


<p>1.1</p>	<p>1.1.1 <math>5x(x - 2) = 2</math>  <math>5x^2 - 10x - 2 = 0</math>  <math>\Delta = 10^2 - 4(5)(-2)</math>  <math>= 140</math>                      which is not a perfect square  <math>\therefore</math> roots not rational.</p> <p><b>OR</b></p> <p><math>5x(x - 2) = 2</math>  <math>5x^2 - 10x - 2 = 0</math>  <math>x = \frac{-(-10) \pm \sqrt{140}}{10}</math>                      but 140 is not a perfect square / <math>\sqrt{140}</math> is irrational  <math>\therefore</math> roots not rational</p>	<p>(4)</p>	<p>✓ Standard form [must have an equation, else penalty of 1 mark – <b>only in this question</b>]                      ✓ Use of <math>\Delta</math>                      ✓ Value of <math>\Delta</math>                      ✓ "not a perfect square"</p> <p>✓ Standard form</p> <p>✓ <math>x</math> in surd form</p> <p>✓ ✓ "but 140 is not a perfect square / <math>\sqrt{140}</math> is irrational" [CA if wrong <math>\Delta</math>]</p> <p><b>Note:</b> If candidate calculates <math>x</math> as 2,18 or -0,18 and then concludes roots not rational, then award only 2 out of 4 marks [the first 2 marks].</p>
	<p>1.1.2 <math>x = \frac{-(-10) \pm \sqrt{140}}{10}</math>  <math>x = 2,18</math> or <math>-0,18</math></p> <p><b>OR</b>                      Answers only</p> <p><b>OR</b></p> <p><math>5x(x - 2) = 2</math>  <math>5x^2 - 10x - 2 = 0</math>  <math>\therefore x^2 - 2x + 1 = \frac{2}{5} + 1</math>  <math>\therefore (x - 1)^2 = 1,4</math>  <math>\therefore x = 1 + \sqrt{1,4}</math> , <math>x = 1 - \sqrt{1,4}</math>  <math>x = 2,18</math> or <math>x = -0,18</math></p>	<p>(4)</p>	<p>✓ Choice of formula                      ✓ Substitution in formula                      ✓ ✓ Each value of <math>x</math></p> <p>2 marks per solution</p> <p>✓ Standard form</p> <p>✓ Completing the square</p> <p>✓ ✓ Each value of <math>x</math></p> <p><b>Note:</b> penalise max of 1 mark for incorrect rounding off <b>in this question only.</b></p>

<p>1.2</p>	<p>1.2.1</p> $(2x - 5)^2 - 49x^2 = 0$ $(2x - 5)^2 = 49x^2$ $2x - 5 = 7x \quad \text{or} \quad 2x - 5 = -7x$ $-5x = 5 \quad \text{or} \quad 9x = 5$ $x = -1 \quad \text{or} \quad x = \frac{5}{9}$ <p><b>OR</b></p> $(2x - 5)^2 - 49x^2 = 0$ $(2x - 5 + 7x)(2x - 5 - 7x) = 0$ $-5x = 5 \quad \text{or} \quad 9x = 5$ $x = -1 \quad \text{or} \quad x = \frac{5}{9}$ <p><b>OR</b></p> $(2x - 5)^2 - 49x^2 = 0$ $4x^2 - 20x + 25 - 49x^2 = 0$ $45x^2 + 20x - 25 = 0$ $9x^2 + 4x - 5 = 0$ $(x + 1)(9x - 5) = 0$ $x = -1 \quad \text{or} \quad x = \frac{5}{9}$	<p>(4)</p>	<p>✓✓ Each equation after taking square roots on each side                  ✓✓ Each solution</p> <p>✓ Factorizing                  ✓ Breaking into 2 equations                  ✓✓ Each solution</p> <p>✓ Squaring                  ✓ Standard form</p> <p>✓ Factorizing                  ✓ Both solutions</p>
<p>1.2.2</p>	$ x - 5  >  4 - 8 $ $ x - 5  > 4$ $x - 5 < -4 \quad \text{or} \quad x - 5 > 4$ $x < 1 \quad \text{or} \quad x > 9$ <p><b>OR</b></p> $ x - 5  > 4 \Rightarrow \text{distance from } x \text{ to } 5 \text{ is at least } 4$  $\therefore x < 1 \quad \text{or} \quad x > 9$ <p><b>OR</b></p> $x^2 - 10x + 25 > 16$ $x^2 - 10x + 9 > 0$ $(x - 9)(x - 1) > 0$ $x < 1 \quad \text{or} \quad x > 9$	<p>(5)</p>	<p>✓ value as 4                  ✓ alternatives                  ✓ <math>x &lt; 1</math> ✓ or ✓ <math>x &gt; 9</math></p> <p>✓ value as 4                  ✓ interpretation                  ✓ <math>x &lt; 1</math> ✓ or ✓ <math>x &gt; 9</math></p> <p>ANSWER ONLY : FULL MARKS</p> <p>✓ Squaring</p> <p>✓ Factorising                  ✓ <math>x &lt; 1</math> ✓ or ✓ <math>x &gt; 9</math></p> <p><b>Note:</b> If get <math> x - 5  &gt; -4</math>                  Max of 2 / 5 for what follows: <math>x \in R</math> or squaring etc.</p>

