## Ma

 Mathematics tests
## Mark scheme for Paper 1

Tiers 3-5, 4-6, 5-7 and 6-8
2003

KEY STAG
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## Introduction

The test papers will be marked by external markers. The markers will follow the mark scheme in this booklet, which is provided here to inform teachers.

This booklet contains the mark scheme for paper 1 at all tiers. The paper 2 mark scheme is printed in a separate booklet. Questions have been given names so that each one has a unique identifier irrespective of tier.

## The structure of the mark schemes

The marking information for questions is set out in the form of tables, which start on page 10 of this booklet. The columns on the left-hand side of each table provide a quick reference to the tier, question number, question part, and the total number of marks available for that question part.

The Correct response column usually includes two types of information:

- a statement of the requirements for the award of each mark, with an indication of whether credit can be given for correct working, and whether the marks are independent or cumulative;
- examples of some different types of correct response, including the most common.

The Additional guidance column indicates alternative acceptable responses, and provides details of specific types of response that are unacceptable. Other guidance, such as when 'follow through' is allowed, is provided as necessary.

Questions with a $U A M$ element are identified in the mark scheme by an encircled $U$ with a number that indicates the significance of using and applying mathematics in answering the question. The $U$ number can be any whole number from 1 to the number of marks in the question.

The 2003 key stage 3 mathematics tests and mark schemes were developed by the Mathematics Test Development Team at QCA.

## General guidance

## Using the mark schemes

Answers that are numerically equivalent or algebraically equivalent are acceptable unless the mark scheme states otherwise.

In order to ensure consistency of marking, the most frequent procedural queries are listed on the following two pages with the prescribed correct action. This is followed by further guidance relating to marking of questions that involve money, time, coordinates, algebra or probability. Unless otherwise specified in the mark scheme, markers should apply the following guidelines in all cases.

What if ...
$\left.\begin{array}{|r|l|}\hline \begin{array}{r}\text { The pupil's response } \\ \text { does not match } \\ \text { closely any of the } \\ \text { examples given. }\end{array} & \begin{array}{l}\text { Markers should use their judgement in deciding whether the response } \\ \text { corresponds with the statement of requirements given in the Correct response } \\ \text { column. Refer also to the Additional guidance. }\end{array} \\ \hline \begin{array}{r}\text { The pupil has } \\ \text { responded in a } \\ \text { non-standard way. }\end{array} & \begin{array}{l}\text { Calculations, formulae and written responses do not have to be set out in any } \\ \text { particular format. Pupils may provide evidence in any form as long as its } \\ \text { meaning can be understood. Diagrams, symbols or words are acceptable for } \\ \text { explanations or for indicating a response. Any correct method of setting out } \\ \text { working, however idiosyncratic, is acceptable. Provided there is no ambiguity, } \\ \text { condone the continental practice of using a comma for a decimal point. }\end{array} \\ \hline \text { The pupil has made a } \\ \text { conceptual error. }\end{array} \begin{array}{l}\text { In some questions, a method mark is available provided the pupil has made } \\ \text { a computational, rather than conceptual, error. A computational error is } \\ \text { a slip such as writing } 4 \times 6=18 \text { in an otherwise correct long multiplication. } \\ \text { A conceptual error is a more serious misunderstanding of the relevant } \\ \text { mathematics; when such an error is seen no method marks may be awarded. } \\ \text { Examples of conceptual errors are: misunderstanding of place value, such as } \\ \text { multiplying by 2 rather than 20 when calculating 35 } \times 27 \text {; subtracting the }\end{array}\right\}$

What if ...

| The final answer is wrong but the correct answer is shown in the working. | Where appropriate, detailed guidance will be given in the mark scheme and must be adhered to. If no guidance is given, markers will need to examine each case to decide whether: <br> the incorrect answer is due to a transcription error; | If so, award the mark. |
| :---: | :---: | :---: |
|  | in questions not testing accuracy, the correct answer has been given but then rounded or truncated; | If so, award the mark. |
|  | the pupil has continued to give redundant extra working which does not contradict work already done; | If so, award the mark. |
|  | the pupil has continued, in the same part of the question, to give redundant extra working which does contradict work already done. | If so, do not award the mark. Where a question part carries more than one mark, only the final mark should be withheld. |
| The pupil's answer is correct but the wrong working is seen. | A correct response should always be marked as correct unless the mark scheme states otherwise. |  |
| The correct response has been crossed or rubbed out and not replaced. | Mark, according to the mark scheme, any legible crossed or rubbed out work that has not been replaced. |  |
| More than one answer is given. | If all answers given are correct or a range of answers is given, all of which are correct, the mark should be awarded unless prohibited by the mark scheme. If both correct and incorrect responses are given, no mark should be awarded. |  |
| The answer is correct but, in a later part of the question, the pupil has contradicted this response. | A mark given for one part should not be disallowed for working or answers given in a different part, unless the mark scheme specifically states otherwise. |  |

