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## STATE EXAMINATIONS COMMISSION MARKING SCHEME

## **LEAVING CERTIFICATE EXAMINATION 2004**

## MATHEMATICS

## FOUNDATION LEVEL

## PAPER 1

#### **GENERAL GUIDELINES FOR EXAMINERS - PAPER 1**

- 1. Penalties of three types are applied to candidates' work as follows:
  - Blunders mahematical errors/omissions (-3)
  - Slips numerical errors
  - Misreadings (provided task is not oversimplified) (-1).

Frequently occurring errors to which these penalties must be applied are listed in the scheme. They are labelled as B1, B2, B3,...., S1, S2, S3,..., M1, M2, etc. Note that these lists are not exhaustive.

(-1)

- 2. When awarding attempt marks, e.g. Att(3), note that
  - any correct relevant step in a part of a question merits at least the attempt mark for that part
  - if deductions result in a mark which is lower than the attempt mark, then the attempt mark must be awarded
  - a mark between zero and the attempt mark is never awarded.
- 3. Worthless work is awarded zero marks. Some examples of such work are listed in the scheme and they are labelled as W1, W2,....etc.
- 4. The phrase "hit or miss" means that partial marks are not awarded the candidate receives all of the relevant marks or none.
- 5. The *same* error in the *same* section of a question is penalised *once* only.
- 6. Special notes relating to the marking of a particular part of a question are indicated by an asterisk. These notes immediately follow the box containing the relevant solution.
- 7. Particular cases, verifications and answers derived from diagrams (unless requested) qualify for attempt marks at most.
- 8. A serious blunder, omission or misreading merits the ATTEMPT mark at most.
- 9. The phrase "and stops" means that no more work is shown by the candidate.
- 10. Accept the best of two or more attempts even when attempts have been cancelled.
- 11. Allow comma for decimal point, e.g.  $\in 5.50$  may be written as  $\notin 5,50$ .

# Each part10 marksAtt 4

#### Part (i)

# 10 marks

Att 4

(i) Find  $\sqrt{55}$ , correct to two decimal places.

## $\sqrt{55}$ = 7.416 = **7.42**

Blunders (-3)

- B1: Square root mistaken for square (Ans. 3025)
- B2: Square root mistaken for half (Ans. 27.5)
- B3: Incorrect or omitted round-off

Slips (-1) S1: If  $55\sqrt{55} = 408.1$ S2: Misplacing decimal point e.g. 74.2 or 0.742

Misreadings (-1) M1:  $\sqrt{5.5} = 2.345$ M2:  $\sqrt{0.55} = 0.741$ 

Attempts Att: Writes 55<sup>2</sup> and stops Att: Writes 55/2 and stops Att: Work at estimating answer e.g.  $\sqrt{64} = 8$  or  $\sqrt{49} = 7$  (ii) Find the exact value of  $(17.5)^2 - (2.5)^2$ .

$$(17.5)^2 - (2.5)^2 = 306.25 - 6.25 = 300$$

or

$$(17.5)^2 - (2.5)^2 = (17.5 + 2.5)(17.5 - 2.5) = (20)(15) = 300$$

#### Blunders (-3)

- B1: Square mistaken for square root (Ans. 4.1833 1.5811 = 2.6022)
- B2: Square mistaken for twice (Ans. 35 5 = 30)
- B3: Blunder in precedence e.g. 15<sup>2</sup>
- B4: Square not found, each time
- B5:  $17.5 \times 10^2 2.5 \times 10^2 = 1500$

#### Slips (-1)

- S1: Early round-off or truncation, each time
- S2: Misplacing the decimal point, each time
- S3: Subtraction omitted

Misreadings (-1)

M1: Misplaced digits or misread numbers, each time

*Attempts* Att: Work at estimating answer e.g. 400 (iii) Find  $(4.08)^3$ , correct to three decimal places.

$$(4.08)^3 = 67.917312 = 67.917.$$

Blunders (-3) B1: Calculates (4.08)3; (Ans. 12.24) B2: Third root calculated instead of power of 3; (Ans. 1.5979) B3: Interprets  $(4.08)^3$  as  $4.08 \times 10^3$ ; (Ans. 4080) B4: Calculates  $(4.08)^2$ ; (Ans. 16.6464) B5: Incorrect or omitted round off

B5: Incorrect or omitted round-off

*Slips (-1)* S1: Misplacing decimal point

*Misreadings (-1)* M1: Power other than 3 or 2 worked

Attempts

- Att: Writes (4.08)3 and stops
- Att: Writes  $4.08 \times 10^3$  and stops
- Att: Work at estimating answer e.g. 64

(iv) Find the exact value of  $61.09 + \frac{3.24}{0.08}$ .

$$61.09 + \frac{3.24}{0.08} = 61.09 + 40.5 = 101.59$$

Blunders (-3) B1: Blunder in precedence e.g. (61.09 + 3.24)/0.08 = 804.125B2: Blunder in calculating fraction e.g. 0.08/3.24 = 0.0246 or  $3.24 \pm 0.08$ 

Slips (-1) S1: Misplacing decimal point, e.g. 6.109, each time S2: Slip in addition or addition omitted

*Misreadings (-1)* M2: Reads × for + (Ans. 2474.145)

*Attempts* Att: Work towards a correct step

Note:  $(61.09 \div 0.08) + 3.24 = 763.5 + 3.24 = 766.74$  $61.09 + (0.08 \div 3.24) = 61.1146$ (61.09 + 3.24) + 0.08 = 64.41(61.09 + 3.24) - 0.08 = 64.25 (v) Find 21% of  $\in$ 43.27, correct to the nearest cent.

€43.27 × 0.21 = €9.0867 = **€9.09** 

*Blunders (-3)* Any blunder in calculating the percentage results in 4 marks at most.