	<p>1.2.3 <math>\frac{3x}{x-3} \geq 4</math>  <math>\frac{3x}{x-3} - 4 \geq 0</math>  <math>\frac{3x - 4x + 12}{x-3} \geq 0</math>  <math>\frac{-x + 12}{x-3} \geq 0</math>  <math>\frac{x-12}{x-3} \leq 0</math>  <math>x &gt; 3</math> and <math>x \leq 12</math> OR <math>3 &lt; x \leq 12</math></p> <p><b>OR</b>  <math>\frac{3(x-3)+9}{x-3} \geq 4</math>  <math>3 + \frac{9}{x-3} \geq 4</math>  <math>\frac{9}{x-3} \geq 1</math>  <math>\therefore x-3 &gt; 0</math> and <math>\frac{x-3}{9} \leq 1</math>  <math>\therefore x &gt; 3</math> and <math>x \leq 12</math>  OR <math>3 &lt; x \leq 12</math></p> <p><b>OR if error:</b>  <math>3x \geq 4x - 12</math>  <math>x \leq 12</math></p>	<p><math>\checkmark</math> 4 to LHS  <math>\checkmark</math> common denominator  <math>\checkmark</math> simplifying</p> <p>[a variety of methods can be used as steps to the solution]</p> <p><math>\checkmark x &gt; 3</math> <math>\checkmark</math> and <math>\checkmark x \leq 12</math>  OR <math>\checkmark \checkmark \checkmark 3 &lt; x \leq 12</math></p> <p>(6)</p> <p><math>\checkmark</math> simplify LHS to  <math>3 + \frac{9}{x-3} \geq 4</math>  <math>\checkmark</math> simplify inequality to  <math>\frac{9}{x-3} \geq 1</math>  <math>\checkmark</math> deduce <math>\frac{x-3}{9} \leq 1</math> or  <math>9 \geq x-3</math>  <math>\checkmark x &gt; 3</math> <math>\checkmark</math> and <math>\checkmark x \leq 12</math>  OR <math>\checkmark \checkmark \checkmark 3 &lt; x \leq 12</math></p> <p>Max. 2 / 6 for last line</p>
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1.3	<p>1.3.1 <math>(x + 4)(y + 4) - xy = 208</math></p> <p><math>xy + 4x + 4y + 16 - xy = 208</math></p> <p><math>4x + 4y = 192</math></p> <p><math>x + y = 48</math></p> <p><b>OR</b></p> <p><math>(x + 4)(y + 4) = 748</math></p> <p><math>xy + 4x + 4y + 16 = 748</math></p> <p><math>540 + 4x + 4y + 16 = 748</math></p> <p><math>4x + 4y = 192</math></p> <p><math>x + y = 48</math></p> <p><b>OR</b></p> <p><math>2(x + 4) + 2(x + 4) + 2 \cdot 2y = 208</math></p> <p><b>OR</b> <math>2(y + 4) + 2(y + 4) + 2 \cdot 2x = 208</math></p> <p><math>4x + 4y = 192</math></p> <p><math>x + y = 48</math></p>	(3)	<p>✓ <math>(x + 4)(y + 4)</math></p> <p>✓ correctly completing equation</p> <p>✓ multiplying</p> <p>✓ <math>(x + 4)(y + 4)</math></p> <p>✓ correctly completing equation</p> <p>✓ multiplying and substituting for <math>xy</math></p> <p>✓✓ setting up equation</p> <p>✓ multiplying</p>
	<p>1.3.2 <math>xy = 540</math></p> <p><math>x(48 - x) = 540</math></p> <p><math>x^2 - 48x + 540 = 0</math></p> <p><math>(x - 30)(x - 18) = 0</math> or <math>x = \frac{48 \pm \sqrt{48^2 - 4 \cdot 540}}{2}</math></p> <p><math>x = 30</math> or <math>18</math></p> <p><math>x = 18</math> (<math>x &lt; y</math>)</p> <p><math>y = 48 - 18 = 30</math></p> <p><b>OR</b></p> <p><math>xy = 540</math></p> <p><math>x(48 - x) = 540</math></p> <p style="padding-left: 40px;"><math>= (18)(30)</math></p> <p><math>\therefore x = 18</math> and <math>y = 30</math></p>	(6)	<p>✓ formulating equation</p> <p>✓ substitution</p> <p>✓ standard form</p> <p>✓ factorising or subst in formula</p> <p>✓ value of <math>x</math> [<b>must make choice</b>]</p> <p>✓ value of <math>y</math></p> <p>✓ formulating equation</p> <p>✓ substitution</p> <p>✓ observation ✓ <math>540 = (18)(30)</math></p> <p>✓ value of <math>x</math></p> <p>✓ value of <math>y</math></p>