## Marking specific types of question

| Responses involving money <br> For example: $£ 3.20$ £7 |  |
| :---: | :---: |
| Accept $\downarrow$ | Do not accept $\times$ |
| $\checkmark$ Any unambiguous indication of the correct amount <br> eg $£ 3.20$ (p), $£ 320, £ 3,20$, <br> 3 pounds 20, f3-20, <br> £3 20 pence, $£ 3: 20$, <br> £7.00 <br> $\checkmark$ The $£$ sign is usually already printed in the answer space. Where the pupil writes an answer other than in the answer space, or crosses out the $f$ sign, accept an answer with correct units in pounds and/or pence <br> eg 320 p , <br> 700p | * Incorrect or ambiguous use of pounds or pence <br> eg $£ 320, £ 320$ p or $£ 700$ p, or 3.20 or 3.20 p not in the answer space. <br> x Incorrect placement of decimal points, spaces, etc or incorrect use or omission of 0 $\begin{aligned} \text { eg } & £ 3.2, £ 3 \text { 200, } £ 320, \\ & £ 3-2-0, \\ & £ 7.0 \end{aligned}$ |


| Responses involving time <br> A time interval For example: 2 hours 30 mins |  |
| :---: | :---: |
| Accept $\sqrt{ }$ | Take care ! Do not accept $\times$ |
| $\checkmark$ Any unambiguous indication eg 2.5 (hours), 2h 30 <br> $\checkmark$ Digital electronic time ie 2:30 | x Incorrect or ambiguous time interval <br> eg 2.3(h), 2.30, 2-30, 2h 3, <br> 2.30 min <br> ! The time unit, hours or minutes, is usually printed in the answer space. Where the pupil writes an answer other than in the answer space, or crosses out the given unit, accept an answer with correct units in hours or minutes, unless the question has asked for a specific unit to be used. |
| A specific time For example: 8.40am, 17:20 |  |
| Accept $\sqrt{ }$ | Do not accept $\times$ |
| $\checkmark$ Any unambiguous, correct indication eg $08.40,8.40,8: 40,0840,840$, 8 -40, twenty to nine, $8,40$ <br> $\checkmark$ Unambiguous change to 12 or 24 hour clock eg 17:20 as $5: 20 \mathrm{pm}, 17: 20 \mathrm{pm}$ | x Incorrect time <br> eg $8.4 \mathrm{am}, 8.40 \mathrm{pm}$ <br> x Incorrect placement of separators, spaces, etc or incorrect use or omission of 0 <br> eg 840, 8:4:0, 084, 84 |

## Responses involving coordinates

For example: $(5,7)$

| Accept $\checkmark$ | Do not accept $\times$ |
| :---: | :---: |
| ```\checkmark ~ U n a m b i g u o u s ~ b u t ~ u n c o n v e n t i o n a l ~ notation eg (05,07) ( five, seven ) (\begin{array}{l}{x}\\{5,}\end{array}>\mp@code{7}) (x=5, y=7)``` | x Incorrect or ambiguous notation <br> eg $(7,5)$ <br> (5x, 7y) <br> $(x 5, y 7)$ <br> $\left(5^{x}, 7^{y}\right)$ |

Responses involving the use of algebra
For example: $2+n \quad n+2 \quad 2 n$

| Accept $\checkmark$ | Take care ! Do not accept $\times$ |
| :---: | :---: |
| $\checkmark$ The unambiguous use of a different case <br> eg $N$ used for $n$ <br> $\checkmark$ Unconventional notation for multiplication <br> eg $n \times 2$ or $2 \times n$ or $n 2$ $\text { or } n+n \text { for } 2 n$ $n \times n \text { for } n^{2}$ <br> $\checkmark$ Multiplication by 1 or 0 <br> eg $\quad 2+1 n$ for $2+n$ $2+0 n \text { for } 2$ <br> $\checkmark$ Words used to precede or follow equations or expressions <br> eg $t=n+2$ tiles or $\text { tiles }=t=n+2$ $\text { for } t=n+2$ <br> $\checkmark$ Unambiguous letters used to indicate expressions $\text { eg } \quad t=n+2 \text { for } n+2$ <br> $\checkmark$ Embedded values given when solving equations <br> eg $3 \times 10+2=32$ $\text { for } 3 x+2=32$ | ! Words or units used within equations or expressions should be ignored if accompanied by an acceptable response, but should not be accepted on their own <br> eg do not accept $n \text { tiles }+2$ $n \mathrm{~cm}+2$ <br> $\times$ Change of variable <br> eg $x$ used for $n$ <br> x Ambiguous letters used to indicate expressions $\text { eg } n=n+2$ <br> However, to avoid penalising any of the three types of error above more than once within each question, do not award the mark for the first occurrence of each type within each question. Where a question part carries more than one mark, only the final mark should be withheld. <br> $\times$ Embedded values that are then contradicted $\begin{array}{ll} \text { eg } \quad \text { for } 3 x+2=32, \\ & 3 \times 10+2=32, x=5 \end{array}$ |

## Responses involving probability

A numerical probability should be expressed as a decimal, fraction or percentage only.

For example: 0.7

| Accept $\checkmark$ | Take care ! Do not accept $\times$ |
| :---: | :---: |
| $\checkmark$ A correct probability that is correctly expressed as a decimal, fraction or percentage. <br> $\checkmark$ Equivalent decimals, fractions or percentages $\text { eg } \quad 0.700, \frac{70}{100}, \frac{35}{50}, 70.0 \%$ <br> $\checkmark$ A probability correctly expressed in one acceptable form which is then incorrectly converted, but is still less than 1 and greater than 0 $\text { eg } \quad \frac{70}{100}=\frac{18}{25}$ | The following four categories of error should be ignored if accompanied by an acceptable response, but should not be accepted on their own. <br> ! A probability that is incorrectly expressed <br> eg 7 in 10, <br> 7 out of 10, <br> 7 from 10 <br> ! A probability expressed as a percentage without a percentage sign. <br> ! A fraction with other than integers in the numerator and/or denominator. <br> However, each of the three types of error above should not be penalised more than once within each question. Do not award the mark for the first occurrence of each type of error unaccompanied by an acceptable response. Where a question part carries more than one mark, only the final mark should be withheld. <br> ! A probability expressed as a ratio eg $7: 10,7: 3,7$ to 10 <br> * A probability greater than 1 or less than 0 |

## Recording marks awarded on the test paper

All questions, even those not attempted by the pupil, will be marked, with a 1 or a 0 entered in each marking space. Where 2 m can be split into 1 m gained and 1 m lost, with no explicit order, then this will be recorded by the marker as 1

The total marks awarded for a double page will be written in the box at the bottom of the right-hand page, and the total number of marks obtained on the paper will be recorded on the front of the test paper.

