓ correct substitution</p> <p>✓ y- values</p> <p>✓ substitution</p> <p>✓ ✓ x- values</p>
QUESTION 2				
2.1	2.1.1	<p><i>For real roots</i></p> $2p - 1 \geq 0$ $2p \geq 1$ $p \geq \frac{1}{2}$	[2]	<p>✓ statement</p> <p>✓ answer</p>
	2.1.2	<p>p can be anyone of $\frac{1}{2}; 1, \frac{5}{2}, 5, \frac{17}{2}, 13, \dots$</p>	[2]	<p>✓ ✓ answer</p>

2.2	$x^2 + x + 1 = 0$ $\Delta = b^2 - 4ac$ $= (1)^2 - 4(1)(1)$ $= -3$ $\Delta < 0$ Since $\Delta < 0$, roots are not real	[5] [9]	✓ standard form ✓ formula (Δ) ✓ correct substitution ✓ simplification ✓ $\Delta < 0$ (conclusion)
QUESTION 3			
3.1	$f(x) = 2x^2 - mx - 4x + 10$ $f(3) = 2(3)^2 - m(3) - 4(3) + 10 = -2$ $\therefore 18 - 3m - 12 + 10 = -2$ $18 - 3m = 0$ $m = 6$	[4]	✓ $f(3)$ ✓ $= -2$ ✓ simplification ✓ answer
3.2	$f(x) = 2x^3 - ax + b$ $f(2) = 2(2)^3 - a(2) + b = 0$ $16 - 2a + b = 0 \dots\dots\dots(1)$ $g(x) = x^3 - ax^2 - bx - 8$ $g(2) = (2)^3 - a(2)^2 - b(2) - 8 = 0$ $8 - 4a - 2b - 8 = 0$ $2a + b = 0$ $b = -2a \dots\dots\dots(2)$ sub.(2) in (1) $16 - 2a + (-2a) = 0$ $4a = 16$ $a = 4$ $\therefore b = -2(4) = -8$	[6] [10]	✓ $f(2)$ ✓ $= 0$ ✓ equation (1) ✓ equation (2) ✓ value of a ✓ value of b

QUESTION 4			
4.1	4.1.1	$y = +\sqrt{9 - x^2}$ or $h(x) = \sqrt{9 - x^2}$	[2] ✓ $y = \sqrt{r^2 - x^2}$ ✓ $y = \sqrt{9 - x^2}$
	4.1.2	$p = 1$ $q = -4$	[2] ✓ p - value ✓ q - value
	4.1.3	$y = a(x - 1)^2 - 4$ $0 = a(3 - 1)^2 - 4$ $0 = 4a - 4$ $a = 1$	[4] ✓ substitute (1; -4) ✓ substitute (3; 0) ✓ simplification ✓ answer
	4.1.4	$y \geq -4$	[2] ✓✓ answer
4.2	4.2.1	$xy = k$ sub.(-1;3) : $k = (-1)(3) = -3$ $\therefore f(x) = -\frac{3}{x}$	[3] ✓ equation ✓ substitution ✓ answer Answer only: full marks
	4.2.2	$y = mx + c$ $(-1; 3): 3 = -m + c \dots\dots\dots(1)$ $(2; 0) : 0 = 2m + c \dots\dots\dots(2)$ $(1) - (2): 3 = -3m$ $\therefore m = -1$ in (1): $3 = -(-1) + c$ $c = 2$ equation of $g: y = -x + 2$ OR $m_g = \frac{y_2 - y_1}{x_2 - x_1}$ $= \frac{3 - 0}{-1 - 2}$ $= -1$ $y = -x + c \dots\dots\dots(1)$ sub: (2;0) in (1) $0 = -(2) + c$ $2 = c$ $\therefore y = -x + 2$	[5] ✓ substitution (-1; 3) ✓ substitution (2; 0) ✓ $m = -1$ ✓ $c = 2$ ✓ equation of g ✓ formula for m ✓ substitution ✓ $m = -1$ ✓ $c = 2$ ✓ equation of g
	4.2.3	$-1 < x < 0$	[2] ✓✓ answer
			[20]