	<p><b>OR</b>  <math>xy = 540</math>  <math>(48 - y)y = 540</math>  <math>y^2 - 48y + 540 = 0</math>  <math>(y - 30)(y - 18) = 0</math> or <math>y = \frac{48 \pm \sqrt{48^2 - 4 \cdot 540}}{2}</math>  <math>y = 30</math> or <math>18</math>  <math>y = 30</math> (<math>x &lt; y</math>)  <math>x = 48 - 30 = 18</math></p>	<p>✓ formulating equation                  ✓ substitution                  ✓ standard form</p> <p>✓ factorising or subst in formula</p> <p>✓ value of <math>y</math> [<b>must make choice</b>]                  ✓ value of <math>x</math></p>
		[32]

2.1	2.1.1		<p>Graph of <math>f</math>                  ✓ shape                  ✓ vertex (2 ; 0)                  ✓ <math>y</math>-intercept</p> <p>graph of <math>g</math>                  ✓ straight line                  ✓ shape coinciding with <math>f</math> for <math>x \geq 2</math>                  ✓ <math>y</math>-intercept</p> <p><b>Note:</b>                  If graph of <math>f</math> has vertex at (-2 ; 0): award 2 / 3 for graph of <math>f</math> and 2 / 3 for graph of <math>g</math>.                  If graph of <math>f</math> has vertex at (0 ; -2): award 2 / 3 for graph of <math>f</math> and 3 / 3 for graph of <math>g</math>.</p>
	2.1.2	$x \geq 2$	<p>(2) ✓✓ answer  <b>Note:</b> CA applies.                  If graph of <math>f</math> has vertex at (-2 ; 0): ✓✓ no solutions.                  If graph of <math>f</math> has vertex at (0 ; -2): ✓✓ <math>x \geq 0</math>.</p>
	2.1.3	$y = - x - 2 $ OR $-y =  x - 2 $	<p>(2) ✓✓ answer</p>

2.2	2.2.1	$y = -x^2 - 6x - 4$ $-y = x^2 + 6x + 4$ $-y = x^2 + 6x + 3^2 - 9 + 4$ $-y = (x + 3)^2 - 5$ $y = -(x + 3)^2 + 5$ <p><b>OR</b></p> $y = -x^2 - 6x - 4$ $y = -[x^2 + 6x + 4]$ $y = -[x^2 + 6x + 3^2 - 9 + 4]$ $y = -[(x + 3)^2 - 5]$ $y = -(x + 3)^2 + 5$ <p><b>OR</b></p> $x = \frac{-b}{2a} = \frac{6}{-2} = -3$ <p>At turn pt. <math>y = 5</math></p> $y = -(x + 3)^2 + 5$ <p><b>OR</b></p> $\frac{dy}{dx} = -2x - 6 = 0$ $x = -3$ $y = 5$ $y = -(x + 3)^2 + 5$ <p><b>OR</b></p> $y = -(x - p)^2 + q$ $y = -x^2 + 2px - p^2 + q = -6x^2 - 6x - 4$ $\therefore 2p = -6$ $p = -3$ $-p^2 + q = -4$ $q = 5$ $\therefore y = -(x + 3)^2 + 5$	<p>(4)</p> <ul style="list-style-type: none"> <li>✓ making co-efficient of <math>x^2</math> positive</li> <li>✓ completing square</li> <li>✓ writing with perfect square</li> <li>✓ answer</li> <li>✓ making co-efficient of <math>x^2</math> positive</li> <li>✓ completing square</li> <li>✓ writing with perfect square</li> <li>✓ answer</li> <li>✓ substitution in formula</li> <li>✓ x-coordinate of turn.pt.</li> <li>✓ y-coordinate of turn.pt.</li> <li>✓ answer</li> <li>✓ derivative = 0</li> <li>✓ x-coordinate of turn.pt.</li> <li>✓ y-coordinate of turn.pt.</li> <li>✓ answer</li> <li>✓ multiplying</li> <li>✓ value of <math>p</math></li> <li>✓ value of <math>q</math></li> <li>✓ answer</li> </ul> <p><b>Note:</b> CA applies</p>
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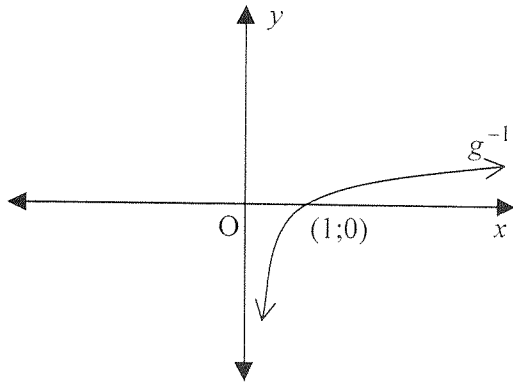
	<p>2.2.2 <math>(x+3)^2 \geq 0</math>  <math>\therefore -(x+3)^2 \leq 0</math>  <math>\therefore -(x+3)^2 + 5 \leq 5</math>  <math>\therefore f(x) \leq 5</math></p> <p><b>OR</b>  Turning point is <math>(-3;5)</math>  From graph: <math>f(x)</math> has maximum value of 5  OR range of <math>f</math> is <math>y \leq 5</math>  <math>\therefore f(x) \leq 5</math></p>	(2)	<p>✓ perfect square <math>\geq 0</math></p> <p>✓ award for second or third line</p> <p>✓ identifying turn pt.  ✓ deduction from graph</p>
	<p>2.2.3 <math>y</math>-intercept is <math>(0 ; -4)</math>  <math>-9 &lt; -4 - k &lt; 0</math>  <math>-4 &lt; k &lt; 5</math></p>	(5)	<p>✓ <math>y</math>-intercept  ✓✓ each endpoint [ "&lt;" must be correct each time]  ✓✓ resultant answer</p> <p><b>Answer only: full marks.</b></p> <p><b>Note:</b> CA must apply</p>
	<p>2.2.4 <math>-x^2 - 6x - 4 - t = 0</math>  <math>\Delta = 36 - 4(-1)(-4 - t)</math>  <math>= 20 - 4t</math>  which is a perfect square for  <math>t = 1; 4</math> or <math>5</math></p> <p><b>OR</b>  <math>t = -(x+3)^2 + 5</math>  <math>\therefore (x+3)^2 = 5 - t</math>  <i>and <math>5 - t</math> is a perf. square only for</i>  <math>t = 1; 4</math> or <math>5</math></p> <p><b>OR</b>  <math>t = -(x+3)^2 + 5</math>  <math>5 - 0^2 = 5 ; 5 - 1^2 = 4 ; 5 - 2^2 = 1</math>  <math>\therefore t = 1; 4</math> or <math>5</math></p> <p><b>OR</b>  Answer only</p>	(5)	<p>✓ substitution in <math>\Delta</math>  ✓ simplifying</p> <p>✓✓✓ each value of <math>t</math></p> <p>✓ use of this form</p> <p>✓ perfect square as subject</p> <p>✓✓✓ each value of <math>t</math></p> <p>✓ <math>f(x) = t</math></p> <p>✓✓✓✓ values of <math>t</math> : penalize 2 per error or omission.</p> <p>✓✓✓✓✓ full marks less 2 per error or omission</p>