A total of 120 marks is available in tiers $3-5,4-6$ and $6-8$.
A total of 122 marks is available in tier 5-7.

## Awarding levels

The sum of the marks gained on paper 1, paper 2 and the mental mathematics paper determines the level awarded. Level threshold tables, which show the mark ranges for the award of different levels, will be available on the QCA website www.qca.org.uk from Monday, 23 June 2003. QCA will also send a copy to each school in July.

Schools will be notified of pupils' results by means of a marksheet, which will be returned to schools by the external marking agency with the pupils' marked scripts. The marksheet will include pupils' scores on the test papers and the levels awarded.

| Tier \& Question |  |  |  |  |  | Pictogram |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 5 | 5-7 6 | 6-8 |  |  |  |
| 1 |  |  |  |  | Correct response | Additional guidance |
| a |  |  |  | 1m | Draws two circles | $\checkmark$ Circles not shaded <br> ! Circles inaccurate in size and/or shape Accept provided the pupil's intention is clear |
| b |  |  |  | 1m | 2 |  |


| Tier \& Question |  |  |  |  | Missing numbers |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 5 | 5-7 6-8 |  |  |  |
| 2 |  |  |  | Correct response | Additional guidance |
|  |  |  | 1m <br> 1m <br> 1m <br> 1m | Gives any three numbers that add to 15 eg <br> - $5+6+4$ <br> - $5+5+5$ <br> Gives any two numbers that multiply to 15 eg <br> - $3 \times 5$ <br> - $1 \times 15$ <br> Gives any two numbers that divide to give 15 eg <br> - $30 \div 2$ <br> - $15 \div 1$ <br> Gives any three numbers that combine as shown to give 15 <br> eg <br> - $2 \times 6+3$ | $\checkmark$ Throughout the question, use of fractions, decimals, negatives or zeros <br> $\mathbf{x}$ Incorrect order <br> eg <br> - $2 \div 30$ <br> $\checkmark$ Brackets inserted to change order of operations <br> eg <br> - $3 \times(1+4)$ <br> $\times$ Incorrect order of operations <br> eg <br> - $3 \times 1+4$ |


| Tier \& Question |  |  |  |  |  | Scales |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 5 | 5-7 6 | 6-8 |  |  |  |
| 3 |  |  |  |  | Correct response | Additional guidance |
| a |  |  |  | 1m | 60 | $\checkmark$ Value between 59 and 61 inclusive <br> ! Units given Ignore |
| b |  |  |  | 1 m | Indicates the correct position | $\checkmark$ Unambiguous indication eg <br> ! Follow through <br> Accept follow through from part (a), provided their (a) is not 0,50 or 100 <br> ! Position not indicated accurately Accept within 2 mm |



| Tier \& Question |  |  |  |  | Clock |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 6-8 |  |  |  |
| 5 |  |  |  | Correct response | Additional guidance |
| a |  |  | 1 m | Indicates only the two correct clocks eg <br> $\checkmark$ $\qquad$ $\qquad$ <br> $\checkmark$ | ! Indication other than ticks eg <br> - $\boldsymbol{x}$ used <br> Accept provided unambiguous |
| b |  |  | 1m | 5:15 or 05:15 | $\checkmark$ Superfluous indication of morning eg <br> - 5:15 am <br> $\mathbf{x}$ Time incorrect <br> eg <br> - 5:15 pm <br> - 17:15 |
| c |  |  | 1m | 17:15 | ! Follow through <br> Accept follow through as 12 hours later than their (b), even if their (b) was 17:15, provided this is written as a possible time <br> eg, from part (b) as 03:26, accept <br> - 15:26 <br> $\checkmark$ Superfluous indication of evening eg <br> - 17:15 pm <br> $\times$ Time incorrect or not using 24 hour clock eg <br> - 17:15 am <br> - 5:15 pm |



| Tier \& Question |  |  |  |  |  |  | Chains |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 | 6-8 |  |  |  |  |
| 7 | 1 |  |  |  | Correct response |  |  |
| a | a |  |  | 1m | Gives both correct values correctly positioned, ie 20 and 320 |  |  |
| b | b |  |  | 1m | Gives both correct values correctly positioned, ie 5 and $2 \frac{1}{2}$ or equivalent | $\checkmark \text { For } 2 \frac{1}{2}, \frac{5}{2}$ |  |



| Tier \& Question |
| :--- |
| 3 |

Wind chill

| 3-5 | 4-6 | 5-7 | 6-8 |  |  | -ind chil |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 9 | 4 |  |  |  | Correct response | Additional guidance |
|  |  |  |  | 1m <br> 1m <br> 1m | $-19$ $16$ $-22$ | ! Incorrect notation for negative numbers eg - 19- <br> Penalise only the first occurrence <br> $x-16$ given for 16 |

