## $A Q A$

# Level 2 Certificate in Further Mathematics 

## Practice Paper Set 4

Paper 2 8360/2

## Mark Schemes

Principal Examiners have prepared these mark schemes for practice papers. These mark schemes have not, therefore, been through the normal process of standardising that would take place for live papers.

It is not possible to indicate all the possible approaches to questions that would gain credit in a 'live' examination. The principles we work to are given in the glossary on page 3 of this mark scheme.

- Evidence of any method that would lead to a correct answer, if applied accurately, is generally worthy of credit.
- Accuracy marks are awarded for correct answers following on from a correct method. The correct method may be implied, but in this qualification there is a greater expectation that method will be appropriate and clearly shown.


## Glossary for Mark Schemes

These examinations are marked in such a way as to award positive achievement wherever possible. Thus, for these papers, marks are awarded under various categories.

M Method marks are awarded for a correct method which could lead to a correct answer.

A Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.

B Marks awarded independent of method.
ft Follow through marks. Marks awarded for correct working following a mistake in an earlier step.

SC Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.

Mdep A method mark dependent on a previous method mark being awarded.

B dep A mark that can only be awarded if a previous independent mark has been awarded.
oe
Or equivalent. Accept answers that are equivalent.
eg, accept 0.5 as well as $\frac{1}{2}$
$[a, b] \quad$ Accept values between $a$ and $b$ inclusive.
$3.14 \ldots \quad$ Allow answers which begin 3.14 eg 31.4, 3142, 3.149
Use of brackets It is not necessary to see the bracketed work to award the marks.

## Paper 2 - Calculator

| Q | Answer |  |  |
| :---: | :---: | :---: | :---: |
| Mark | Comments |  |  |
| $\mathbf{1}$ | positive odd | B1 | Exactly two boxes selected in each |
|  | negative even | B1 |  |
|  | positive odd | B1 |  |


| 2(a) | $P^{2}=Q R-1$ | M 1 |  |
| :--- | :--- | :---: | :--- |
|  | $P^{2}+1=Q R$ | M 1 | Correct step after their first step |
|  | $\frac{P^{2}+1}{R}=Q$ | A 1 |  |
| 2(b) | $\frac{12^{2}+1}{5}$ | M 1 | $145=5 Q$ |
|  | 29 | A 1 |  |

$\begin{array}{|c|l|c|l|}\hline 3 & 7 x+8 x=180 & \text { M1 } & \text { oe eg } 7 x=180-8 x \\$\cline { 2 - 4 } \& $x=12 & \text { A1 } & \begin{array}{l}7 x=84 \text { and } 8 x=96 \\
\text { May be seen on diagram }\end{array} \\$\cline { 2 - 4 } \& $2 \times \text { their } 12+60 & \text { M1 } & \begin{array}{l}84 \text { if correct } \\
\text { May be seen on diagram }\end{array} \\$\cline { 2 - 4 } \& \(\left.$$
\begin{array}{l}2 x+60=84 \text { and angle } P Q R=84 \\
\text { and Yes }\end{array}
$$ \& A1ft \& $$
\begin{array}{l}\text { ft from M1 A0 M1 } \\
\text { oe eg } 2 x+60=84 \quad \text { and } \\
\text { angle } S R Q=96 \text { and } \\
\text { angle } P Q C=96 \text { and } \\
\text { Yes }\end{array}
$$ <br>

Angles may be seen on diagram\end{array}\right]\)|  |
| :--- |


| Q Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 4(a) | $(0,0)$ and (-6, 8) | B1 | Seen or implied |
| :---: | :---: | :---: | :---: |
|  | $(-6)^{2}+8^{2}$ | M1 | oe eg $6^{2}+8^{2}$ or 100 or $\sqrt{100}$ |
|  | 10 | A1 |  |
| 4(b) | Do not overlap and complete reason <br> Example 1: <br> Do not overlap and $4+5<10$ <br> Example 2: <br> Do not overlap and diagram drawn showing 4, 5 and 10 in appropriate places <br> Example 3: <br> Do not overlap and there will be a gap of 1 | B2ft | ft their distance in (a) <br> B1ft Do not overlap and partial reason <br> Example 1 <br> Do not overlap and 9 <br> Example 2 <br> Do not overlap and diagram drawn showing two of 4,5 and 10 <br> B1 4 and 5 seen |