2.3	$r = 3$ $\sqrt{2k} = 3$ $2k = 9$ $k = 4,5$ <p><b>OR</b></p> $y = x \text{ so}$ $x = \sqrt{9 - x^2} \text{ and } x^2 = k$ $x^2 = 9 - x^2$ $2x^2 = 9$ $x^2 = 4,5$ $\therefore k = 4,5$ <p><b>OR</b></p> $\frac{k}{x} = \sqrt{9 - x^2}$ $\frac{k^2}{x^2} = 9 - x^2$ $x^4 - 9x^2 + k^2 = 0$ $\Delta = 0$ $81 - 4k^2 = 0$ $k = 4,5$	(5)	<ul style="list-style-type: none"> <li>✓ value of <math>r</math></li> <li>✓ using <math>\sqrt{2k}</math> (distance formula)</li> <li>✓ <math>\sqrt{2k} = 3</math></li> <li>✓ squaring</li> <li>✓ answer</li>   <li>✓✓ substitution in each equation</li>   <li>✓ squaring</li> <li>✓ value of <math>x^2</math></li> <li>✓ value of <math>k</math></li>   <li>✓ substitution</li>   <li>✓ standard form</li>   <li>✓ <math>\Delta = 0</math></li> <li>✓ extracting <math>\Delta</math></li> <li>✓ answer</li> </ul>
<b>[31]</b>			