\begin{tabular}{|c|c|c|c|c|c|}
\hline \multicolumn{3}{|l|}{Tier \& Question} \& \& \& \multirow[t]{2}{*}{Throwing dice} \\
\hline 3-5 \& 4-6 5 \& 5-7 6-8 \& \& \& \\
\hline 10 \& 5 \& \& \& Correct response \& Additional guidance \\
\hline a \& a \& \& \begin{tabular}{l}
\[
2 \mathrm{~m}
\] \\
or
1m
\end{tabular} \& \begin{tabular}{l}
Indicates only the five points with positive integer coordinates whose sum is 6 eg \\
Indicates at least four correct points with no incorrect points \\
or \\
Indicates all five correct points with not more than one incorrect point
\end{tabular} \& \begin{tabular}{l}
! Point(s) not indicated accurately Accept in parts (a) and (b) provided the pupil's intention is clear \\
! Additional points indicated that assume zero to be on the dice \\
eg \\
- \((0,6)\) and/or \((6,0)\) indicated \\
If this is the only error, mark as 1,0 \\
! Additional points with non-integer coordinates whose sum is 6 indicated eg \\
If this is the only error, mark as 1,0
\end{tabular} \\
\hline b \& b \& \& \(2 m\)

or

$1 m$ \& | Indicates only the six points with positive integer coordinates such that $y=x$ eg |
| :--- |
| Indicates at least five correct points with no incorrect points |
| or |
| Indicates all six correct points with not more than one incorrect point | \& | ! Additional point indicated that assumes zero to be on the dice eg |
| :--- |
| $(0,0)$ indicated |
| If this error has been penalised in part (a), condone |
| If this is the only error and it has not been penalised in part (a), mark as 1,0 |
| ! Additional points with non-integer coordinates such that $y=x$ indicated eg |
| If this error has been penalised in part (a), condone |
| If this is the only error and it has not been penalised in part (a), mark as 1,0 | <br>

\hline
\end{tabular}

| Tier \& Question |  |  | Throwing dice (cont) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 4 | 4-6 5 | 5-7 6-8 |  |  |  |
| 10 | 5 |  |  | Correct response | Additional guidance |
| c | c |  | 1m | Completes the sentence to give a correct rule eg <br> - One less than the number on the red dice <br> - Red - 1 <br> - Needing 1 added to get the number on the red dice | $\checkmark$ Minimally acceptable rule <br> eg <br> - 1 below the other dice <br> - The number below the red dice <br> $\checkmark$ Rule expressed algebraically <br> eg <br> - $b=r-1$ <br> - $r-1$ <br> $!$ Rule that does not use the given starting phrase <br> Accept only if unambiguous <br> eg, accept <br> - Red = blue + 1 <br> eg, do not accept <br> - 1 more on the red <br> $\times$ Ambiguous rule <br> eg <br> - -1 <br> - 1 below <br> - A number below the red dice <br> - The number lower than the red dice <br> - Followed by the number on the red dice <br> $\mathbf{x}$ Incomplete rule <br> eg <br> - Less than the number on the red dice <br> $\times$ Rule not generalised <br> Do not accept rules only shown through particular numerical examples <br> eg <br> - $2-1=1,3-2=1,4-3=1$ etc |






| Tier \& Question |  |  |  |  |  | Simplifying |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 | 6-8 |  |  |  |
| 14 | 9 | 3 |  |  | Correct response | Additional guidance |
|  |  |  |  | $1 \mathrm{~m}$ $1 \mathrm{~m}$ | $8 k+7$ $2 k+5$ | $\times$ Use of multiplication sign in simplified expressions eg, for the first mark <br> - $8 \times k+7$ <br> $\times$ Partially simplified expressions |



| Tier \& Question |  |  |  |  |  |  | Thinking fractions |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 5 | 5-7 6 | 6-8 |  |  |  |  |
| 16 | 11 | 4 |  |  |  | Correct response | Additional guidance |
|  |  |  |  | 1m | 40 |  |  |
|  |  |  |  | 1m | 150 |  |  |
|  |  |  |  | 1m | 30 |  |  |


| Tier \& Question |  |  |  | Marking overlay available |  | Moving C |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 | 6-8 |  |  |  |
| 17 | 12 | 5 |  |  | Correct response | Additional guidance |
| a | a | a |  | 1 m | Gives correct coordinates eg <br> - (6, any value except 6 or 1$)$ <br> - $(4,5)$ <br> - $(8,5)$ <br> - $(4,-3)$ <br> - $(8,-3)$ | ! Use of overlay <br> As there is an infinite number of correct coordinates, a marking overlay is available for use if pupils give non-integer coordinates. Accept coordinates of any point that lies exactly on the straight line or on one of the circles, provided their point is neither $(6,6)$ nor on the same straight line as A and B |
| b | b | b |  | 1 m | Gives correct coordinates, ie $(4,5)$ or $(8,5)$ or $(6,3)$ or $(4,-3)$ or $(8,-3)$ or $(6,-1)$ | $\checkmark$ Same correct position used for part (b) as for part (a) |


| Tier \& Question |  |  |  |  |  | Shoe sizes |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 | 6-8 |  |  |  |
| 18 | 13 | 6 |  |  | Correct response | Additional guidance |
| a | a | a |  | 1 m | 6 |  |
| b | b | b |  | $\begin{gathered} 1 \mathrm{~m} \\ \mathrm{U} 1 \end{gathered}$ | 2 |  |