| 5(a) | $n^{-4}$ | B2 | B1 $\left(n^{2}\right)^{5}=n^{10}$ seen or implied eg $\frac{1}{n^{4}}$ |
| :---: | :---: | :---: | :---: |
| 5(b) | $c^{2}+1$ | B2 | B1 for each correct term <br> Do not accept $c^{2}+c^{0}$ for B2 <br> Accept $c^{0}$ as an alternative to 1 for B1 |
| 5(c) | $\left(\frac{1}{2}\right)^{4}$ | M1 | oe |
|  | $\frac{1}{16} \text { or } 0.0625$ | A1 |  |


| 6(a) | $30 \times 20-4 \times x \times x$ | M1 | $\begin{aligned} \text { oe eg } & 2 x(30-2 x)+2 x(20-2 x) \\ & +(30-2 x)(20-2 x) \end{aligned}$ |
| :---: | :---: | :---: | :---: |
|  | $600-4 x^{2}$ | A1 | oe eg $4\left(150-x^{2}\right)$ |
| 6(b) | $(30-2 x)$ or (20-2x) | B1 | Seen or implied |
|  | $x(30-2 x)(20-2 x)$ | M1 | ft their three dimensions but all must be in terms of $x$ |
|  | $x\left(600-60 x-40 x+4 x^{2}\right)$ | M1dep | ft their three dimensions but must involve product of two linear expressions |
|  | $600 x-100 x^{2}+4 x^{3}$ | A1 |  |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 7(a) | $\frac{S T}{\sin 54}=\frac{40}{\sin (180-54-25)}$ | M1 | $\frac{S T}{\sin 54}=\frac{40}{\sin 101}$ |
| :---: | :---: | :---: | :---: |
|  | $(S T=) \frac{40}{\sin 101} \times \sin 54$ | M1 dep | Must use 101 <br> Allow M2 if this is the first line of working |
|  | 32.966(....) | A1 | Only award if correct working for both M marks are seen |
| 7(b) | $\sin 25=\frac{w}{32.97}$ | M1 | $\cos 65=\frac{w}{32.97}$ |
|  | $32.97 \times \sin 25$ | M1 dep | Allow $32.97 \times \cos 65$ |
|  | [13.9, 13.934] | A1 | Allow 14 if correct method seen $\begin{aligned} & \text { SC2 [12.6, 12.62] } \\ & \text { SC1 [-4.4, -4.3636] } \end{aligned}$ |


| 8 | $\left(A X^{2}=\right) 3^{2}+3^{2}(=18)$ | M 1 | oe eg $(A X=) \sqrt{18}$ or [4.2, 4.243] |
| :---: | :---: | :---: | :---: |
|  | $10^{2}-$ their $18 \quad(=82)$ | M 1 |  |
|  | $\sqrt{10^{2}-\text { their } 18}$ | M1 dep |  |
|  | $[9.055,9.1]$ or $\sqrt{82}$ | A1 |  |


| 9(a) | $-2 \leqslant x \leqslant 4$ | B2 | B1 $-2<x \leqslant 4$ or $-2 \leqslant x<4$ <br> or $-2<x<4$ <br> SC1 Fully correct response in words |
| :---: | :---: | :---: | :---: |
| 9(b) | $-3 \leqslant g(x) \leqslant 5$ | B2 | B1 $-3<\mathrm{g}(x) \leqslant 5$ or $-3 \leqslant \mathrm{~g}(x)<5$ or $-3<g(x)<5$ <br> SC1 Fully correct response in words |
| 9(c) | -1.2 | B1 |  |
|  | 3 | B1 |  |
| 9(d) | -4 | B2 | B1 4 or $-\frac{8}{2}$ oe |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 10 | Enlargement | B1 |  |
| :--- | :--- | :---: | :--- |
|  | Scale factor -2 | B1 |  |
|  | Centre (0,0) | B1 |  |