<p>3.1</p> $p(x) = 2x^3 + x^2 - 2m^2x - 3m$ $p(-3) = 0$ $\therefore 2(-3)^3 + (-3)^2 - 2m^2(-3) - 3m = 0$ $6m^2 - 3m - 45 = 0$ $2m^2 - m - 15 = 0$ $(2m + 5)(m - 3) = 0$ $m = -\frac{5}{2} \text{ or } m = 3$ $p(3) = 0$ $\therefore 2(3)^3 + (3)^2 - 2m^2(3) - 3m = 0$ $-6m^2 - 3m + 63 = 0$ $2m^2 + m - 21 = 0$ $(2m + 7)(m - 3) = 0$ $m = -\frac{7}{2} \text{ or } m = 3$ <p>Both are factors for <math>m = 3</math>.</p> <p><b>OR</b></p> $p(x) = 2x^3 + x^2 - 2m^2x - 3m$ $p(-3) = 0$ $\therefore 2(-3)^3 + (-3)^2 - 2m^2(-3) - 3m = 0$ $6m^2 - 3m - 45 = 0$ $2m^2 - m - 15 = 0 \dots\dots(1)$ $p(3) = 0$ $\therefore 2(3)^3 + (3)^2 - 2m^2(3) - 3m = 0$ $-6m^2 - 3m + 63 = 0$ $2m^2 + m - 21 = 0 \dots\dots(2)$ <p>(2)-(1): <math>2m - 6 = 0</math> <math>m = 3</math></p> <p>OR (1)+(2): <math>4m^2 - 36 = 0</math> <math>m = -3 \text{ or } 3</math></p> <p><b>OR</b></p> <p><math>(x + 3)</math> and <math>(x - 3)</math> are factors</p> <p><math>\therefore x^2 - 9</math> is a factor</p> $\therefore p(x) = (x^2 - 9)(2x + \frac{1}{3}m) = 2x^3 + \frac{1}{3}mx^2 - 18x - 3m$ $\therefore \frac{1}{3}m = 1 \quad \text{and} \quad -2m^2 = -18$ $\therefore m = 3 \quad \quad \quad m = 3 \text{ or } -3$ $\therefore m = 3$	<ul style="list-style-type: none"> <li>✓ use theorem correctly</li> <li>✓ substitution</li> <li>✓ standard form</li>   <li>✓ both values</li>   <li>✓ correct use of theorem</li> <li>✓ substitution</li>   <li>✓ standard form</li>   <li>✓ both values</li>   <li>(9) ✓ answer</li>   <li>✓ use theorem correctly</li> <li>✓ substitution</li> <li>✓ standard form</li>   <li>✓ use theorem correctly</li> <li>✓ substitution</li> <li>✓ standard form</li>   <li>✓✓ simultaneous solution</li> <li>✓ value of <math>m</math></li>   <li>✓✓ simultaneous solution</li> <li>need to also determine unique solution <math>m = 3</math> to get last mark</li>   <li>✓✓✓✓ for deduction of <math>x^2 - 9</math> as factor</li> <li>✓<math>2x</math> ✓<math>\frac{1}{3}m</math></li> <li>✓✓ for <math>\frac{1}{3}m = 1</math></li> <li>or for <math>-2m^2 = -18</math></li> <li>✓ final solution <math>m = 3</math></li> </ul>
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	<p><b>OR</b></p> $p(x) = (x^2 - 9)(2x + 1) + 18x - 2m^2x + 9 - 3m$ $= (x^2 - 9)(2x + 1) + [2(9 - m^2)x + 3(3 - m)] = 0$ <p>In the square bracket lives a linear function which is zero for TWO values of <math>x</math> (<math>x = 3</math> and <math>x = -3</math>) Therefore it must be identically zero. So <math>3 - m = 0</math> AND <math>9 - m^2 = 0</math>. This only happens for <math>m = 3</math></p> <p><b>OR</b></p> <p>In <math>p(x)</math> replace <math>x^2</math> by 9 and simplify  <math>18x + 9 - 2m^2x - 3m = 0</math>  <math>3(m - 3) + 2(m^2 - 9)x = 0</math>  <math>(m - 3)[2(m + 3)x + 3] = 0</math>  <math>2(m + 3)x + 3</math> is a linear function therefore only zero for <b>one</b> value of <math>x</math></p> <p><math>\therefore m - 3</math> must be <math>= 0</math>  <math>\therefore m = 3</math></p>	<p>✓✓ writing in this form</p> <p>✓✓ grouping inside [ ]</p> <p>✓✓ deduction          ✓✓ each equation          ✓ answer</p> <p>✓ method          ✓ substitution          ✓✓ grouping          ✓ factorising</p> <p>✓✓ deduction</p> <p>✓ conclusion          ✓ answer</p>
3.2	$p(x) = 2x^3 + x^2 - 18x - 9$ $= (x^2 - 9)(2x + 1) \text{ OR } (x + 3)(2x^2 - 5x - 3)$ $\text{OR } (x - 3)(2x^2 + 7x + 3)$ $= (x - 3)(x + 3)(2x + 1)$	<p>✓✓ two factors</p> <p>✓ third factor</p> <p>(3)</p>
	<b>[12]</b>	

4.1				
	4.1.1	P(0 ; 1)	(1)	✓ answer
	4.1.2	$1 < a < 5$	(3)	✓ $1 < a$ ✓ $a < 5$
	4.1.3		(3)	✓ shape ✓ indicates x- intercept ✓ y-axis as asymptote
	4.1.4	$0 < x < 1$	(2)	✓ $0 < x$ ✓ $x < 1$
4.2				
	4.2.1	$\frac{15 \cdot 5^{p-1} + 5^{p+1}}{2^{-p}}$ $= \frac{5^p(15 \cdot 5^{-1} + 5)}{2^{-p}}$ $= \frac{5^p(8)}{2^{-p}}$ $= 5^p \cdot 2^p \cdot 8$ $= 8 \cdot 10^p$ $= 8M$ <p><b>OR</b></p> $\frac{15 \cdot 5^{p-1} + 5^{p+1}}{2^{-p}}$ $= 2^p(15 \cdot 5^{-1} \cdot 5^p + 5 \cdot 5^p)$ $= 3 \times 10^p + 5 \times 10^p$ $= 8 \times 10^p$ $= 8M$	(5)	✓ taking out common factor ✓ simplifying bracket ✓ index law applied ✓ further index law applied ✓ <b>realizing that <math>10^p = M</math></b>  ✓ multiplying by $2^p$ ✓ index law $5^{p-1} = 5^p \cdot 5^{-1}$ ✓ $15 \times 5^{-1} = 3$ ✓ index law $2^p \times 5^p = 10^p$ ✓ <b>realizing that <math>10^p = M</math></b>

