

POSSIBLE ANSWERS FOR:

-1- *Mathematics First Paper SG*
NATIONAL SENIOR CERTIFICATE -SET B

QUESTION 1

| | | | |
|-------|---|-----|--|
| 1.1.1 | $f(-1) = 2(-1)+3$ = 1 | (2) | ✓ substitution ✓ correct answer |
| 1.1.2 | $2x + 3 = -1$ $\therefore x = -2$. | (2) | ✓ correct statement ✓ answer |
| 1.2 | $2x^2 - 6x - 1 = 0$ $x = \frac{6 \pm \sqrt{36 - 4(2)(-1)}}{4}$ $= \frac{6 \pm \sqrt{44}}{4}$ $= 3,16 \text{ or } -0,16$ | (5) | ✓ standard form ✓ substitution ✓ simplification ✓ ✓ one each answer |
| 1.3 | $y+2 = 2x \dots \dots \dots \quad (1)$ $y = 2x - 2$ Substitute in $2x^2 = 2 - y^2$ $\therefore 2x^2 = 2 - (2x - 2)^2$ $= 2 - (4x^2 - 8x + 4)$ $= 2 - 4x^2 + 8x - 4$ $\therefore 6x^2 - 8x + 2 = 0 \text{ or } 3x^2 - 4x + 1 = 0$ $\therefore (3x - 1)(2x - 2) = 0$ $\therefore x = \frac{1}{3} \text{ or } x = 1$ $\therefore y = -1\frac{1}{3} \text{ or } y = 0$ | (8) | ✓ solve y in (1) ✓ substitute y in (2) ✓ finding product ✓ simplification ✓ factorization ✓ for both x values ✓ ✓ for each y |

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QUESTION 2

| | | | |
|-----|--|-----|---|
| 2.1 | $10x^2 - x - 2 = 0$ $\therefore \Delta = b^2 - 4ac$ $= 1 + 80$ $= 81$ Roots are rational and unequal | (4) | ✓ know to use delta ✓ substitution ✓ rational ✓ unequal |
|-----|--|-----|---|

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2.2.1 $3x^2 - 4x + p = 0$

$$\Delta = b^2 - 4ac \\ = 16 - 12p$$

For non-real roots $\Delta < 0$

$$16 - 12p < 0$$

$$p > \frac{4}{3}$$

- ✓ know delta
- ✓ correct substitution
- ✓ ✓ correct statement about delta

(6) $\checkmark \frac{4}{3} \checkmark > \text{sign}$

2.2.2 $p=1$

(2) $\checkmark \checkmark \text{ answer}$
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QUESTION 3

3.1.1.1 $r^2 = x^2 + y^2$
 $= 2^2 + (3)^2$
 $= 4 + 9$
 $= 13$

✓ substitution

$$y = \sqrt{13 + x^2}$$

(3) ✓ form of equation

3.1.1.2 $xy = k$
 $k = 2(3) = -8$

(2) ✓ format
✓ $k = (2)(3)$

3.1.2 $B(3; 2)$

(1) ✓ answer

3.2 Say function is $f(x) = mx + c$

$$f(0) = m(0) + c = -3 \quad \therefore c = -3$$

✓ substitute, $f(0) = -3$
✓ $c = -3$

and $f(1) = m(1) - 3 = 0 \quad \therefore m = 3$

✓ substitute(1) = 0
✓ $m = 3$

Equation: $y = 3x - 3$

(5) ✓ answer

OR

x/c: (1; 0) ✓

y/c: (0; -3) ✓

$$m = \frac{-3}{-1} = 3 \quad \checkmark \quad \therefore y = 3x - 3 \quad \checkmark$$

3.3.1

Turning point: (1; -4)