QUESTION 5				
5.1	5.1.1	$\frac{3^{2-x} - 4 \cdot 3^{-x}}{3^{-x+2}}$ $= \frac{3^2 \cdot 3^{-x} - 4 \cdot 3^{-x}}{3^{-x} \cdot 3^2}$ $= \frac{3^{-x}(3^2 - 4)}{3^{-x}(3^2)}$ $= \frac{(3^2 - 4)}{(3^2)}$ $= \frac{5}{9}$	[4]	✓ splitting factors ✓ factors in brackets ✓ simplification ✓ answer
	5.1.2	$\frac{\log 9}{\log\left(\frac{1}{3}\right)}$ $= \frac{\log 3^2}{\log 3^{-1}}$ $= \frac{2 \log 3}{-1 \log 3}$ $= -2$	[4]	✓ exp law: $\log 9 = \log 3^2$ ✓ exp law: $\log\left(\frac{1}{3}\right) = \log 3^{-1}$ ✓ log law: $\log a^b = b \log a$ ✓ answer
	5.2.1	$\left(\frac{1}{2}\right)^{x-9} = 4^{x+3}$ $(2^{-1})^{x-9} = (2^2)^{x+3}$ $2^{-x+9} = 2^{2x+6}$ $\therefore -x+9 = 2x+6$ $-3x = -3$ $x = 1$	[5]	✓✓ writing as base 2 ✓ exponential law ✓ simplification ✓ answer

	5.2.2	$\log_4(x-1) + \log_4(x+2) = 1$ $\log_4(x-1)(x+2) = 1$ $\therefore (x-1)(x+2) = 4$ $x^2 + x - 2 = 4$ $x^2 + x - 6 = 0$ $(x+3)(x-2) = 0$ $\therefore x \neq -3$ $\therefore x = 2$	[6]	✓ log law (single log) ✓ log law (removing log) ✓ removing brackets ✓ factorisation ✓ $x \neq -3$ ✓ $x = 2$
5.3	5.3.1	$12^{x+1} = 36(6^x)$ $12^x \cdot 12 = 36 \cdot 6^x$ $\frac{12^x}{6^x} = \frac{36}{12}$ $\left(\frac{12}{6}\right)^x = 3$ $2^x = 3$	[3]	✓ splitting factors ✓ simplification (dividing by 6^x and 12) ✓ exponential law
	5.3.2	$2^x = 3$ $\log 2^x = \log 3$ $x \log 2 = \log 3$ $x = \frac{\log 3}{\log 2}$ $x = 1,54$	$or \quad x = \log_2 3$ $= \frac{\log 3}{\log 2}$ $= 1,54$	✓ log law ✓ x-subject ✓ answer
			[3]	
			[25]	