	<p>4.2.2 <math>\log 2 \cdot \log_2 5 \cdot \log_{25} M</math></p> $= \log 2 \cdot \frac{\log 5}{\log 2} \cdot \frac{\log M}{\log 25}$ $= \log 2 \cdot \frac{\log 5}{\log 2} \cdot \frac{\log M}{2 \log 5}$ $= \frac{1}{2} \log M$ $= \frac{1}{2} p$ <p>OR</p> $\log 2 \cdot \log_2 5 \cdot \log_{25} M$ $= \log 2 \cdot \log_2 5 \cdot \log_{25} 10^p$ $= \log 2 \cdot \log_2 5 \cdot p \log_{25} 10$ $= p \log 5 \cdot \log_{25} 10$ $= p \log_{25} 5$ $= \frac{1}{2} p$	(4)	<p>✓✓ each application of change of base law</p> <p>✓ application of further log law</p> <p>✓ simplification</p> <p>✓ <math>\log_{25} 10^p = p \log_{25} 10</math></p> <p>✓ <math>\log 2 \cdot \log_2 5 = \log 5</math></p> <p>✓ <math>\log 5 \cdot \log_{25} 10 = \log_{25} 5</math></p> <p>✓ <math>\log_{25} 5 = \frac{1}{2}</math></p>
4.3			
	<p>4.3.1 <math>\sqrt[3]{x^4} - \sqrt{24} = 0</math></p> $\sqrt[3]{x^4} = \sqrt{8}$ $x = (\sqrt{8})^{\frac{4}{3}}$ $x = (2^2)^{\frac{3}{3} \cdot \frac{4}{3}}$ $x = 2^2$ $x = 4$ <p>[may not use calculator for last 2 marks]</p>	(4)	<p>✓ <math>x^{\frac{3}{4}}</math> as subject</p> <p>✓ raising to power</p> <p>✓ <math>\sqrt{8}</math> as power of 2</p> <p>✓ answer [accept <math>2^2</math> or 4]</p>
	<p>4.3.2 <math>2^{2x+1} - 2^x = 3</math></p> $2 \cdot 2^{2x} - 2^x = 3$ $2 \cdot 2^{2x} - 2^x - 3 = 0$ $(2^x + 1)(2 \cdot 2^x - 3) = 0$ $2^x = -1 \text{ no solution}$ <p>or <math>2^x = 1,5</math></p> $x \log 2 = \log 1,5$ $x = \frac{\log 1,5}{\log 2} = 0,58$	(7)	<p>✓ standard form</p> <p>✓ factorising</p> <p>✓ no solution one alternative</p> <p>✓ other alternative</p> <p>✓ use of logs</p> <p>✓ <math>x</math> as subject</p> <p>✓ answer</p>
		[29]	