| 11(a) | $(n+1)^{2}+(n+1) \quad\left(-\left(n^{2}+n\right)\right)$ | M1 |  |
| :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & n^{2}+2 n+1+n+1-n^{2}-n \\ & (=2 n+2) \end{aligned}$ | A1 | oe <br> Example 1: $n^{2}+3 n+2+n+1-n^{2}-n(=2 n+2)$ <br> Example 2: $n^{2}+n+n+1+n+1-n^{2}-n(=2 n+2)$ <br> Must be clearly shown and have brackets removed <br> $=2 n+2$ is not needed but if simplification shown it must be correct |
| 11(b) | $2 n+2=32$ | M1 |  |
|  | $n=15$ | A1 |  |
|  | their $15^{2}+$ their 15 or (their $15+1)^{2}+$ their $15+1$ | M1 |  |
|  | 240 and 272 | A1 |  |


| Q Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 12(a) | $35+4 x^{2}=36$ | B1 |  |
| :---: | :---: | :---: | :---: |
|  | $\begin{array}{ll} 4 x^{2}=1 & \text { or } \\ (2 x+1)(2 x-1) & \text { or } \\ \frac{0 \pm \sqrt{0^{2}-4 \times 4 \times-1}}{2 \times 4} & \end{array}$ | M1 | Simplifies their quadratic to $a x^{2}=b$ or correctly factorises their quadratic or substitutes correctly for their quadratic |
|  | $\frac{1}{2}$ and $-\frac{1}{2}$ | A1ft | ft from B0 M1 <br> Must have 2 solutions |
| 12(b) | $27=8 x^{3}$ | M1 | oe eg $\frac{27}{8}=x^{3}$ <br> Must have $x^{3}$ |
|  | $3=2 x$ | M1 dep | $\sqrt[3]{\frac{27}{8}}$ |
|  | $\frac{3}{2}$ | A1 | oe Solutions $\frac{3}{2}$ and $-\frac{3}{2}$ is AO |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 13 | $\angle S Q R=2 x$ | M1 | Working may be seen on the diagram throughout |
|  | $\angle Q R S \text { or } \angle Q S R=\frac{180-\text { their } 2 x}{2}$ | M1 | $90-x$ |
|  | $\begin{aligned} & 7 x+\text { their }(90-x)=180 \text { or } \\ & 2 x+\text { their }(90-x)=7 x \end{aligned}$ | M1 | oe eg $6 x=90$ |
|  | 15 | A1 |  |
|  | Alternative method 1 |  |  |
|  | $\angle Q R S=180-7 x$ | M1 | Working may be seen on the diagram throughout |
|  | $\angle Q S R=$ their (180-7x) | M1 |  |
|  | $2 x+$ their $(180-7 x)=7 x$ | M1 | oe eg $12 x=180$ |
|  | 15 | A1 |  |
|  | Alternative method 2 |  |  |
|  | $\angle Q R S=180-7 x$ | M1 | Working may be seen on the diagram throughout |
|  | $\angle S Q R=180-2 \times$ their ( $180-7 x$ ) | M1 | oe eg $\angle S Q R=14 x-180$ |
|  | $2 x=$ their $(14 x-180)$ | M1 | oe eg $12 x=180$ |
|  | 15 | A1 |  |
|  | Alternative method 3 |  |  |
|  | $\angle Q S R=5 x$ | M1 | Working may be seen on the diagram throughout |
|  | $\angle S R Q=$ their $5 x$ | M1 |  |
|  | $7 x+$ their $5 x=180$ | M1 | oe eg $12 \mathrm{x}=180$ |
|  | 15 | A1 |  |
|  | Alternative method 4 |  |  |
|  | $\angle Q S R=5 x$ | M1 | Working may be seen on the diagram throughout |
|  | $\angle S R Q=$ their $5 x$ | M1 |  |
|  | $\begin{aligned} & \angle S Q R=2 x \text { and } \\ & \text { their } 5 x+\text { their } 5 x+2 x=180 \end{aligned}$ | M1 | oe eg $12 x=180$ |
|  | 15 | A1 |  |