✓ answer

$$\text{and } (x-1)^2 - 4 = x^2 - 2x + 1 - 4$$

$$= x^2 - 2x - 3$$

$$= (x-3)(x+1) = 0$$

$$x = 3 \text{ or } x = -1$$

✓ expanding

✓ factorization

✓ both values of x

OR

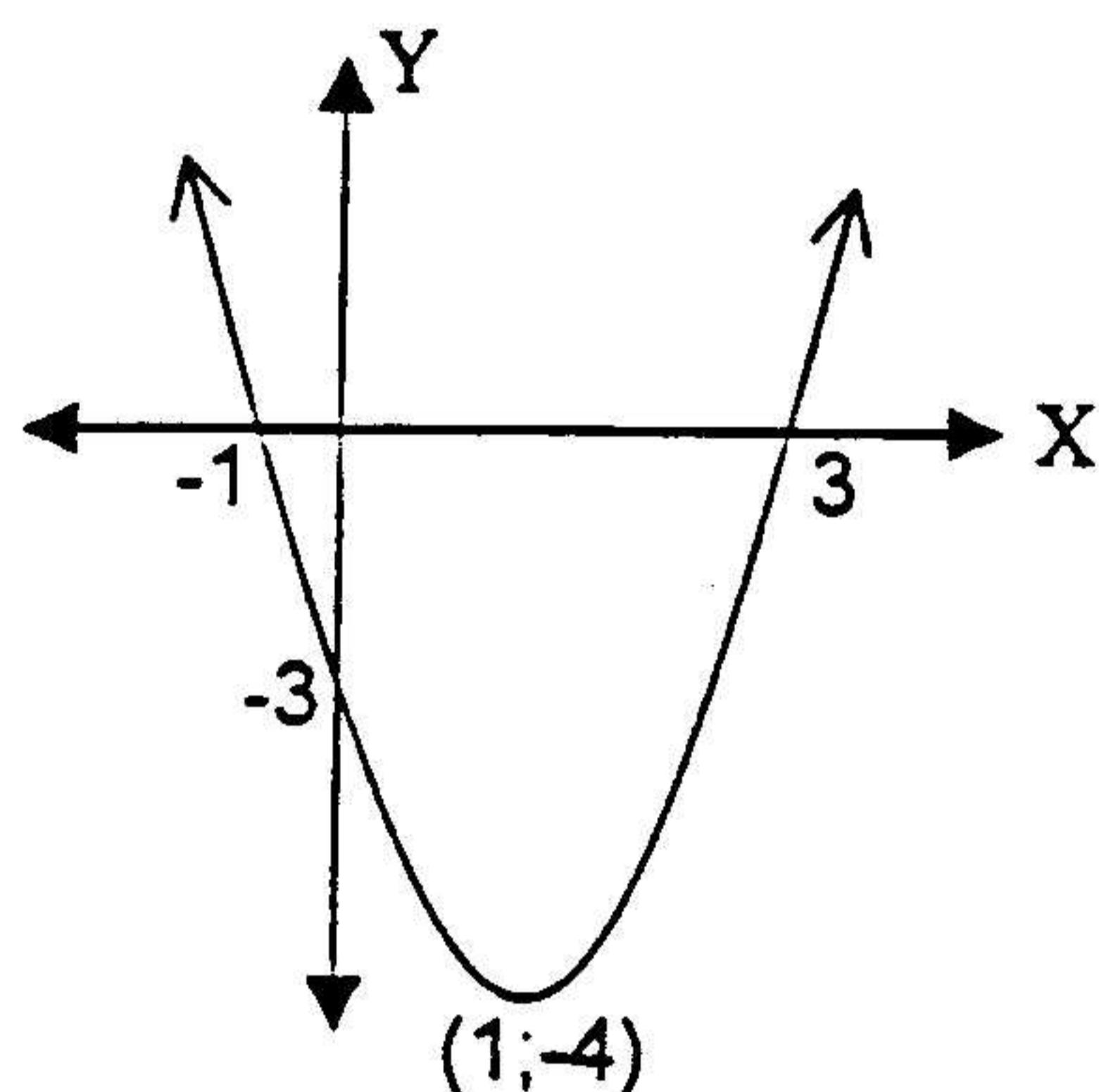
$$(x-1)^2 - 4 = 0$$

$$(x-1)^2 = 4$$

$$x-1 = \pm 2$$

$$x = 3 \text{ or } -1$$

Cut y-axis -3



(7)