<p>5.1</p>	$S_n = a + [a + d] + [a + 2d] + \dots + [a + (n - 1)d]$ $S_n = [a + (n - 1)d] + [a + (n - 2)d] + \dots + a$ $2S_n = [2a + (n - 1)d] + [2a + (n - 1)d] + \dots \text{to } n \text{ terms}$ $2S_n = n[2a + (n - 1)d]$ $S_n = \frac{n}{2}[2a + (n - 1)d]$ <p><b>OR</b></p> $S_n = a + [a + d] + [a + 2d] + \dots + T_n$ $S_n = T_n + [T_n - d] + [T_n - 2d] + \dots + a$ $2S_n = [a + T_n] + [a + T_n] + \dots \text{to } n \text{ terms}$ $2S_n = n[a + T_n]$ $S_n = \frac{n}{2}[a + T_n]$ <p>but <math>T_n = a + (n - 1)d</math></p> $\therefore S_n = \frac{n}{2}[2a + (n - 1)d]$ <p><b>OR</b></p> $1 + 2 + 3 + \dots + (n - 1) = \frac{1}{2}(n - 1)n$ $S_n = na + d[1 + 2 + 3 + \dots + (n - 1)]$ $= na + \frac{1}{2}dn(n - 1)$ $= \frac{n}{2}[2a + (n - 1)d]$	<p>(4)</p> <p>✓ expansion ✓ reverse order</p> <p>✓ addition ✓ RHS as product</p> <p>✓ expansion ✓ reverse order</p> <p>✓ addition ✓ RHS as product</p> <p>✓ statement</p> <p>✓ substitution ✓ substitution</p> <p><b>max: 3 for this alternative.</b></p>
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<p>5.2</p>	<p>5+6+7+ ... is an arithmetic series with  <math>a = 5</math> and <math>d = 1</math>                  2200 m needs 110 shuttles  <math>S_n = \frac{n}{2}[2a + (n-1)d]</math>  <math>110 = \frac{n}{2}[2.5 + (n-1).1]</math></p> <p><math>n^2 + 9n - 220 = 0</math>  <math>(n+20)(n-11) = 0</math> or <math>n = \frac{-9 \pm \sqrt{9^2 - 4(-220)}}{2}</math>                  or <math>n(n+9) = 220 = 11 \times 20</math>  <math>n = 11</math> minutes</p> <p><b>OR</b></p> <p><math>100 + 120 + 140 + \dots = \frac{n}{2}[200 + (n-1)20] = 2200</math></p> <p><math>n^2 + 9n - 220 = 0</math>  <math>(n-11)(n+20) = 0</math> OR <math>n(n+9) = 220 = 11 \times 20</math>                  or <math>n = \frac{-9 \pm \sqrt{9^2 - 4(-220)}}{2}</math>  <math>n = 11</math> minutes</p>	<p>(6)</p> <ul style="list-style-type: none"> <li>✓ recognising Arithmetic sequence</li> <li>✓ number of shuttles needed</li> <li>✓ substitution in correct formula [first 3 marks for formulating equation]</li> <li>✓ standard form</li> <li>✓ factorising or subst in formula</li> <li>✓ answer</li> </ul> <ul style="list-style-type: none"> <li>✓ recognising Arithmetic sequence</li> <li>✓ <math>S_n = 2200</math></li> <li>✓ substitution in correct formula [first 3 marks for formulating equation]</li> <li>✓ standard form</li> <li>✓ factorising or subst in formula</li> <li>✓ answer</li> </ul> <p><b>Notes:</b>                  Answer only 3 / 6</p> <p>Answer with evidence of understanding 6 / 6</p> <p>Wrong formula: max. of 2 / 6</p>
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5.3			
	5.3.1	$\frac{m}{m+2} = \frac{2m-3}{m}$ $m^2 = 2m^2 + m - 6$ $m^2 + m - 6 = 0$ $(m+3)(m-2) = 0$ $m = -3 \text{ or } m = 2$	<p>(5)</p> <ul style="list-style-type: none"> <li>✓ setting up equation</li> <li>✓ simplification</li> <li>✓ standard form</li> <li>✓ factorising</li> <li>✓ values for <math>m</math></li> </ul>
	5.3.2	<p>if <math>m = 2</math> <math>r = \frac{2}{2+2} = \frac{1}{2}</math>  <math>\therefore</math> converges for <math>m = 2</math></p> <p><b>OR</b></p> <p>if <math>m = -3</math> <math>r = \frac{-3}{-3+2} = 3 \Rightarrow</math> series diverges  <math>\therefore</math> must converge for <math>m = 2</math></p>	<p>(3)</p> <ul style="list-style-type: none"> <li>✓✓ testing for <math>r</math> [1 of these marks is for knowing convergence needs <math>-1 &lt; r &lt; 1</math>]</li> <li>✓ answer</li> <li>✓✓ testing for <math>r</math> [1 of these marks is for knowing convergence needs <math>-1 &lt; r &lt; 1</math>]</li> <li>✓ answer</li> <li><b>Note:</b> CA applies</li> </ul> <p>Answer only: 1 / 3</p>
	5.3.3	4; 2; 1	<p>(2)</p> <ul style="list-style-type: none"> <li>✓ 4</li> <li>✓ 2 and 1</li> <li>[if <math>m</math> wrong can get max of 1 mark for method]</li> </ul>
	5.3.4	$S_{\infty} = \frac{a}{1-r}$ $= \frac{4}{1-\frac{1}{2}}$ $= 8$	<p>(2)</p> <ul style="list-style-type: none"> <li>✓ choice of formula</li> <li>✓ answer</li> <li><b>Note:</b> CA applies <b>provided</b> series is convergent, otherwise max. of 1 / 2</li> </ul>
5.4		$\frac{1(3^n - 1)}{3 - 1} > 100\,000$ $3^n > 200\,001$ $n > \frac{\log 200\,001}{\log 3} \approx 11,1$ $\therefore n \geq 12$ <p>so 12 terms</p>	<p>(6)</p> <ul style="list-style-type: none"> <li>✓ use of correct formula</li> <li>✓ substitution in formula</li> <li>✓ setting up inequality <b>or</b> equation</li> <li>✓ <math>3^n</math> as subject</li> <li>✓ use of logs</li> <li>✓ answer</li> <li><b>Note:</b> Trial and error methods acceptable</li> </ul>

5.5		$T_4 = S_4 - S_3$ $= 4^3 - 3^3$ $= 37$	(4)	✓ method ✓✓ values of $S_4$ and $S_3$ ✓ answer
			[32]	