| Q Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 14 | $\sin ^{-1}-\frac{1.36}{2} \quad(=[-42.844,-42.8])$ | M1 | oe eg $\sin ^{-1}-0.68$ |
| :---: | :---: | :---: | :---: |
|  | [222.8, 222.844] | A1 |  |
|  | [317.156, 317.2] | A1ft | ft 540 - their [222.8, 222.844] |
|  | Alternative method |  |  |
|  | $\sin ^{-1}-\frac{1.36}{2}(=[-42.844,-42.8])$ | M1 | oe eg $\sin ^{-1}-0.68$ |
|  | [317.156, 317.2] | A1 |  |
|  | [222.8, 222.844] | A1ft | ft 540 - their [317.156, 317.2] |

15

| $2+8 x-2 x^{2}=5$ | M1 |  |
| :---: | :---: | :---: |
| $(0=) 2 x^{2}-8 x+3$ | A1 | $-3+8 x-2 x^{2} \quad(=0)$ |
| $\frac{--8 \pm \sqrt{(-8)^{2}-4 \times 2 \times 3}}{2 \times 2}$ | M1 | oe eg $\frac{8 \pm \sqrt{64-24}}{4}$ <br> ft their 3-term quadratic |
| [3.58, 3.6] and [0.4, 0.42] | A1 | oe eg $\frac{8+\sqrt{40}}{4}$ and $\frac{8-\sqrt{40}}{4}$ |
| [3.16, 3.2] | A1ft | oe eg $\frac{\sqrt{40}}{2}$ or $\sqrt{10}$ <br> ft their 3-term quadratic solutions |
| Alternative method |  |  |
| $2+8 x-2 x^{2}=5$ | M1 |  |
| $x^{2}-4 x=-\frac{3}{2}$ | A1 | oe |
| $(x-2)^{2}-4=-\frac{3}{2}$ | M1 | oe eg $(x-2)^{2}=\frac{5}{2}$ <br> ft their 3-term quadratic |
| [3.58, 3.6] and [0.4, 0.42] | A1 | oe eg $\sqrt{\frac{5}{2}}+2$ and $-\sqrt{\frac{5}{2}}+2$ |
| [3.16, 3.2] | A1ft | oe eg $2 \sqrt{\frac{5}{2}}$ or $\sqrt{10}$ <br> ft their 3-term quadratic solutions |


| Q | Answer |  | Comments |  |
| :---: | :---: | :---: | :---: | :---: |
| 16 | $\sin ^{2} x+\cos ^{2} x$ or $-\cos x \sin x+\sin x \cos x$ | M1 | oe eg $\cos x \cos x+\sin x \sin x$ <br> One correct element <br> Does not have to be seen in a matrix |  |
|  | $\left(\begin{array}{cc}\sin ^{2} x+\cos ^{2} x & -\cos x \sin x+\sin x \cos x \\ -\cos x \sin x+\sin x \cos x & \sin ^{2} x+\cos ^{2} x\end{array}\right)$ |  | ) M1 | oe <br> All 4 correct elements in correct positions in a matrix |
|  | $\left(\begin{array}{ll}1 & 0 \\ 0 & 1\end{array}\right)$ |  | oe eg I or identity (matrix) |  |