- B1: Calculates 121% (Ans. €52.3567)
- B2: Calculates 79% (Ans. €34.18)
- B3: Calculates 1% of €43.27
- B4: Incorrect or omitted round-off

*Slips (-1)* S1: Numerical slips in calculation

Attempts Att: Writes 21/100 without working Att: 43.27/21 or 21/43.27 and stops (vi) A book costs £18 sterling. Find its cost in euro if  $\notin 1 = \pm 0.72$  sterling.

$$\frac{\pounds 18.00}{\pounds 0.72} = \pounds 25.$$

*Blunders (-3)* B1: Calculates 18 × 0.72 (Ans. 12.96)

*Slips (-1)* S1: Misplacing decimal point

Attempts Att: Calculates 1/0.72 = 1.38888Att: Calculates 1/18 = 0.0555 Part (vii)

Att 4

(vii) Write  $\frac{6}{11} - \frac{3}{13}$ , as a decimal, correct to one decimal place.

$$\frac{6}{11} - \frac{3}{13} = 0.54 - 0.23 = 0.31 = 0.3$$
or
$$\frac{6}{11} - \frac{3}{13} = \frac{6 \times 13 - 3 \times 11}{11 \times 13} = \frac{78 - 33}{143} = \frac{45}{143} = 0.31 = 0.3$$

## Blunders (-3)

Blunder in converting fraction to decimal merits attempt mark at most except where candidate works correctly to 45/143.

B1: Each step of three omittedB2: Incorrect or omitted round-off

*Slips (-1)* S1: Slip in minus sign

Misreadings (-1) M1: Reads ÷ for – (Ans. 2.363)

*Attempts* Att: Works with 3/3 or 9/24 or 78/33 or 33/78 or 6/2 or 3/2 or 6/24 or 3/24

$$\frac{116}{140} \times 100 = 82.85 = 83.$$

*Blunders (-3)* Any blunder in calculating the percentage results in 4 marks at most. B1: Incorrect or omitted round-off

*Slips (-1)* S1: Slips in multiplication or addition

*Misreadings (-1)* M1: Misreading any number

*Attempts* Att: Effort at calculating any step. Att: Answer of 24, 14 or 34 Part (ix)

(ix) Find the exact value of

 $\frac{(1.25 \times 10^4) - (9.1 \times 10^3)}{(6.8 \times 10^1)}.$ 

$$\frac{\left(1.25 \times 10^{4}\right) - \left(9.1 \times 10^{3}\right)}{\left(6.8 \times 10^{1}\right)} = \frac{12500 - 9100}{68} = \frac{3400}{68} = \mathbf{50}$$
  
or  
$$\frac{\left(1.25 \times 10^{4}\right) - \left(9.1 \times 10^{3}\right)}{\left(6.8 \times 10^{1}\right)} = \frac{12.5 \times 10^{3} - 9.1 \times 10^{3}}{6.8 \times 10^{1}} = \frac{3.4 \times 10^{3}}{6.8 \times 10^{1}} = 0.5 \times 10^{2} = \mathbf{50}$$

Blunders (-3)

- B1: Blunders in dealing with scientific notation
- B2: Blunders in order of precedence
- B3: Each omitted or incorrect step, if slips not clear
- B4: Fraction inverted (Ans (0.02)
- B5: Blunder  $1.25 \times 40$ , once only, if blunder consistent

*Slips (-1)* S1: Any number incorrect by factor of 10 when written in decimal form

Attempts

Att: Some correct work, e.g. approximation with correct order of magnitude 1.25 - 0.1

Att:  $\frac{1.25 - 9.1}{6.8} = -1.154$ 

Note:  $(12500 \div 68) - 9100 = -8916.176$  $12500 - (9100 \div 68) = 12366.176$  Part (x)

(x) Find the exact value of

 $\frac{59.4 - 3.85}{6.54 + 4.46}.$ 

$$\frac{59.4 - 3.85}{6.54 + 4.46} = \frac{55.55}{11} = 5.05.$$

Blunders (-3)

B1: Blunders in order of precedence, applied once

B2: Each omitted or incorrect step if slips not clear

B3: Fraction inverted (Ans. 0.198)

*Slips (-1)* S2: Numerical slips, including misplacing decimal point – max. of 3

*Misreading (-1)* M1: Uses  $\times$  instead of + or  $\div$  instead of - vice versa

Attempt Att: Some correct step Att: Work at estimating answer

Note:  $(59.4 \div 6.54) - (3.85 \div 4.46) = 9.0825 - 0.8632 = 8.2193$   $(59.4 \div 6.54) + (3.85 \div 4.46) = 9.0825 + 0.8632 = 9.9457$   $59.4 - [3.85 \div (6.54 + 4.46)] = 59.4 - 0.35 = 59.05$   $(59.4 - 3.85) \div 6.54 + 4.46 = 55.55 \div 6.54 + 4.46 = 8.4938 + 4.46 = 12.9538$  $59.4 - (3.85 \div 6.54) + 4.46 = 59.4 - 0.5886 + 4.46 = 63.2714$ 

Part (a)	10 marks	Att 0
Part (b)	20 marks	Att 8
Part (c)	20 marks	Att 0

Part (a)

## 10 (5 + 5) marks

Hit or miss

(a) Change to metres
 (i) 2.5 km
 (ii) 650 cm.

(i)	$2.5 \text{ km} = 2.5 \times 1000 = 2500 \text{ m}$
(ii)	$650 \text{ cm} = \frac{650}{100} = 6.5 \text{ m}.$

100

(i) Correct answer 5 marks, otherwise 0

(ii) Correct answer 5 marks, otherwise 0

Part (b)

(b) Michael is paid  $\in 8.50$  per hour. The table below shows the hours he worked last week.

Day	Starting Time	Finishing Time
Monday	10:00	13:00
Tuesday	15:00	17:30
	10.00	<b>A</b> 1 AA

- (i) How many hours did Michael work last week?
- (ii) How much did he earn last week?

(i) Number of hours = 3 + 2.5 + 3 = 8.5 hours

(ii) Earns €8.5 × 8.5 = €72.25

Section (i):

Blunders (-3)

- B1: Blunder in calculating hours worked, each time, if not consistent
- B2: Incorrect conversion of hours and minutes
- B3: Time interval not calculated, each time

*Slips (-1)* S1: Slips in addition

*Attempts* Att: One time interval calculated.