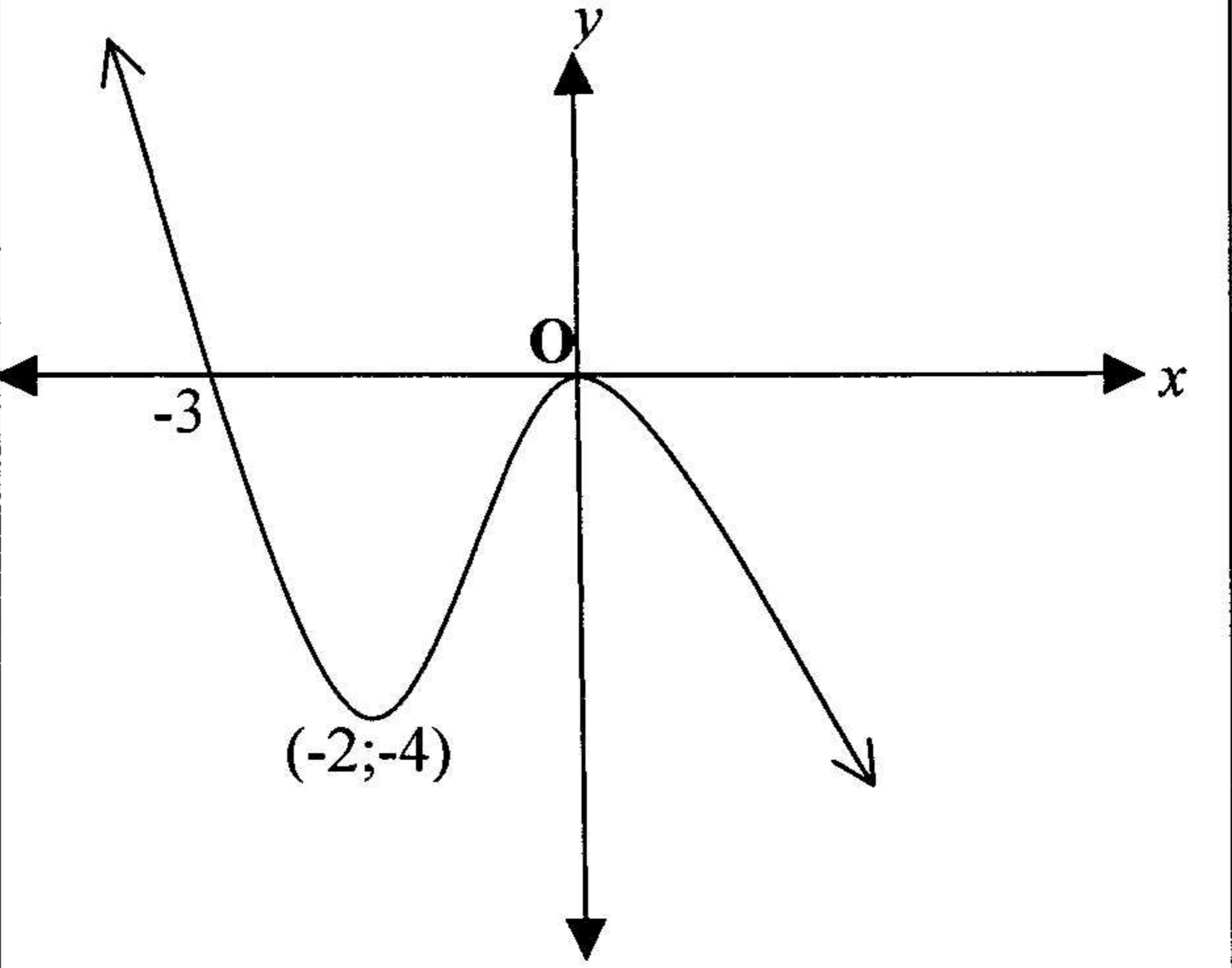
QUESTION 6

6.1	6.1.1	$T_n = a + (n-1)d$ $T_n = 401$ $\therefore a + (n-1)d = 401$ $5 + (n-1)4 = 401$ $5 + 4n - 4 = 401$ $4n = 400$ $\therefore n = 100$ there are 100 terms	[4]	✓ formula ✓ equation ✓ substitution ✓ answer
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	6.1.2	$S_n = \frac{n}{2}(a + T_n)$ $S_{100} = \frac{100}{2}(5 + 401)$ $= 50(406)$ $= 20300$	[3]	✓ formula ✓ substitution ✓ answer
6.2	6.2.1	$18 - x = x - 2$ $2x = 20$ $x = 10$	[3]	✓ $T_2 - T_1 = T_3 - T_2$ (M) ✓ simplification ✓ answer
	6.2.2	$\frac{x}{2} = \frac{18}{x}$ $x^2 = 36$ $x = \pm 6$	[4]	✓ $\frac{T_2}{T_1} = \frac{T_3}{T_2}$ (M) ✓ simplification ✓ $\pm \sqrt{6}$
6.3	6.3.1	$T_1 = 3(2)^{1+1} = 3 \cdot 2^2 = 12$ $T_2 = 3(2)^{1+2} = 3 \cdot 2^3 = 24$ $T_3 = 3(2)^{1+3} = 3 \cdot 2^4 = 48$	[3]	✓ value for T_1 ✓ value for T_2 ✓ value for T_3
	6.3.2	$12 + 24 + \dots + 3 \cdot 2^{11}$ $a = 12$ $r = 2$ $n = 10$ $S_{10} = \frac{a(1 - r^n)}{1 - r}$ $= \frac{12(1 - 2^{10})}{1 - 2}$ $= 12276$	[5]	✓✓✓ value for a, r, n ✓ formula ✓ answer
6.4		$A = P \left(1 + \frac{r}{100} \right)^n$ $= 6530 \left(1 + 1,25 \cdot \frac{1}{100} \right)^{18}$ $= 6530(1,0125)^{18}$ $= 8166,27$ <p>∴ Cost is R8166.27</p>	[6]	✓ formula ✓ P ✓ $n=18$ ✓ $r=1,25$ ✓✓ answer
			[28]	

QUESTION 7				