| 17 | Any two of: $\begin{array}{lll} a+5 b=5 & \text { or } & 2 a+8 b=6 \text { or } \\ 3 a+12 b=9 & \text { or } & 4 a+17 b=14 \end{array}$ | B2 | B1 Any one of: $\begin{array}{lll} a+5 b=5 & \text { or } & 2 a+8 b=6 \text { or } \\ 3 a+12 b=9 & \text { or } & 4 a+17 b=14 \end{array}$ |
| :---: | :---: | :---: | :---: |
|  | Makes their pair of equations have a common coefficient and subtraction attempt $\text { eg } \begin{aligned} & 2 a+10 b=10 \\ & 2 a+8 b=6 \quad \text { and } \\ & 2 b=4 \end{aligned}$ | M1 | Allow up to two errors |
|  | $b=2$ | A1 |  |
|  | $a=-5$ | A1 |  |
|  | Alternative method |  |  |
|  | (First differences) $a+3 b \quad a+4 b \quad a+5 b$ | M1 | At least 2 correct |
|  | (Second differences) $b \quad b$ | A1 |  |
|  | $b=2$ | A1 |  |
|  | Any one of: $\begin{array}{lll} a+5 b=5 & \text { or } & 2 a+8 b=6 \text { or } \\ 3 a+12 b=9 & \text { or } & 4 a+17 b=14 \end{array}$ | B1 |  |
|  | $a=-5$ | B1ft | ft their $b$ |


| Q Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 18 | $3 m(8-3 m)$ or $m(24-9 m)$ | M1 |  |
| :---: | :--- | :---: | :--- |
|  | $(8+3 m)(8-3 m)$ | M1 |  |
|  | $\frac{3 m}{8+3 m}$ | A1 | Further incorrect work is A0 |


| 19 | $\cos (x)=\frac{8}{12}$ | M1 |  |
| :---: | :--- | :---: | :--- |
|  | $\cos ^{-1} \frac{8}{12}$ | M1 dep |  |
|  | $[48.1896851,48.2]$ | A1 | Allow 48 if correct method seen <br> SC2 [53.5, 53.5441] <br> SC1 [0.84, 0.8411] |


| 20(a) | $(-1,0)$ | B1 |  |
| :---: | :---: | :---: | :---: |
| 20(b) | $(y=) 2+2 x-x-x^{2}$ | M1 | $2+x-x^{2}$ |
|  | $\left(\frac{d y}{d x}=\right) 1-2 x$ | M1 dep | oe <br> ft their expansion |
|  | $\text { (At } x=0, \frac{d y}{d x}=\text { ) } 1$ | M1 | ft their $\frac{\mathrm{d} y}{\mathrm{~d} x}$ |
|  | grad normal = -1 | A1ft | ft their $\frac{\mathrm{d} y}{\mathrm{~d} x}$ Must have gained M3 |
|  | $y=($ their grad normal) $x+2$ | M1 | $y=-x+2$ if correct |
|  | $y=-x+2$ and $x=2 y=0$ | A1 | oe eg $y+x=2$ and $2+0=2$ |


| 21 | $a^{2} b\left(3 a^{2}-2 a b-5 b^{2}\right) \quad$ or | M1 |  |
| :---: | :--- | :--- | :--- | :--- |
| $a b\left(3 a^{3}-2 a^{2} b-5 a b^{2}\right)$ | or |  |  |
| $a^{2}\left(3 a^{2} b-2 a b^{2}-5 b^{3}\right)$ |  |  |  |
|  | $a^{2} b(3 a-5 b)(a+b)$ | A1 |  |


| Q Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 22(a) | $y=10$ | B 1 |  |
| :--- | :--- | :---: | :--- |
| 22(b) | $x=2$ | B 1 |  |
| 22(c) | Increasing | B 1 |  |
| 22(d) | $\left(\frac{\mathrm{d} y}{\mathrm{~d} x}=\right) 3 p x^{2}-6 x+8$ | M 1 | At least 2 terms correct |
|  | $3 p \times(2)^{2}-6 \times 2+8=0$ | M 1 | oe <br> Substitutes $x=2$ in their $\frac{\mathrm{d} y}{\mathrm{~d} x}$ <br> a quadratic and equates to zero |
|  | $(p=) \frac{1}{3}$ | M 1 | oe <br> Substitutes $x=2$ in their $p x^{3}-3 x^{2}+8 x+r$ <br> and equates to 10 |
|  | $\frac{1}{3} \times(2)^{3}-3 \times(2)^{2}+8 \times 2+r=10$ | A 1 ft | ft their $p$ if M3 gained |