Note: No work shown other than 8.5 written allow 10 marks for part (i)

Section (ii): Work from candidates answer to part (i) Apply maximum of three slips if long multiplication used. Blunders (-3) B1: Writes €8.5 × 8.5 without working

*Slips (-1)* S1: Slips in multiplication Part (c)

- (c) A family travelled 110 km by car from Cavan to Dublin, and a further 50 km to Wicklow. The total time for the journey was 4 hours.
  - (i) Calculate the total distance travelled.
  - (ii) Calculate the average speed for the whole journey.
  - (iii) The average speed from Cavan to Dublin was 44 km/hr. How long did this part of the journey take?
  - (i) Total distance = 110 + 50 = 160 km

(ii) Speed = 
$$\frac{160}{4}$$
 = 40 km per hour

(iii) Time = 
$$\frac{110}{44}$$
 = 2.5 hours

- (i) Correct distance merits 5 marks, otherwise 0
- (ii) Correct average speed merits 5 marks, otherwise 0
- (iii) Correct time merits 10 marks, otherwise 0.

Part (a)	10 marks	Att 4
Part (b)	20 marks	Att 8
Part (c)	20 marks	Att 4

Part (a)	<b>10</b> (5 + 5) marks	Att (2 + 2)
(a)	A student estimates the height of a tree to be 12 metres. The true hei 11.35 metres. Find (i)the error in the estimate.	ght of the tree is

(ii) the percentage error, correct to two decimal places.

(i) Error = 12 - 11.35 = **0.65**  
(ii) Percentage error = 
$$\frac{0.65}{11.35} \times 100 = 5.726\% = 5.73\%$$

#### Blunders (-3)

- B1: Takes 12 + 11.35 (Ans. 23.35)
- B2: Blunders in percentages e.g. 11.35/0.65 (Ans. 24)
- B3: Divides by 12
- B4: Incorrect or omitted round-off

Slips (-1) S1: Writes  $(12/11.35) \times 100 = 105.73\%$ 

Attempts Att: Writes 12/11.35 and stops Att: Writes 11.35/12 and stops Att: Writes  $12 \times 11.35$  and stops Att: Writes 100/11.35 Att: Writes 11.35 × 100 or 11.35/100 Att: Mean of 12 and 11.35 found

- (b) (i)Express the ratio 15:21 in its simplest form.
  - (ii) A prize of €72 is divided between two people in the ratio 15:21. How much does each person get?

(i) 15: 21 = 5: 7(ii) 5+7=12One person gets  $\frac{72}{12} \times 5 = \textbf{€30}$ Second person gets €72 - €30 = €42 or  $\frac{72}{12} \times 7 = \textbf{€42}$ .

Section (i) Blunders (-3) B1: Blunder in simplifying ratio B2: Answer 7 : 5

Slips (-1)S1: Correct ratio not in simplest form e.g. 30: 42S2: Numerical slips in calculation

Section (ii) Blunders (-3) B1: Uses incorrect ratio e.g. 5/7 or 7/5 B2: Calculates 1/5 or 1/7 as person's shares B3: Calculates only one person's share

*Slips (-1)* S1: Numerical slips in calculation

Attempts Att: Answer 72/2 = 36 Part (c)

(c) €3500 is invested for four years at a fixed rate of compound interest. During the first year it earns €140.
(i) What is the annual rate of interest?
(ii) How much will the investment be worth at the end of the four years? Give your answer correct to the nearest euro.

rate =  $\frac{140}{3500} \times 100 = 4\%$ . (i) (ii) A =  $\notin 3500(1+0.04)^4 = \notin 3500(1.04)^4 = \notin 3500(1.169858)$ = €4094.50 = €4095 or Year 1: Principal €3500, Interest €140 Year 2: Principal €3640, Interest €145.60 Year 3: Principal €3785.60, Interest €151.424 Year 4: Principal €3937.024, Interest €157.48096 Amount after 4 years €4094.50 = €4095

Section (i) Correct answer merits 10 marks, otherwise 0.

Section (ii) Blunders (-3) Working with an incorrect rate from (i) merits attempt mark at most.

Award 10 marks for a fully correct answer. Award 7 marks for a correct answer not rounded correctly. Award Attempt 4 for any other work of merit.

Part (a)	10 marks	Att 4
Part (b)	20 marks	Att 8
Part (c)	20 marks	Att 6
Part (a)	10 marks	Att 4
(a) Solve $5x - 7 = 2x + 14$ .		

$$5x - 7 = 2x + 14 \implies 5x - 2x = 14 + 7 \implies 3x = 21 \implies x = 7$$

Award full marks for a correct answer with no work shown

Blunders (-3) B1: Blunders in grouping terms e.g. 2x + 14 = 16xB2: Each step omitted B3:  $3x = 21 \implies x = 18$  or x = 24 or x = 63

Slips (-1) S1: Slips in signs on crossing "=", each time

Attempts

\*

- Att: Some correct step towards solution
- Att: Stops after one transposition
- Att: Effort at trial and error, by substitution

(b) Solve the simultaneous equations

x + 3y = 42x - y = 15

$$\begin{array}{rcrcrcrc} x + 3y &= & 4 &=> & x + 3y = & 4 \\ 2x - y &= & 15 &=> & \underline{6x - 3y = 45} \\ & & & 7x &= & 49 &=> & x = & 7 \end{array}$$
$$x + 3y = & 4 &=> & 7 + & 3y = & 4 &=> & 3y = & 4 - & 7 = & -3 &=> & y = & -1 \end{array}$$

First variable found:

Award 15 marks for first variable fully correct, with or without work. Award Attempt 6 for other work of merit, e.g. work towards cancelling one variable.

*Second variable found:* Award 5 marks for second variable correct (from candidates previous work) otherwise 0.