7.1		$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ $= \lim_{h \rightarrow 0} \frac{4(x^2 + 2xh + h^2) - 4x^2}{h}$ $= \lim_{h \rightarrow 0} \frac{4x^2 + 8xh + 4h^2 - 4x^2}{h}$ $= \lim_{h \rightarrow 0} \frac{8xh + 4h^2}{h}$ $= \lim_{h \rightarrow 0} (8x + 4h)$ $= 8x$	[6]	✓ formula ✓ substitution ✓ remove () ✓ simplification ✓ dividing by h ✓ answer
7.2	7.2.1	$y = x^3 - 3x^{-1}$ $\frac{dy}{dx} = 3x^2 + 3x^{-2}$	[3]	✓ exponential form ✓✓ each derivative
	7.2.2	$y = x^2 - 2x - 3$ $\frac{dy}{dx} = 2x - 2$	[3]	✓ remove brackets ✓✓ each derivative
7.3	7.3.1	$y = 2^2 - 1$ $= 3$	[1]	✓ answer
	7.3.2	$f'(x) = 2x$ $f'(2) = 4$ slope = 4	[3] [16]	✓ derivative ✓ substitution ✓ answer

QUESTION 8				
8.1	8.1.1	$f(x) = -x^3 - 3x^2$ $-x^2(x+3) = 0$ $x = 0 \text{ or } x = -3$	[3]	✓ factors ✓ = 0 ✓ x-intercept
		y- intercept = 0		y- intercept
	8.1.2	$f'(x) = 0$ $-3x^2 - 6x = 0$ $-3x(x+2) = 0$ $x = 0 \text{ or } x = -2$ $y = 0 \text{ or } y = -4$	[6]	✓ $f'(x) = 0$ ✓ derivative ✓ factors ✓ x-values ✓✓ y-values

	8.1.3		[4]	✓ x-intercepts ✓✓ TP's ✓ shape
	8.1.4	$-2 < x < 0$ or $-2 \leq x \leq 0$	[2]	✓✓ answer
8.2	8.2.1	$l = (x - 2) \text{ cm}$ $b = 52 - x - 2 = (50 - x) \text{ cm}$	[2]	✓ l ✓ b
	8.2.2	$A = l \times b$ $A = (x - 2)(50 - x)$ $= 50x - x^2 - 100 + 2x$ $A = -x^2 + 52x - 100$	[2]	✓ formula ✓ multiplication
	8.2.3	$A'(x) = -2x + 52 = 0$ $-2x = -52$ $x = 26$ $A = -x^2 + 52x - 100$ $A = (26)^2 + 52(26) - 100$ $A = 1928 \text{ cm}^2$	[4]	✓ derivative ✓ =0 ✓ substitution ✓ answer
			[23]	