6.1				<b>Note:</b> Penalise max of 1 mark for wrong notation in whole Q6
	6.1.1	Tangent to curve at P	(2)	✓ tangent ✓ P
	6.1.2	$f(x+h) = \frac{1}{2}(x+h)^2 + x+h$ $= \frac{1}{2}x^2 + xh + \frac{1}{2}h^2 + x+h$ $f(x+h) - f(x) = xh + \frac{1}{2}h^2 + h$ $m = \frac{xh + \frac{1}{2}h^2 + h}{h}$ $= x + \frac{1}{2}h + 1$ <p>Accept:</p> $f(x+h) = \frac{1}{2}(x+h)^2 + x+h$ $f(x+h) - f(x) = \frac{1}{2}(x+h)^2 + x+h - (\frac{1}{2}x^2 + x)$ $m = \frac{\frac{1}{2}(x+h)^2 + x+h - (\frac{1}{2}x^2 + x)}{h}$	(4)	✓ substitution ✓ simplification ✓ subtraction ✓ answer ✓✓ substitution ✓ subtraction ✓ answer
	6.1.3	$\lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} = \lim_{h \rightarrow 0} (x + \frac{1}{2}h + 1)$ $= x + 1$	(2)	✓ substitution of answer to Question 6.1.2 for quotient ✓ answer CA applies
	6.1.4	$f'(x) = x + 1$ $f'(1) + f'(2) = 2 + 3 = 5$ <p>but <math>f'(3) = 4</math></p> <p>∴ Not equal</p>	(4)	✓ derivative ✓ value of sum of derivatives ✓ value of derivative of sum ✓ Not equal
6.2	6.2.1	$g(x) = \frac{-2x}{\sqrt{x}} - x^{10} = -2x^{\frac{1}{2}} - x^{10}$ $g'(x) = -x^{-\frac{1}{2}} - 10x^9$ <p>[Accept: <math>g'(x) = \frac{1}{2} \times (-2x^{-\frac{1}{2}}) - 10x^9</math> ]</p>	(3)	✓ simplification of g ✓✓ each term in derivative of g



	6.2.2	$h(x) = (x^5 + 5x^{-1})(x^5 - 5x^{-1}) = x^{10} - 25x^{-2}$ $h'(x) = 10x^9 + 50x^{-3}$ <p>[accept: <math>10x^9 - 2(-25)x^{-3}</math>]</p>	(3)	✓✓ simplification of $h$ ✓ derivative of $h$
	6.2.3	$\frac{d}{dx}[2g(x) + h(x)] = 2g'(x) + h'(x)$ $= -2x^{-\frac{1}{2}} - 20x^9 + 10x^9 + 50x^{-3}$ $= -2x^{-\frac{1}{2}} - 10x^9 + 50x^{-3}$ <p>[Accept: <math>2(-2 \times \frac{1}{2}x^{-\frac{1}{2}} - 10x^9) + 10x^9 + 50x^{-3}</math>]</p> <p><b>OR</b></p> $\frac{d}{dx}[2g(x) + h(x)]$ $= \frac{d}{dx}[2(-2x^{\frac{1}{2}} - x^{10}) + x^{10} - 25x^{-2}]$ $= \frac{d}{dx}[-4x^{\frac{1}{2}} - x^{10} - 25x^{-2}]$ $= -2x^{-\frac{1}{2}} - 10x^9 + 50x^{-3}$	(4)	✓✓✓ applying differentiation laws ✓ substitution  ✓ substitution  ✓ simplification  ✓✓ answer [1 <sup>st</sup> and last term]
				<b>[22]</b>

7.1				
	7.1.1	$5^3 - 9.5^2 + 24.5 = 20$ $\therefore P$ is on the graph	(2)	✓ substitution ✓ "=20"
	7.1.2	$f(x) = x^3 - 9x^2 + 24x$ $f'(x) = 3x^2 - 18x + 24$ at turning point $f'(x) = 0$ $3x^2 - 18x + 24 = 0$ $x^2 - 6x + 8 = 0$ $(x - 4)(x - 2) = 0$ $x = 4$ or $x = 2$ $y = 16$ or $y = 20$ turning points: (4 ; 16) and (2 ; 20)	(6)	✓ differentiation ✓ derivative equal to 0  ✓ factorising ✓ values of $x$ ✓ values of $y$
	7.1.3		(5)	✓ shape ✓ through origin ✓ each turning point  <b>Note:</b> CA from 7.1.2 applies with each turning point.
	7.1.4	(a) max. is 20 (b) occurs at $x = 2$ and $x = 5$ (c) min. is 0	(1) (3) (1)	✓ answer ✓ 2 ✓ 5 ✓ answer  <b>Note:</b> CA applies according to candidate's graph.
7.2				
		$C'(x) = 5 + 0,003x^2$ $C'(100) = 5 + 0,003(100)^2$ $= 35$ rand/shirt	(4)	✓ derivative  ✓ substitution ✓ answer ✓ units