| Tier \& Question |  |  |  |  |  | Travel to work |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 | 6-8 |  |  |  |
| 20 | 15 | 8 |  |  | Correct response | Additional guidance |
| a | a | a |  | $\begin{gathered} 2 \mathrm{~m} \\ \text { or } \\ 1 \mathrm{~m} \end{gathered}$ | £ 729(.00) <br> Shows the digits 729 <br> eg <br> - 72900 <br> - 72.90 <br> or <br> Shows a complete correct method with not more than one computational error, but with the decimal point correctly positioned eg <br> - $20 \times 45=900$ <br> $16 \times 45=8 \times 90=720$ <br> $720+9$ <br> - 1620 $\begin{aligned} & \frac{45}{64800} \\ & \frac{8100}{73900} \text { (error) } \quad \text { so } £ 739 \end{aligned}$ <br> (error) 1 <br> So $£ 719$ | $\times$ Conceptual error <br> eg $\begin{array}{r} 1620 \\ \begin{array}{r} 45 \\ 6480 \\ 8100 \\ \hline 14580 \end{array} \text { so } £ 145.80 \end{array}$ |
| b | b | b |  | 1 m | £ 14 |  |


| Tier \& Question |  |  |  |  |  | Solving |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 | 6-8 |  |  |  |
| 21 | 16 | 9 | 1 |  | Correct response | Additional guidance |
|  |  |  |  | 1m <br> 1m | 2 $2 \frac{1}{2}$ or equivalent | ! Throughout the question, incorrect notation eg, as an answer for the first mark $\text { - } k=\times 2$ <br> Withhold one mark only for the first occurrence |
|  |  |  |  | 2 m <br> or <br> 1m | $4 \frac{1}{2}$ or equivalent <br> Shows or implies a correct first step of algebraic manipulation that either reduces the number of terms or collects variables on one side of the equation and numbers on the other eg <br> - $2 t+4=13$ <br> - $3 t=t+9$ <br> - $3 t-t=13-4$ <br> - $2 t=9$ | ! Method used is trial and improvement Note that no partial credit can be given |
|  |  |  |  | 1 m | -1 |  |


| Tier \& Question |  |  |  | Shapes |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 5 |  | 6-8 |  |  |  |
|  | 171 | 10 | 2 |  | Correct response | Additional guidance |
|  |  |  |  | 3 m <br> or 2m <br> or <br> 1m | All four angles correct and correctly positioned, ie <br> At least three angles correct and correctly positioned <br> or <br> All four correct angles shown but identification of which angle is which size is not clear <br> At least two angles correct and correctly positioned | $\checkmark$ Units omitted <br> ! Units incorrect <br> eg <br> - $50 \%$ <br> Withhold one mark only for the first occurrence <br> $\checkmark$ Follow through <br> For 2 m or 1 m , follow through for $47^{\circ}$ as 360 - sum of their other three angles or 97 - their 50 |


| Tier \& Question |  |  |  |  |  | Mixed numbers |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 | 6-8 |  |  |  |
|  | 18 | 11 | 3 |  | Correct response | Additional guidance |
|  | a | a | a | $\begin{gathered} 1 \mathrm{~m} \\ \\ 1 \mathrm{~m} \end{gathered}$ | Gives the value $1 \frac{4}{5}$ or $\frac{9}{5}$ or equivalent fraction or decimal <br> Indicates the correct position on the number line, ie | ! Indication inaccurate <br> Accept provided the pupil's intention is clear <br> ! Follow through <br> Accept provided their incorrect value for the addition is between 0 and 2 , but is not an integer <br> eg, from $\frac{12}{15}$ for the first mark, accept |
|  | b | b | b | 1 m | 20 | $\checkmark$ Answer given as a fraction eg <br> - $\frac{60}{3}$ <br> $\checkmark$ Answer repeats sixths eg <br> - $\frac{20}{6}$ |


| Tier \& Question |  |  |  |  |  | Mixed numbers (cont) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 | 6-8 |  |  |  |
|  | 18 | 11 | 3 |  | Correct response | Additional guidance |
|  | c | c | c | $2 \mathrm{~m}$ <br> or 1m | Shows a complete correct method with not more than one computational error eg <br> - $20 \div 5$ <br> - $\frac{10}{3} \times \frac{6}{5}=\frac{60}{15}=3$ (error) <br> - $3 \frac{1}{3}=\frac{7}{3}$ (error), $\frac{7}{3} \times \frac{6}{5}=\frac{42}{15}$ | $\checkmark$ Answer given as a fraction eg <br> - $\frac{4}{1}$ <br> - $\frac{60}{15}$ <br> ! Follow through <br> For 2 m or 1 m , accept their (b) $\div 5$ provided their (b) is a positive integer <br> x Conceptual error <br> eg <br> - $20 \div 5=\frac{4}{6}$ <br> - $\frac{20}{6} \div \frac{5}{6}=\frac{4}{6}$ <br> - $\frac{10}{3} \times \frac{6}{5}=\frac{16}{15}$ <br> - $\frac{1}{10} \times \frac{6}{5}=\frac{6}{50}$ <br> - $3 \frac{1}{3} \times \frac{6}{5}=3 \frac{6}{15}$ |