*Worthless (0)* W1: Incorrect answers, no work shown

Part (c)	20 (10 + 10) marks	Att (4 + 4)	
(c)	When 8 is added to five times a certain number, the result is the same as when 12 is added to three times the number.		
	<ul> <li>Let <i>x</i> represent this number.</li> <li>(i) Write this information as an equation in <i>x</i>.</li> <li>(ii) Solve the equation to find the value of <i>x</i>.</li> </ul>		

(i) 5x + 8 = 3x + 12

(ii)  $5x + 8 = 3x + 12 \implies 2x = 4 \implies x = 2$ 

\* There must be an effort to set up equation in *x*, including 5 or 3, for the award of any of the first 10 marks.

\* For award of marks for solving – use candidate's equation.

Blunders (-3)

- B1: Blunder in setting up equation e.g. 5(8 + x) for 5x + 8
- B2: Each omitted step of three steps, 5x + 8, 3x + 12, equality

*Slips (-1)* S1: Slips in signs

Attempts Att: Set-up: Writes 5x or x + 8 etc. and stops Att: Effort at trial and error

Part (a)	10 marks	Att 4
Part (b)	20 marks	Att 8
Part (c)	20 marks	Att 8

Part (a)	10 (5 + 5) marks	Att (2 + 2)
(a) (i) (ii	Write down the whole number factors of 20. Write down the factors of 20 that are prime.	

(i)1, 2, 4, 5, 10, 20 (ii) 2, 5

Section (i) Slips (-1) S1: Each omitted or incorrect factor

Attempts Att: Any one correct value

Section (ii) Slips (-1) S1: Each omitted or incorrect prime number

Attempts Att: Attempt at factors of 20 Att: Defines prime number Att: List from (i) is repeated in (ii). (b) Solve the quadratic equation  $2x^2 + 5x - 1 = 0$ . Give your answers correct to two decimal places.

$$2x^{2} + 5x - 1 = 0 \Longrightarrow x = \frac{-5 \pm \sqrt{25 - 4(2)(-1)}}{2(2)} = \frac{-5 \pm \sqrt{25 + 8}}{4} = \frac{-5 \pm \sqrt{33}}{4}$$
$$\implies x = \frac{-5 \pm 5.744}{4} = \frac{0.744}{4} \text{ or } \frac{-10.744}{4} \Longrightarrow x = 0.186 \text{ or } -2.686$$
$$\implies x = 0.19 \text{ or } -2.69$$

Award 20 marks for fully correct (both solutions) correctly rounded.

Award 17 marks for both solutions correct but one or both not correctly rounded.

Award 10 marks for one correct solution (rounded or otherwise)

## Award Attempt 8 for any work of merit.

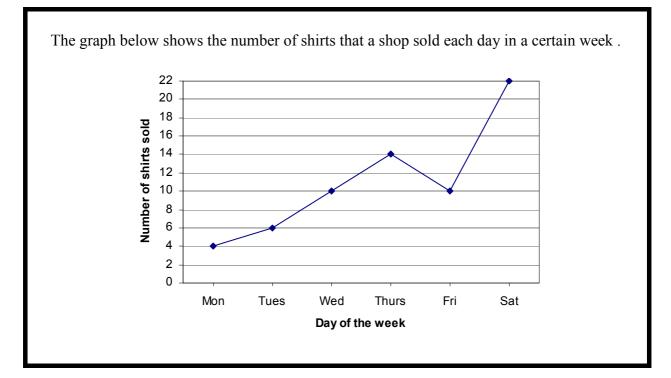
Part (c)

(c) (i) Solve 2x-5≤1
(ii)Solve 4-x ≤ 3
(iii) Write down all the whole numbers which satisfy both 2x-5≤1 and 4-x ≤ 3.

(i) $2x - 5 \le 1 \Longrightarrow 2x \le 6 \Longrightarrow x \le 3$ (ii)  $4 - x \le 3 \Longrightarrow -x \le -1 \Longrightarrow x \ge 1$ (iii)  $\{1, 2, 3\}$ 

- (i) Award 5 marks for fully correct answer. Award attempt 2 for anything else of merit.
- (ii) Award 5 marks for fully correct answer. Award attempt 2 for anything else of merit.
- (iii) Award 10 marks for fully correct answer.Award attempt 4 for anything else of merit.Candidates answers to (i) and (ii) not both correct => attempt 4 at most.

<b>QUESTION 6</b>		
Part (i)	10 marks	Att 4
Part (ii)	10 marks	Att 4
Part (iii)	10 marks	Att 4
Part (iv)	10 marks	Att 4
Part (v)	10 marks	Att 4



#### Part (i)

#### 10 marks

Att 4

(i) How many shirts were sold on Tuesday?

6 shirts

*Blunders(-3)* B1: Answer 14 (Thursday)

Attempts Att: Ans is 4 or 10 or 22

*Worthless* W1: Any other value (ii) On which day of the week was the smallest number of shirts sold?

#### Monday

*Blunders(-3)* B1: Answer is 4 B2: Answer is Saturday

*Worthless (0)* W1: Any other day given

## Part (iii)

## 10 marks

Att 4

(iii) The shop had 100 shirts at the start of the week. How many were left at the end of the week?

100 - (4+6+10+14+10+22) = 100 - (66) = 34 shirts

*Blunders (-3)* B1: Subtraction omitted

Slips (-1) S1: Each omitted or incorrect value in calculating addition

Attempts Att: One correct value read At: 100 – one day's sales (Ans 96, 94, 90, 86, 78) (iv) Calculate the average number of shirts sold per day.

Average = 
$$\frac{66}{6}$$
 = 11 shirts

*Blunders (-3)* B1: Blunder in average e.g. division by 7 B2: 34/6 = 5.6 B3: Answer left as 66/6 or equivalent. *Slips (-1)* S1: Slips in calculation

*Attempts* Att: Some effort at finding average

Part (v)	10 marks	Att 4

(v) The shirts were sold for €10 each. The shop paid €6 for each shirt. Calculate the average daily profit from shirt sales.

Profit on a shirt =  $\notin 10 - \# 6 = \# 4$ . Average daily profit is (# 4)(11 shirts) = # 44.