- ✓ x intercepts
- ✓ y intercept
- ✓ turning point

3.3.2 $x \leq -1 \text{ or } x \geq 3$

(2)

- ✓ $x \leq -1$
- ✓ $x \geq 3$

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QUESTION 4

4.1 $x - a$ is a factor of $f(x)$

✓ correct answer

OR

 a is a root of $f(x)$

(1)

4.2 $f(x) = 2x^3 - 3x^2 + kx - 4$

$$f(-1) = 4$$

$$4 = 2(-1)^3 - 3(-1)^2 + k(-1) - 4$$

$$k = -13$$

(4)

- ✓ subs $x = -1$, ✓ $f(-1) = 4$
- ✓ simplification
- ✓ answer - 13

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4.3.1

$$f(x) = x^3 - 12x - 16$$

Put $f(-2) = -8 + 24 - 16 = 0$
 $\therefore x + 2$ is a factor

(2)

- ✓ get $f(-2)$
- ✓ get = 0

4.3.2

$$\begin{aligned} x^3 - 12x - 16 &= (x + 2)(x^2 - 2x - 8) \\ &= (x + 2)(x - 4)(x + 2) \\ x &= -2 \text{ or } 4 \end{aligned}$$

(4)

- ✓ ✓ quadratic factor (✓ -2 ; ✓ -8)
- ✓ linear factors
- ✓ solutions

[11]

QUESTION 5

5.1

$$4^x = \frac{1}{64}$$

$$(2^2)^x = \frac{1}{2^6} \quad OR \quad 4^x = \frac{1}{4^3}$$

- ✓ same base (2 or 4)

$$2^{2x} = 2^{-6} \quad OR \quad 4^x = 4^{-3}$$

- ✓ same base 2 or 4

$$2x = -6$$

$$x = -3 \quad OR \quad x = -3$$

(3)

- ✓ answer

5.2

$$\begin{aligned} \frac{2 \cdot 3^x - 3^{x-1}}{5 \cdot 3^x} &= \frac{2 \cdot 3^x - 3^x \cdot 3^{-1}}{5 \cdot 3^x} \\ &= \frac{3^x(2 - 3^{-1})}{5 \cdot 3^x} \\ &= \frac{2 - 3^{-1}}{5} = \frac{2 - \frac{1}{3}}{5} = \frac{\frac{5}{3}}{5} \\ &= \frac{1}{3} \end{aligned}$$

(5)

- ✓ breaking up

- ✓ remove common factor correctly

- ✓ cancellation CF

$$\checkmark 3^{-1} = \frac{1}{3}$$

- ✓ answer

OR

$$\begin{aligned} \frac{2 \cdot 3^x - 3^{x-1}}{5 \cdot 3^x} &= \frac{2 \cdot 3 \cdot 3^{x-1} - 3^{x-1}}{5 \cdot 3 \cdot 3^{x-1}} \\ &= \frac{3^{x-1}(6 - 1)}{15 \cdot 3^{x-1}} \\ &= \frac{5}{15} \\ &= \frac{1}{3} \end{aligned}$$

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5.3
$$\frac{\sqrt{5}+2}{\sqrt{5}} \cdot \frac{\sqrt{5}}{\sqrt{5}} = \frac{5+2\sqrt{5}}{5}$$

OR
$$\frac{\sqrt{5}}{\sqrt{5}} + \frac{2}{\sqrt{5}} = 1 + \frac{2\sqrt{5}}{5}$$

(3) [11]

- ✓ multiplying by $\frac{\sqrt{5}}{\sqrt{5}}$
- ✓ simplify numerator
- ✓ simplify denominator

QUESTION 6

6.1.1 $\log_x 0,25 = 2$

$$0,25 = x^2$$

$$(0,5)^2 = x^2$$

$$x = \pm 0,5$$

$$x = 0,5 (x > 0)$$

(3)