| Tier \& Question |  |  |  |  |  | Areas algebraically |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 | 6-8 |  |  |  |
|  | 19 | 12 | 4 |  | Correct response | Additional guidance |
|  | a | a | a | 1 m <br> 1m | Gives a correct simplified expression for the area eg <br> - $15 a b$ <br> - $15 \times a \times b$ <br> Gives a correct simplified expression for the perimeter <br> eg <br> - $6 a+10 b$ <br> - $2(3 a+5 b)$ <br> - $6 \times a+10 \times b$ <br> - $2 \times(3 a+5 b)$ | ! Partially simplified or unsimplified expressions <br> eg, for the area <br> - $3 a 5 b$ <br> eg, for the perimeter <br> - $2(3 a)+2(5 b)$ <br> - $2 \times(3 \times a+5 \times b)$ <br> If both expressions are correct but are partially simplified or unsimplified, mark as 0,1 , provided neither has subsequently been incorrectly simplified <br> ! Expressions transposed but otherwise correct and simplified Mark as 0,1 |
|  | b | b | b | 1 m | Gives both correct dimensions in either order, ie $4 a$ and $3 a$ | ! Correct dimensions embedded <br> Accept provided both the area and perimeter have been considered <br> eg, accept $\begin{aligned} -12 a^{2}=3 a \times 4 a \\ 14 a=2(3 a+4 a) \end{aligned}$ <br> ! Dimensions labelled as length or width Ignore |


| Tier \& Question |  |  |  |  |  | Arranging |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 | 6-8 |  |  |  |
|  | 20 | 13 | 5 |  | Correct response | Additional guidance |
|  | a | a | a | 1m <br> U1 | Gives a correct arrangement using each of the numbers 1 to 6 once only, ie for each 3 digit number: <br> eg <br> - $543+621$ <br> - $641+523$ <br> Gives a correct arrangement using each of the numbers 1 to 6 once only, ie for each 3 digit number: <br> eg <br> - $514+236$ <br> - $216+534$ |  |
|  | b | b | b |  | $536-421 \text { or } 356-241$ | $\times$ Incorrect order of subtraction eg <br> - 421 - 536 |


| Tier \& Question |  |  |  |  |  | Lines on a square |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 |  | 6-8 |  |  |  |
|  | 21 | 14 | 6 |  | Correct response | Additional guidance |
|  |  | a | a | 2 m <br> or 1m | Matches all three equations correctly, ie <br> Matches any two equations correctly | $\times$ Any equation matched more than once |
|  |  | b | b | 1 m | Gives a correct equation eg $x=1$ |  |



| Tier | \& Q | Quest |  | Scatter graphs |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 | 6-8 |  |  |  |
|  | 22 | 15 | 7 |  | Correct response | Additional guidance |
|  | a | a | a | 1m | Indicates a positive correlation eg <br> - There is positive correlation between diameter and height <br> - As diameter increases, height increases <br> - Higher trees have wider trunks <br> - Bigger trees are fatter <br> - They both increase together | $\checkmark$ Minimally acceptable response eg <br> - Big trees have big diameters <br> $\times$ Incomplete response <br> eg <br> - It's positive <br> - Big trees have big heights <br> - Higher trees are bigger <br> $\times$ Incorrect reference to proportion eg <br> - It's directly proportional |
|  | b | b | b | 1 m | Gives a correct explanation <br> The most common correct explanations: <br> Refer to the trend in the data <br> eg <br> - It would be too far away from the other points <br> - It would be an outlier <br> - It doesn't fit the general trend <br> - It would be a long way from the line of best fit <br> - This diameter is far too big for the height <br> - It is too small to have such a big diameter <br> Give a value for the height or diameter if the tree were a poplar <br> eg <br> - If it was a poplar you would expect it to be about 6 metres high <br> - Poplars that are 3 m high are only about 2 cm in diameter | $\checkmark$ Minimally acceptable explanation eg <br> - It's on its own on the graph <br> - It doesn't fit the correlation <br> - It doesn't fit the pattern <br> - It doesn't have the same relationship <br> - The diameter in cm is bigger than the height in m <br> - The diameter is big but the height is small <br> $\times$ Incomplete or incorrect explanation <br> eg <br> - It's different from the others <br> - It's on its own <br> - It doesn't fit the graph <br> - Poplar trees are tall and thin <br> - It would not be on the line of best fit <br> - It's not in the same range <br> - The diameter is too big <br> - Poplar trees don't have diameters bigger than their height <br> - For poplars, diameter $+1=$ height <br> ! Height for diameter of 5 cm given Accept values in the range 5.5 m to 7 m inclusive <br> ! Diameter for height of $3 m$ given Accept values in the range 1 cm to 2.3 cm inclusive |
|  | c | c | c | 1m | Indicates a value between 4 and 5.2 inclusive |  |
|  |  | d | d | $\begin{array}{\|c} 2 \mathrm{~m} \\ \\ \text { or } \\ 1 \mathrm{~m} \end{array}$ | Indicates that all four statements are false <br> Makes three correct decisions | ! Indication other than ticks Accept only if unambiguous |