\* Accept incorrect answer from (iv) without further penalty

Blunders (-3)

B1: Omission of each step of three (maximum)

B2: Blunder in finding profit e.g. 10 + 6

B3: Profit for week calculated (Ans 264)

*Slips (-1)* S1: Numerical slips

*Attempts* Att: Some relevant calculation attempted

Graph	30 marks	Att 12
Values	20 marks	Att 8
Table	30 marks	Att 8
Graph	10 marks	Att 4

#### Blunders (-3)

- B1: Additional line in table
- B2: Blunder such as  $2x^2 = (2x)^2$  or 4x or +1 = x + 1 or +1 = x consistently across full line Otherwise (-1) applied to each incorrect value in the line

#### *Slips (-1):*

- S1: Each incorrect or omitted value in body of table
- S2: Each incorrect or omitted f(x) value, calculated from candidate's work
- S3: Error in sign applied consistently across a line

#### Attempts:

Att: Any four correct calculated values in the table or function form

## **Plotting Graph:**

If candidate's values not fully correct than attempt mark at most for graph.

#### Blunders (-3)

- B1: Points joined in incorrect order
- B2: Blunders in scales on axes, including reversing + for -.

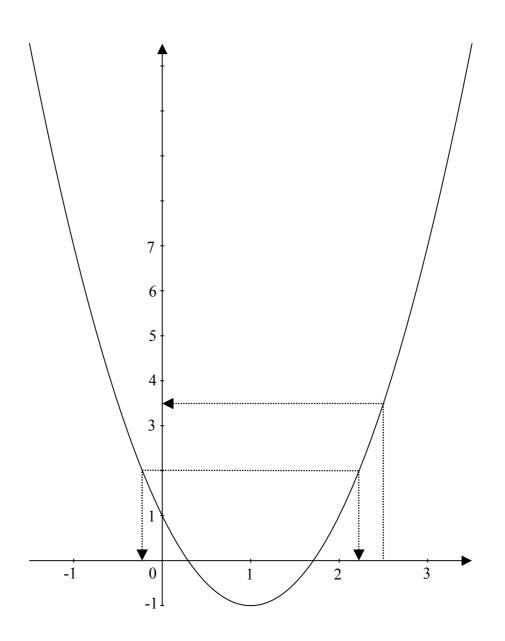
## *Slips (-1):*

- S1: Each point plotted incorrectly, using students values
- S2: Each pair of successive points not joined, maximum of 3
- S3: Points joined by line segments in the correct order
- S4: Axes reversed

Attempts:

Att: Any two of candidate's points plotted.

x	-1	0	1	2	3
$2x^2$	2	0	2	8	18
- 4 <i>x</i>	4	0	- 4	- 8	- 12
+ 1	1	1	1	1	1
f(x)	7	1	- 1	- 1	7



Use your graph to estimate

- (i) the minimum value of f(x)
- (ii) the value of f(2.5)
- (iii) the values of x for which f(x) = 2
- (iv) the range of values of x for which f(x) is increasing.

(i)Minimum value of f(x) = -1

- (ii) f(2.5) = 3.5
- (iii) f(x) = 2 for x = -0.2 or x = 2.2
- (iv) f(x) is increasing for  $1 < x \le 3$
- \* Accept candidate's value from graph for award of marks
- \* Allow tolerance in reading values of  $\pm 0.2$

Blunders (-3)

- B1: Each value outside the tolerance
- B2: Only one value given in part (iii)

*Misreading (-1)* 

- M1: Misreads the value of x corresponding to the minimum of f(x)
- M2: Misreads increasing for decreasing

Attempts:

Att: Effort at reading values from graph

Att: For solving equation algebraically, correctly

## STATE EXAMINATIONS COMMISSION MARKING SCHEME

## **LEAVING CERTIFICATE EXAMINATION 2004**

## MATHEMATICS

## FOUNDATION LEVEL

## PAPER 2

#### **GENERAL GUIDELINES FOR EXAMINERS - PAPER 2**

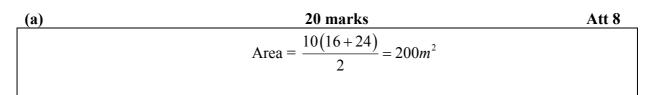
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Frequently occurring errors to which these penalties must be applied are listed in the scheme. They are labelled as B1, B2, B3,...., S1, S2, S3,..., M1, M2, etc. Note that these lists are not exhaustive.

- 2. When awarding attempt marks, e.g. Att(3), note that
  - any correct relevant step in a part of a question merits at least the attempt mark for that part
  - if deductions result in a mark which is lower than the attempt mark, then the attempt mark must be awarded
  - a mark between zero and the attempt mark is never awarded.
- 3. Worthless work is awarded zero marks. Some examples of such work are listed in the scheme and they are labelled as W1, W2,....etc.
- 4. The phrase "hit or miss" means that partial marks are not awarded the candidate receives all of the relevant marks or none.
- 5. The *same* error in the *same* section of a question is penalised *once* only.
- 6. Special notes relating to the marking of a particular part of a question are indicated by an asterisk. These notes immediately follow the box containing the relevant solution.
- 7. Particular cases, verifications and answers derived from diagrams (unless requested) qualify for attempt marks at most.
- 8. A serious blunder, omission or misreading merits the ATTEMPT mark at most.
- 9. The phrase "and stops" means that no more work is shown by the candidate.
- 10. Accept the best of two or more attempts even when attempts have been cancelled.
- 11. Allow comma for decimal point, e.g. €5.50 may be written as €5,50.

Att 8
Att 12
_

Part (a)	20 marks	Att 8
	Find the area of the trapezium shown $a  16 \text{ m}  d$ $b  24 \text{ m}  c$	10 m



Blunders (-3)

- B1 Area =  $\frac{ah}{2}$  or  $\frac{bh}{2}$  or  $\frac{ab}{2}$  and continues
- B2 Failure to divide by 2

B3  $10 \times 16 \times 24$  apply  $2 \times (-3)$ , no division by 2 and multiplication for addition.

