# JUNIOR LYCEUM ANNUAL EXAMINATIONS 2006 

Educational Assessment Unit - Education Division
FORM 3
MATHEMATICS (Non-Calculator)
TIME: 10 minutes
Name $\qquad$ Class $\qquad$

Mark

- ANSWER ALL QUESTIONS.
- EACH QUESTION CARRIES 1 MARK.
- CALCULATORS, RULERS, PROTRACTORS AND OTHER MATHEMATICAL INSTRUMENTS ARE NOT ALLOWED.
- WRITE DOWN YOUR ANSWER ONLY IN THE SPACE PROVIDED.


# DO NOT WRITE IN <br> THIS SPACE 

|  | QUESTION | Space for working if required |
| :---: | :---: | :---: |
| 1. | Work out $\sqrt{\frac{9}{25}}$. <br> Ans: $\qquad$ |  |
| 2. | $1 \frac{1}{4}$ litres of milk are mixed with 10 litres of coffee. <br> What fraction of the mixture is milk? <br> Ans: |  |
| 3. | Simplify: $27 b^{5} \div 9 b$. Ans: |  |
| 4. | If $314 \times 28=8792$, find $3.14 \times 2.8$. <br> Ans: |  |
| 5. | What is the reciprocal of $1 \frac{3}{4}$ ? <br> Ans: $\qquad$ |  |
| 6. | Elaine is 3 years younger than Eric. If Eric is $x$ years old, how old will Elaine be next year? <br> Ans: |  |
| 7. | A man has a bundle of Lm5 notes numbered consecutively from 232426 to 232440 . What is their total value? <br> Ans: |  |
| 8. | Put the following numbers in ascending order of magnitude: $4^{0}, 4^{2}, 4^{\frac{1}{2}}, 4^{-1}$ <br> Ans: $\qquad$ |  |
| 9. | Complete the following: <br> The exterior angle of a triangle is equal to the $\qquad$ of the two interior $\qquad$ angles. <br> Ans: $\qquad$ |  |
| 10. | Expand: $3(2 x-3 y)$. Ans: |  |



DO NOT WRITE ABOVE THIS LINE

Name $\qquad$ Class $\qquad$
CALCULATORS ARE ALLOWED BUT ALL NECESSARY WORKING MUST BE SHOWN

Answer All Questions.

1. From the numbers $18,19,20,23,25,27$, write down:
a) a prime number $\qquad$
b) a square number
c) a number which is a multiple of 3 $\qquad$
d) two numbers whose sum is $\mathbf{4 4}$ $\qquad$ .
2. The marks of 12 students in a test were $5,5,6,6,6,7,8,8,10,10,14,17$.

For these marks find:
a) the mode $\qquad$
b) the median $\qquad$
c) the mean $\qquad$
d) the range $\qquad$ .
3. Given that $a x+b y=c$,
a) Make $y$ subject of the equation.

## Answer:

$\qquad$
b) Work out the value of $y$ when $a=1, b=2, c=5$ and $x=-3$.

Answer: $\qquad$
4. The price of a camera is increased by $30 \%$. Later in a sale, the price is reduced by $\mathbf{2 0 \%}$ of its new value. This final price is Lm78. What was the original price?

Answer: $\qquad$
5. Find the size of the angles marked $p, q, r$ and $s$ in this diagram.

Answer:
$p=$ $\qquad$
$q=$ $\qquad$
$r=$ $\qquad$
$s=$ $\qquad$
6. a) Express 1080 in prime factors.

Answer: $\qquad$
b) Given that $1080=2^{a} \times 3^{b} \times 5^{c}$, state the values of $a, b, c$.

Answer: $\mathbf{a}=$ $\qquad$ $b=$ $\qquad$ $c=$ $\qquad$
c) What is the smallest whole number by which 1080 must be multiplied to make a perfect square?

Answer: $\qquad$
7. a) This sketch shows the side of a shed.
i) Find its area.


Answer: $\qquad$
ii) Find the volume of the shed, if it is 4 m long.

Answer:
b) A map has a scale of 2 cm to represent 1 km . Two villages are 8.4 cm apart on the map. What is the actual distance between them?

Answer: $\qquad$
8. a) When a kite is flying, the string makes an angle of $22^{\circ}$ with the horizontal and the string is 200 m long. How high is the kite?
(Give your answer correct to 3 sig. figures.)


Answer: $\qquad$
b) The histogram shows the distances from home to school of a group of children. What is the probability that a child chosen at random from this group lives within 1 km of the school?
(Give your answer as a fraction.)


Answer: $\qquad$
c) A cylindrical candle has diameter 6 cm and height 15 cm . Calculate its volume in $\mathrm{cm}^{3}$. (Give your answer correct to the nearest whole number of cubic centimetres.)