| Tier \& Question |  |  |  |  | Winning ticket |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 5-7 | 6-8 |  |  |  |
|  | 16 | 8 |  | Correct response | Additional guidance |
|  | a | a | 1 m | Gives a correct probability eg <br> - $\frac{75}{245}$ <br> - $\frac{15}{49}$ <br> - 0.306(...) <br> - $31 \%$ | ! Answer of 0.3(0) or 30\% Accept provided a correct method or a more accurate value is seen <br> $\times$ Incorrect method <br> eg <br> - 3 colours so $\frac{1}{3}=0.3$ |
|  | b | b | 1 m | Gives a correct probability eg <br> - $\frac{3}{245}$ | ! Follow through <br> Accept follow through from an incorrect total number of tickets seen in part (a), provided their total is not 3 or 100 <br> eg, from $\frac{75}{255}$ for part (a), accept <br> - $\frac{3}{255}$ <br> ! Decimal or percentage value Accept 0.01 or $0.012(\ldots)$, or the equivalent percentages, provided no incorrect method is seen |
|  | c | c | 1m | $\frac{1}{3}$ or equivalent probability | ! Decimal or percentage value Accept 0.33 or better, or the equivalent percentages |



| Tier \& Question |  |  |  |  |  | Journeys (cont) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 5-7 | 5-7 6- |  |  |  |  |
|  |  | 17 | 9 |  | Correct response | Additional guidance |
|  |  | c | c | $2 \mathrm{~m}$ <br> or <br> 1m | Indicates 40 miles per hour or $\frac{2}{3}$ mile per minute <br> Shows or implies a complete correct method for calculating the speed in miles per hour or miles per minute eg <br> - $20 \div 30 \times 60$ <br> - $20 \times 2$ <br> - $20 \div 30$ <br> or <br> Indicates a correct speed in miles per minute, rounded or truncated to one decimal place eg <br> - 0.6 miles per minute <br> - 0.7 miles per minute | Note to markers: <br> Apply the additional guidance from parts (a) and (b) to part (c) <br> ! Answer given in miles per minute and rounded or truncated <br> In this context, accept rounding or truncation to two or more decimal places. For 2 m , do not accept an answer of 0.6 or 0.7 unless a correct method or a more accurate value is seen <br> $\mathbf{x}$ For $1 m$, method leading to rate of travel as time per distance <br> eg <br> - $30 \div 20$ <br> $\times$ For 1m, incomplete method <br> eg <br> - 20 miles in 30 minutes, so <br> 2 miles per 3 minutes |


| Tier \& Question |  |  | ( Different ways |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 5-7 | 6-8 |  |  |  |
|  | 18 | 10 |  | Correct response | Additional guidance |
|  | a | a | 3 m <br> or <br> 2m <br> or <br> 1m | Indicates correct decisions for all six statements, ie <br> Indicates correct decisions for five statements <br> Indicates the correct decision for at least one of the false statements, and makes at least three other correct decisions eg | $\checkmark$ Unambiguous indication eg <br> - $\boldsymbol{J}$ for True and $\mathbf{x}$ for False |
|  | b | b | $1 \mathrm{~m}$ | Gives a correct explanation <br> The most common correct explanations: <br> Refer explicitly or implicitly to the more efficient method of algebraic manipulation suggested by part (a) <br> eg <br> - You can solve the equation quickly by doing the same thing to both sides of the equation <br> - Because $2 x=3, x=1 \frac{1}{2}$ <br> Refer to the time taken or the number of trials needed <br> eg <br> - Takes a long time <br> - You need to try lots of values <br> - It is inefficient <br> Refer to the difficulty of finding an exact answer <br> eg <br> - If there are lots of decimal places it might be hard to be exact | $\checkmark$ Minimally acceptable explanation <br> eg <br> - Using algebra is better <br> - Decimal answers can be hard to find <br> - It can be inaccurate <br> ! Incomplete explanation <br> eg <br> - There is a better method <br> - The answer is always one value <br> - Easy to make a mistake <br> - It is inaccurate <br> - It's like guess work <br> - You could go on forever <br> Do not accept unless alongside a correct explanation |


| Tier \& Question |  |  |  | Marking overlay available |  | Locus of points |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 5 | 5-7 | 6-8 |  |  |  |
|  |  | 19 | 11 |  | Correct response | Additional guidance |
|  |  | a | a | 1 m | Indicates the two points of intersection of the circles with radius 4 cm , within the tolerance as shown on the overlay | ! More than two points indicated Ignore additional points that are equidistant from $A$ and $B$, as these may be working for part (b). Ignore other additional points provided it is clear which two points are the pupil's answer for part (a) |
|  |  | b | b | 1 m | Draws a straight line that fulfils the following three conditions below: <br> 1. Ruled <br> 2. Within the tolerance as shown on the overlay <br> 3. Extended to at least both the 6 cm circles as shown on the overlay | $\times$ Shading, or additional lines or curves marked <br> $\times$ Line indicated by a series of points or shown dashed or dotted |