B4 16 + 24 = 40 only, apply  $2 \times (-3)$ , no multiplication by h and no division

B5  $16 \times 10 = 160$  or  $24 \times 10 = 240$  or  $16 \times 24$  apply  $2 \times (-3)$ 

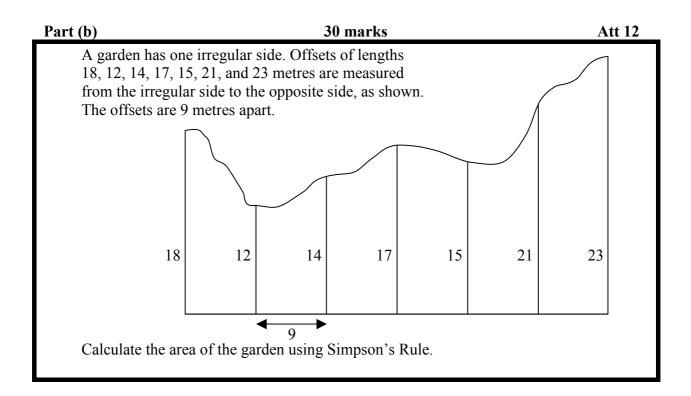
Slips (-1)

S1 Numerical errors to a max of three

S2 Area =  $\frac{24(10+16)}{2}$ 

Attempts (8 marks)

- A1 Copies diagram
- A2 Defines length or area.
- A3 Correct formula only



$$Area = \frac{1}{3}height \Big[ 1^{st} + Last + 2(odd) + 4(even) \Big]$$
$$Area = \frac{9}{3} \Big[ 18 + 23 + 2(14 + 15) + 4(12 + 17 + 21) \Big]$$
$$Area = 3 \Big[ 299 \Big] = 897m^2$$

Blunders (-3)

- B1 Uses 'four odd and twice even'
- B2 Omits 2 or 4 in the formula or both.
- B3 Omits h or uses an incorrect h or does not divide h by 3.

## Slips (-1)

- S1 Each incorrect or omitted altitude
- S2 Numerical errors to a max of three.

## Attempts (12)

- A1 Gives Simpson's formula only
- A2 Copies diagram

Part (a)	20 (10,10) marks	Att (4, 4)	
Part (b)	<b>30</b> (15, 15) marks	Att (6, 6)	
Part (a)	20 (10, 10) marks	Att (4, 4)	
(a) A disc has a diame Write down the rad Find the area of the		12 cm	

Radius	10 marks	Att 4
	$Diameter = 12cm \Longrightarrow Radius = 6cm$	

Blunders (-3)

B1 Multiplies 12 by 2

*Slips (-1)* S1 Error in calculations

Attempts (3)

A1 Draws diagram

A2 Defines radius

Area	10 marks	Att 4
	$Area = \pi r^2 \Longrightarrow Area = 113 cm^2$	
	or	
	$Area = \frac{\pi d^2}{4} = \frac{\pi (12^2)}{4} = 113cm^2$	

#### Blunders (-3)

- B1 Incorrect value of radius, accept candidate's value.
- B2 Addition for multiplication

B3  $r^2 = 2r$ 

B4 Incorrect or no value for  $\pi$ .

B5 No round off or incorrect round off.

Slips(-1) S1 Numerical errors Misreading: uses  $4\pi r^2$ 

## *Att(-4)*

A1 Gives any circle formula or value for  $\pi$  from any line with circle disc or sphere.

(b)(i	)	15 marks	Att6
(b)	<ul> <li>A container in the shape of an filled with orange juice. The cone is 18 cm and the height if</li> <li>(i) Find the volume of oran container, in terms of π</li> </ul>	diameter of the is 27 cm. nge juice in the	27 cm
<b>(b</b> )	)(i)	15 marks	Att6
		$Vol = \frac{\pi r^2 h}{3}$	
		$Vol = \frac{\pi \times (9)^2 \times 27}{3} = 729\pi$	
<i>Blun</i> B1 B2 B3 B4	<i>iders(-3)</i> $r^2 = 2r$ or fails to evaluate $r^2$ Incorrect value for r Incorrect or no value for h. 729 or 2290.22		
<i>Slips</i> S1	s(-1) Numerical errors		
Atter A1	<i>npts</i> Draws diagram		
(ii)		15 marks	Att 6
	The orange juice is then pour cylindrical can of diameter 12 Find <i>h</i> , the depth of the orang in the can.	2 cm.	h
(ii)		15 marks	Att 6
		$\pi r^2 h = 729\pi$ $\Rightarrow h = \frac{729\pi}{36\pi} = 20.25$	

## Blunders(-3)

- B1 Uses incorrect radius
- Transposition error B2
- B3  $r^2 = 2r$

*Slips(-1)* S1 Numerical errors A1

*Att(3)* Draws diagram

Part (a)	10 (5, 5) marks	Att (2, 2)
Part (b)	20 (5, 5, 5, 5) marks	Att (2, 2, 2, 2)
Part (c)	20 (5, 5, 5, 5) marks	Att (2, 2, 2, 2)

Part	t (a)	10 marks	Α	tt (2, 2)
(a)	The (i) (ii)	diagram shows an isosceles triangle. Find the value of $x$ Find the value of $y$	y <sup>o</sup> x 1	30

(i) <i>x</i>	5 marks	Att 2
(ii) <i>y</i>	5 marks	Att 2
	$x = 180^{\circ} - 130^{\circ} = 50^{\circ}$	
	$y = 180^{\circ} - 100^{\circ} = 80^{\circ}$	
* Accept answers of	n diagram	

Accept answers on diagram

## Blunders (-3)

- Sum of internal angles  $\neq 180^{\circ}$ B1
- Straight angle  $\neq 180^{\circ}$ B2