Answer: $\qquad$
9. The diagram shows two lines marked (1) and (2).
a) State whether the following statements are TRUE or FALSE.
i) The gradient of line 1 is positive.
ii) The gradient of line 1 is greater than that of line 2. $\qquad$
iii) Line 1 passes through the point $(2,5)$. $\qquad$

iv) Points $(2,1)$ and $(5,4)$ lie on line 2. $\qquad$
b) Calculate the gradient of line 2.

Answer: $\qquad$
10.a) Solve the equations:
i) $2 d+7=31-4 d$
ii) $3(2 x-5)-4(x+7)=13$

Answer: (i) $\qquad$ (ii) $\qquad$
b) Calculate the simple interest on Lm250 invested for $\mathbf{3}$ years at $\mathbf{8 \%}$ per annum.

Answer: $\qquad$
11.a) The mass of the Earth is $5.974 \times 10^{21}$ tonnes. The moon's mass is 0.0123 of the Earth's mass. Work out the Moon's mass in tonnes, giving your answer in standard form correct to 3 significant figures.

Answer: $\qquad$
b) One morning an explorer sets out from his base camp $C$. He walks 8 km due West and then 5 km due North to arrive at $A$.
In the afternoon he returns to the camp along the path AC.


Calculate correct to the nearest km:
(i) the distance AC

Answer: $\qquad$
(ii) the total distance covered.

Answer: $\qquad$
c) Solve the simultaneous equations:

$$
2 x+y=5, \quad 4 x-y=7
$$

Answer: $\qquad$
12. Find the marked angles in the diagrams below. Give reasons for your answers. ( $O$ is the centre of the circle.)
(a)

(b)


Answer: (a) $e=$ $\qquad$
$f=$ $\qquad$
(b) $j=$ $\qquad$
$k=$ $\qquad$
13. On the graph paper provided, draw axes with the values for both $x$ and $y$ from - 8 to 8 . Use $1 \mathbf{c m}$ to represent 1 unit on both axes.
(a) Draw the triangle $A B C$ where $A$ is $(1,1), B$ is $(4,2)$ and $C$ is $(3,7)$.
(b) Draw the reflection of $\triangle A B C$ in the $y$-axis.

Label the image of $\triangle A B C$ as $\Delta A_{1} B_{1} C_{1}$.
What are the co-ordinates of the points $A_{1}, B_{1}, C_{1}$ ?
Answer: $\mathrm{A}_{1}=$ $\qquad$ , $B_{1}=$ $\qquad$ , $\mathrm{C}_{1}=$ $\qquad$ .
(c) Rotate $\Delta A_{1} B_{1} C_{1}$ about the origin through $180^{\circ}$.

Label the image of $\Delta A_{1} B_{1} C_{1}$ as $\Delta A_{2} B_{2} C_{2}$.
What are the co-ordinates of the points $A_{2}, B_{2}, C_{2}$ ?
Answer: $\mathrm{A}_{\mathbf{2}}=$ $\qquad$ , $\mathrm{B}_{2}=$ $\qquad$ , $\mathrm{C}_{2}=$ $\qquad$ .
(d) What single transformation would map $\Delta A B C$ into $\Delta A_{2} B_{2} C_{2}$ ?

Answer: $\qquad$
14. a) Complete the following table for $y=x^{2}-4 x+3$.

| $x$ | -2 | -1 | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $x^{2}$ |  | 1 | 0 | 1 | 4 | 9 | 16 | 25 |
| $-4 x$ | 8 | 4 | 0 | -4 |  | -12 | -16 | -20 |
| +3 | +3 | +3 | +3 | +3 | +3 | +3 | +3 | +3 |
| $y$ | 15 |  | 3 | 0 | -1 |  | 3 | 8 |

b) Draw the graph of $y=x^{2}-4 x+3$ for values of $x$ from -2 to 5 .

Take 2 cm as 1 unit on the $x$-axis and 1 cm as 1 unit on the $y$-axis.
c) What is the minimum value of $y$ ? Give the corresponding value of $x$.

Answer: $y=$ $\qquad$
$\qquad$
$x=$
d) Use your graph to solve the equation $x^{2}-4 x+3=0$.

Answer: $\qquad$
15. Complete the table below for regular polygons.

| Number of <br> sides | Name | Sum of <br> exterior <br> angles | Size of an <br> exterior <br> angle | Sum of <br> interior <br> angles | Size of an <br> interior <br> angle |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3 | equilateral <br> triangle | $360^{\circ}$ | $120^{\circ}$ | $180^{\circ}$ | $60^{\circ}$ |
| 4 |  |  | $90^{\circ}$ | $360^{\circ}$ | $90^{\circ}$ |
|  |  |  |  | $540^{\circ}$ | $108^{\circ}$ |


|  | pentagon |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 6 | regular <br> hexagon |  | $60^{\circ}$ |  | $120^{\circ}$ |
|  | regular <br> octagon |  | $45^{\circ}$ | $1080^{\circ}$ |  |

## End of paper