- ✓ switch from log to exp form
- ✓ to powers 2/process
- ✓ answer

OR

$$x^2 = \frac{1}{4} = \left(\frac{1}{2}\right)^2$$

$$x = \frac{1}{2}$$

6.1.2 $\log 25 - \log(x-1) = 1$

$$\log \frac{25}{(x-1)} = 1 = \log 10$$

$$\frac{25}{x-1} = 10$$

$$10x - 10 = 25$$

$$10x = 35$$

$$x = \frac{35}{10} = \frac{7}{2}$$

(5)

- ✓ $\log 10 = 1$
- ✓ log laws applied
- ✓ without logs
- ✓ simplification
- ✓ answer

OR

$$\log 25 - \log(x-1) = 1$$

$$\log \frac{25}{(x-1)} = 1$$

$$\frac{25}{x-1} = 10^1$$

$$10x - 10 = 25$$

$$10x = 35$$

$$x = \frac{35}{10} = \frac{7}{2}$$

- ✓ correct application
- ✓ ✓ log to exponent
- ✓ simplification
- ✓ answer

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6.2

$$\begin{aligned}
 A &= P \left(1 + \frac{r}{100} \right)^n \\
 &= 375 \left(1 + \frac{9}{100} \right)^4 \\
 &= 375(1.09)^4 \\
 &= 529,3431 \\
 \therefore \text{the expenses are R } &529\,343\,100
 \end{aligned}$$

(6)

[14]

✓ formula

✓ ✓ ✓ substituting K, r and n

✓ answer calculated

✓ answer transferred to monetary terms

QUESTION 7

7.1

$$\begin{aligned}
 \sum_{k=1}^3 a \cdot 2^{k-1} &= 28 \\
 a \cdot 2^0 + a \cdot 2^1 + a \cdot 2^2 &= 28 \\
 7a &= 28 \\
 a &= 4
 \end{aligned}$$

(4)

✓ ✓ expanding correctly

✓ simplification

✓ answer

7.2.1

$$\begin{aligned}
 T_n &= a + (n - 1)d \\
 T_3 &= a + 2d = -7 \\
 T_7 &= a + 6d = 9 \\
 4d &= 16 \\
 d &= 4 \\
 a &= -15
 \end{aligned}$$

(5)

✓ formula

✓ substitution T_3

✓ substitution T_7

✓ d

✓ a

7.2.2

$$\begin{aligned}
 T_{51} &= a + 50d \\
 &= -15 + 50(4) \\
 &= 185
 \end{aligned}$$

(2)

✓ substituting in formula

✓ answer

7.2.3

$$\begin{aligned}
 S_n &= \frac{n}{2}(a + l) \\
 &= \frac{51}{2}(-15 + 185) \\
 &= 4335
 \end{aligned}$$

(3)

✓ formula

✓ substitution

✓ answer

OR

$$\begin{aligned}
 S_n &= \frac{n}{2}[2a + (n - 1)d] \\
 &= \frac{51}{2}[-30 + 50 \cdot 4] \\
 &= 4335
 \end{aligned}$$

7.3.1 $a = 1, r = -3$

✓ a and r

$$T_n = ar^{n-1}$$

✓ formula

$$T_8 = ar^7$$

$$= (-3)^7$$

$$= -2187$$

(4)

✓ substitution

✓ answer

7.3.2

$$S_n = \frac{a(r^n - 1)}{r - 1}$$

✓ formula

$$= \frac{(-3)^8 - 1}{(-3) - 1}$$

✓ substitution

$$= -1640$$

(3)

✓ answer

7.4

$$a = 280, r = 2, S_n = 143080$$

✓ values of a, r and S

$$S_n = \frac{a(r^n - 1)}{r - 1}$$

✓ formula

$$\frac{280(2^n - 1)}{2 - 1} = 143080$$

$$2^n - 1 = 511$$

✓ simplification

$$2^n = 512$$

(7)