## Slips(-1)

S1 Numerical error

## *Attempts*(4,2,2)

Uses protractor Copies diagram A1

A2

Part (b)	20(5, 5, 5, 5) marks	Att (2, 2, 2, 2)
(b) The diagram shows a p Find the measure of: (i) the angle A (ii) the angle B (iii) the angle C (iv) the angle D	oarallelogram.	80° A B ° D
Angle A	5 marks	Att2
Angle B	5 marks	Att2
Angle C	5 marks	Att2
Angle D	5 marks	Att2
	$A = 100^{\circ}$	
	$B = 30^{0}$	
	$C = 50^{0}$	
	$\mathrm{D}=100^o$	

- B1 Angle on straight line  $\neq 180^{\circ}$
- B2  $B \neq 30^{\circ}$
- B3  $C \neq 50^{\circ}$
- B4  $D \neq 100$  (watch for A=D)

Slips (-1)

S1 Numerical errors

# Attempts(2)

- A1 Additional material on a diagram
- A2 Copies diagram

(c)	20 (5, 5, 5, 5) marks	Att (2, 2, 2, 2)
	<ul> <li><i>o</i> is the centre of the circle,</li> <li>[<i>pt</i>] is a diameter of the circle and <i>r</i> is a point on the circle and <i>l ∠pro</i>   = 37°,  <i>rt</i>   = 6 cm and  <i>ot</i>   = 5 cm. Find: <ul> <li>(i) the measure of the angle X</li> <li>(ii) the measure of the angle Y</li> <li>(iii) the length of the diameter [<i>pt</i>]</li> <li>(iv) the length of [<i>pr</i>].</li> </ul> </li> </ul>	ircle. $7$ $7^{\circ}X$ $6$ $7$ $7^{\circ}X$ $6$ $7$ $7^{\circ}X$ $6$ $7$ $7^{\circ}X$ $6$ $7$ $7^{\circ}X$ $7^{$
(i)	5 marks	Att2

(i)	5 marks	Att2
(ii)	5 marks	Att2
(iii)	5 marks	Att2
(iv)	5 marks	Att2
	$(i)X = 90^{\circ} - 37^{\circ} = 53^{\circ}$	
	$(ii)Y = 37^{\circ}$	
	(iii) pt  = 10cm	
	$(iv) pr ^2 = 100 - 36$	
	$\Rightarrow  pr  = 8$	

- B1  $|\angle prt| \neq 90^{\circ}$
- B2  $Y \neq 37^{\circ}$
- B3 Diameter = 5 divided by 2
- B4 Any error in setting up or solving Pythagoras

# Slips (-1)

S1 Numerical errors

# *Attempts*(2,2,2,2)

- A1 Draws diagram
- A2 Any attempt to define Pythagoras
- A3 Uses trigonometric ratio unsuccessfully

15 marks	Att 6
20(5, 5, 5, 5) marks	Att (2, 2, 2, 2)
15(5, 5, 5)marks	Att (2, 2, 2)
	20(5, 5, 5, 5) marks

Part (a)15 marksAtt 6(a)p(3,6) and q(-3,-2) are two points.<br/>Find the length of [pq]

Find the length of  $\lfloor pq \rfloor$ 

Part (a)	15 marks	Att 6
	$ pq  = \sqrt{(-3-3)^2 + (-2-6)^2}$	
	pq  = 10	

### Blunders (-3)

B1 No use of square root

B2  $X^2 = 2X$ 

B3 Error in signs

Slips (-1)

- S1 Numerical errors
- S2 Each incorrect substitution

### Attempts(6)

- A1 Plots points only
- A2 Correct slope or mid point formula plus some substitution

Part (b)		20(5, 5, 5, 5)	Att (2, 2, 2, 2)
a(-1, (i) (ii) (iii) (vi)	<ul> <li>3) and b(3,5) are two points.</li> <li>Plot the points a and b on graph Write down the co-ordinates of Find the slope of ab</li> <li>Find the equation of the line ab</li> </ul>	f the midpoint of [ab].	
(i) (ii) (iii) (iv)		5 marks 5 marks 5 marks 5 marks	Att2 Att2 Att2 Att2 Att2
	(i) Plot points (ii) <i>Mid Point</i> = $\left(\frac{-1+3}{2}, \frac{3+3}{2}, \frac{3+3}{2}\right)$ (iii) <i>Slope</i> = $\frac{5-3}{3-(-1)} = \frac{2}{4} = \frac{1}{2}$ (iv)	$\left(\frac{+5}{2}\right) = (1,4)$	$5 \bullet b \bullet $ $4 + $ $a \bullet 3 + $ $2 + $ $1 + $ $-1 + 2 = 3$
	$y-5 = \frac{1}{2}(x-x)$ or $y-3 = \frac{1}{2}(x+x)$		

- B1 No division by 2
- B2 No division
- B3 Mathematical error

# Slips(-1)

- S1 Numerical errors
- S2 Each incorrectly plotted point
- S3 Each incorrect substitution

# Atts(2)

A1 Draws axes

Part	z (c)	15 (5, 5, 5) marks	Att (2, 2, 2)
	The line <i>L</i> has equation $k$ is the point (2,-1).	on $4x + y - 7 = 0$	
(i) (ii) (iii)	Show that the point A Write down the slop Find the equation of		pendicular to the line <i>L</i> .
(i)		5 marks	Att 2
(ii)		5 marks	Att 2
(iii)		5 marks	Att 2
	(i)		
		4x + y - 7 = 0	
		4(2) + (-1) - 7	
		8 - 1 - 7 = 0	
	(ii)		
		4x + y - 7 = 0	
		$\Rightarrow y = -4x + 7$	
		$\Rightarrow m = -4$	
	(iii)		
		$y - (-1) = \frac{1}{4}(x - 2)$	
		$\Rightarrow y+1=\frac{1}{4}(x-2)$	

B1 In (ii) slope = 
$$4,\pm 1,\pm 7,\pm \frac{1}{4},\pm \frac{7}{4},\pm \frac{4}{7}$$

B2 Incorrect slope in (iii)

Slips(-1)

- S1 Numerical errors
- S2 Each incorrect substitution

*Attempts*(2,2,2)