| Tier \& Question |  |  | Straight line |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 6-8 |  |  |  |
|  |  | 13 |  | Correct response | Additional guidance |
|  |  | a | 1m | Gives a correct explanation <br> eg <br> - Right-angled triangle drawn on graph, with correct dimensions which are then used for height $\div$ base <br> - $\frac{\text { Change in } y}{\text { Change in } x}=\frac{5}{10}$ <br> - 6 right, 3 up, so $3 \div 6$ <br> - Half a square up for every one square along <br> - $(10,6)$ is on the line, so $6=10 m+1$ $\begin{aligned} 10 m & =5 \\ m & =0.5 \end{aligned}$ | $\checkmark$ Correct description of method eg <br> - You draw a right-angled triangle on the line, then you divide height by base <br> $\checkmark$ Minimally acceptable explanation <br> eg <br> - Right-angled triangle drawn on graph, with correct dimensions labelled <br> - $\frac{y}{x}=\frac{5}{10}$ <br> - 6 right, 3 up <br> - Half a square up each time <br> ! Units given <br> Ignore <br> $\times$ Incomplete explanation <br> eg <br> - $\frac{5}{10}$ <br> - It's 1 on the $y$-axis, -2 on the $x$-axis, and $1 \div 2=0.5$ |
|  |  | b | $2 \mathrm{~m}$ <br> or 1m | Gives a correct equation <br> eg <br> $y=\frac{1}{2} x+1$ <br> - $y=0.5 x+1$ <br> - $2 y-x=2$ <br> $\frac{1}{2} x$, or equivalent, seen <br> eg <br> - $\frac{1}{2} x+1$ <br> or <br> Shows understanding that the equation is of the form $y=m x+c$ and that $m=\frac{1}{2}$ and $c=1$, even if there are subsequent errors eg $\begin{aligned} & y=m x+c \\ & y=0.5+1 \text { (error) } \end{aligned}$ |  |
|  |  | c | 1m | Gives any equation equivalent to $y=\frac{1}{2} x+c$, where $c$ is any value other than 1 eg <br> - $y=\frac{1}{2} x-7$ <br> - $y=0.5 x+5$ <br> - $2 y=x$ | ! Follow through from part (b) Accept an equation of a line parallel to their (b), provided the equations contain both the variables $x$ and $y$ eg, from $y=2 x+1$ for part (b), accept - $y=2 x+4$ |


| Tier \& Question |  |  |  |  | Theme park |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 5 | 5-7 6-8 |  |  |  |
|  |  | 14 |  | Correct response | Additional guidance |
|  |  | a | 1 m | Gives a value between 27.5 and 28.5 inclusive |  |
|  |  | b | $2 \mathrm{~m}$ <br> or 1m | Gives a value between 16 and 18 inclusive <br> Identifies both the upper quartile age as a value between 37.5 and 38.5 inclusive and the lower quartile age as a value between 20.5 and 21.5 inclusive <br> or <br> On the graph, indicates on the $x$-axis two correct points corresponding to one value between 37.5 and 38.5 inclusive, and one value between 20.5 and 21.5 inclusive, even if the values are not stated or are stated incorrectly | ! More than two points indicated on the $x$-axis Ignore a point intended to correspond to the median. Otherwise do not accept |
|  |  | c | 1m | Gives a correct statement of comparison, interpreting the data <br> eg <br> - On average, younger people went to the theme park <br> - There was not as much variation of age at the theme park <br> - Older people tended to go to the flower show <br> - More people from different age groups went to the flower show | $\checkmark$ Follow through from incorrect values for parts (a) or (b) <br> $\checkmark$ Minimally acceptable statement <br> eg <br> - The average age was higher at the flower show <br> - Younger people went to the theme park <br> - The theme park had people closer to each other in age <br> ! Comparison with the theme park is implicit Given the wording of the question, condone eg, accept <br> - Older people tended to go <br> $\times$ No interpretation of the median or IQR within the context given <br> eg <br> - The median age in the theme park is lower <br> - The range was higher at the flower show <br> $\mathbf{x}$ Incorrect statement <br> eg <br> - People at the theme park were between 20 and 40 but people at the flower show were between 30 and 60 <br> - Young people went to the theme park but did not go to the flower show |



| Tier \& Question |  |  | ( Inequality (cont) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 6-8 |  |  |  |
|  |  | 15 |  | Correct response | Additional guidance |
|  |  | b | $1 \mathrm{~m}$ <br> (U1) | Gives a correct explanation <br> The most common correct explanations: <br> Give the correct solution <br> eg <br> - $-3<y<3$ <br> - It's only true if $y$ is between -3 and 3 <br> - $y$ must be bigger than -3 as well <br> Give a counter-example <br> eg <br> - -4 is less than 3 but $16>9$ <br> - If you square minus 8 the answer isn't less than 9 | $\checkmark$ Minimally acceptable explanation <br> eg <br> - Numbers less than -3 don't work <br> - $(-5)^{2}>9$ <br> - $-4 \times-4=16$ <br> - It's not true for -7 <br> $\times$ Incomplete explanation <br> eg <br> - When you square a negative number, the answer is positive <br> - $\sqrt{ } 9=3$ |



| Tier \& Question$\begin{array}{\|l\|l\|l\|l} \hline 3-5 & 4-6 & 5-7 & 6-8 \\ \hline \end{array}$ |  |  | Computer game |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
|  |  | 17 |  | Correct response | Additional guidance |
|  |  | a | 1 m | Indicates W, L, L | $\checkmark$ Unambiguous indication eg $\cdot 1,0,0$ |
|  |  | b | 1m | 45 | ! Qualifier used <br> eg <br> - About 45 <br> Accept, even though the exact value can be determined from the information given |
|  |  | c | 1m | 0.6 ( 0.02) or equivalent probability | $\checkmark$ Qualifier used eg <br> - About 60\% |
|  |  | d | 1m | Joins $(100,0.6)$ to $(120,0.5)$ using a curve with negative but increasing gradient, or by marking and joining any number of individual points on such a curve eg | ! Point (120, 0.5) not accurately marked Accept if on line $x=120$ and within 1 mm of correct height <br> ! Part(s) of curve with incorrect gradient Condone use of a straight line, ruled or unruled, ie <br> However do not accept other incorrect gradients eg <br> (decreasing gradient) <br> (gradient stops increasing) <br> (gradient positive in parts) |

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## NATIONAL

CURRICULUM
5-16

## GCSE

## GNVQ

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