✓ exponential form

$$2^n = 2^9$$

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✓ answer

$$n = 9$$

QUESTION 8

- 8.1.1
$$\begin{aligned} f'(x) &= \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} \\ &= \lim_{h \rightarrow 0} \frac{-2(x+h)^2 - (-2x^2)}{h} \\ &= \lim_{h \rightarrow 0} \frac{-2(x^2 + 2xh + h^2) - (-2x^2)}{h} \\ &= \lim_{h \rightarrow 0} \frac{-2x^2 - 4xh - 2h^2 + 2x^2}{h} \\ &= \lim_{h \rightarrow 0} \frac{h(-4x - 2h)}{h} \\ &= \lim_{h \rightarrow 0} (-4x - 2h) \\ &= -4x \end{aligned}$$
 (5) ✓ correct substitution
✓ expand $(x + h)$
✓ brackets removed
✓ eliminating h
✓ answer
- 8.1.2 $f'(x) = -4x$
 $f'(-1) = 4$
Gradient is 4 (2) ✓ derivative
✓ answer
- 8.1.3
$$\begin{aligned} \frac{f(3) - f(-1)}{3 - (-1)} &= \frac{-2(3)^2 - [-2(-1)^2]}{4} \\ &= -4 \end{aligned}$$
 (3) ✓ formula
✓ substitution
✓ answer
- 8.2.1
$$\begin{aligned} f(x) &= 4x^2 - 4x + 1 \\ f'(x) &= 8x - 4 \end{aligned}$$
 (2) ✓ multiply factors
✓ answer
- 8.2.2
$$\begin{aligned} y &= \sqrt{x} - \frac{2}{x} \\ &= x^{\frac{1}{2}} - 2x^{-1} \\ \frac{dy}{dx} &= \frac{1}{2}x^{-\frac{1}{2}} + 2x^{-2} \end{aligned}$$
 (4) ✓ ✓ writing as powers
✓ ✓ finding answers
- 8.3.1
$$\begin{aligned} f(x) &= (x+1)^2(x-1) = 0 \\ x &= -1; 1 \\ BA &= 2 \end{aligned}$$
 (3) ✓ $f(x) = 0$
✓ x values
✓ length BA

8.3.2

$$f'(x) = 3x^2 + 2x - 1 = 0$$

$$(3x - 1)(x + 1) = 0$$

$$x = \frac{1}{3} \quad \text{or} \quad -1$$

$$f\left(\frac{1}{3}\right) = \left(\frac{1}{3}\right)^3 + \left(\frac{1}{3}\right)^2 - \frac{1}{3} - 1$$

$$= \frac{1}{27} + \frac{1}{9} - \frac{1}{3} - 1$$

$$= \frac{-32}{27} (-1\frac{5}{27})$$

$$E \text{ is } \left(\frac{1}{3}; \frac{-32}{27}\right)$$

(6)

- ✓ derivative
- ✓ =0
- ✓ factors
- ✓ answers for x

✓ correct answer for $f\left(\frac{1}{3}\right)$

✓ coordinates E

8.3.3

$$3x^2 + 2x - 1 = \frac{5}{3}$$

$$9x^2 + 6x - 8 = 0$$

$$(3x + 4)(3x - 2) = 0$$

$$x = -\frac{4}{3} \text{ or } x = \frac{2}{3}$$

(5)

[30]

✓ ✓ derivative = $\frac{5}{3}$

✓ standard form

✓ factorization

✓ x answer

QUESTION 9

9.1

$$QL = 4 - x$$

(1)

✓ answer

9.2

$$A = QP^2$$

$$= x^2 + (4 - x)^2$$

$$= x^2 + 16 - 8x + x^2$$

$$= 2x^2 - 8x + 16$$

(3)

✓ answer

9.3

$$\frac{dA}{dx} = 4x - 8 = 0$$

$$x = \frac{8}{4} = 2$$

(3)

✓ derivative

✓ =0

✓ get x

[7]

TOTAL: 150