- A1 Draws a sketch
- A2 Writes down correct relevant formula

Part (a)	10 (5, 5) marks	Att (2, 2)
Part (b)	20 marks	Att 8
Part (c)	20(5, 15) marks	Att (2, 6)

Part (a)	10 marks	Att (2, 2)
The diagram shows a right-angled triangle with sides of length 5, 12 and 13 cm and angles named $A$ and $B$ .	13 B	5
<ul><li>(i) Write down sin<i>A</i> as a fraction</li><li>(ii) Write down cos<i>B</i> as a fraction</li></ul>	$A \square$	

(i) (ii)				5 marks 5 marks	Att 2 Att 2
	(i)	$SinA = \frac{5}{13}$	(ii)	$CosB = \frac{5}{13}$	

\* Accept correct decimals

\* Accept 
$$Sin\left(\frac{5}{13}\right), Cos\left(\frac{5}{13}\right)$$

Blunders(-3)

B1 Incorrect trigonometric ratio

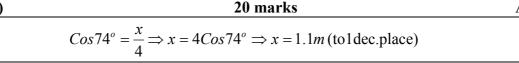
Slips

S1 Uses  $Sin = Sin^{-1}or \ Cos = Cos^{-1}$  to find the value of the angle  $A = 22.62^{\circ} orB = 67.38^{\circ}$ 

# Attempts(2,2)

- A1  $Cos = \frac{adj}{hyp}$  only, same for Sin.
- A2 SOHCAHTOA or equivalent in (i),(ii)
- A3 Draws diagram

Part(b)	20 marks	Att 8
A ladder leans against a makes an angle of 74° w	wall. The ladder is 4 m long and ith the ground.	
Find <i>x</i> , the distance from the wall to the foot of th		4 m 74°
Give your answer corre	ct to one decimal place.	<u> </u>
Part(b)	20 marks	Att 8



- B1 Incorrect trigonometric ratio
- B2 Transposition error

# Slips(-1)

- S1 Fails to round off
- S2 Numerical errors
- S3 Wrong mode (calculator)

### Attempts(6)

- A1 Measures from diagram
- A2 Some attempt at Pythagoras
- A3 Any combination of 4 and 7

(ii) Find the measure of the angle <i>A</i> .	Part(c)	20 (5, 15) marks	Att (2, 6)
Give your answer to the nearest degree.		in the diagram.	

_(i)	5 marks	Att2
	$h^2 = 3^2 + 4^2$	
	$h = \sqrt{25} = 5$	

B1 Any error in setting up Pythagoras B2  $3^2 = 3 \times 2$ 

*Slips(-1)* S1 Numerical errors

Attempts(-1) A1 States Pythagoras

_(ii)	15 marks	Att 6
	TanA = 0.75	
	$\Rightarrow A = 37^{\circ}$	
Blunders(-3)	* Note:	

B1 Uses incorrect ratio	RATIO	DRG	RAD	GRAD	
<i>Slips(-1)</i> S1 Numerical errors	$\cos(\frac{4}{5})$	0.013	0.6967	0.9999	
Atts	$\operatorname{Sin}(\frac{3}{5})$	0.01047	0.5646	0.0094	
A1 Copies diagram	2	0.013	0.9315	0.0118	
	$\operatorname{Tan}(\frac{3}{4})$				

Part(a)	10 marks	Att 4
Part(b)	20 (10, 5, 5) marks	Att (4, 2, 2)
Part(c)	20 (5, 5, 5, 5) marks	Att (2, 2, 2, 2)

Part (a)10marksAtt 4(a)Lunch in a certain hotel consists of a main course and a dessert. There are five<br/>different main courses and three different desserts. How many different lunch<br/>selections are possible?

Part (a)	10marks	Att 4
	5 × 3 =15	
Rhunders(-3)		

Blunders(-3) B1 3+5 B2 3! by 5!=720 B3 3! + 5!=126 B4 3 by 3 + 5 by 5 =34

*Slips(-1)* S1 Numerical

### Att(4)

A1 Number other than those above

Part (b)	20(10, 5, 5) marks	Att(4, 2, 2)
three are blue. The student takes (i) a blue (ii) a gree	homework copies in her bag. Eight of the s one copy at random from the bag. Fine copy n or a red copy red copy.	
(i) (ii) (iii)	10 marks 5 marks 5 marks	Att 4 Att 2 Att 2
(i) $P(Blue) = \frac{3}{12}$	$\frac{3}{5} = \frac{1}{5}$ , (ii) P(G or R) = $\frac{12}{15}$ , (iii) P(G or R) = $\frac{12}{15}$	$(Not Red) = \frac{7}{15}$
Blunders(-3)	2)	

B1 Incorrect n(S)

B2 Incorrect n(E)

B3  $\frac{15}{3}$  or  $\frac{5}{1}$ 

*Slips(-1)* S1 Numerical A school has two second-year classes: 2A and 2B. The table below shows the number of boys and girls in these classes.

_	2A	2B
Boys	10	15
Girls	14	11

(i) How many second-year students are there in the school?

One second-year student is chosen at random.

Find the probability that the student

(ii) is a boy in 2A

- (iii) is not a boy in 2A
- (iv) is a girl.

(i) (ii)	5 marks 5 marks	Att2 Att2
(ii) (iii)	5 marks	Att2
(iv)	$\frac{5 \text{ marks}}{(i) Students = 50}$	Att2
	$(ii)P(Boy/2A) = \frac{10}{50} = \frac{1}{5}$	
	$(iii)P(Not / Boy2A) = \frac{40}{50} = \frac{4}{5}$	
	$(iv)P(Girl) = \frac{25}{50} = \frac{1}{2}$	

### Blunders(-3)

B1 Incorrect n(S) apply once only, accept answer from (i)

B2 Incorrect n(E)

B3 Fails to divide by n(S) apply once only

B4 Inverted fraction apply once only

### Slips(-1)

S1 Numerical errors

Part (a)	10 marks	Att 4
Part (b)	25 (5, 10, 5, 5) marks	Att (2, 4, 2, 2)
Part (c)	15 (5,10) marks	Att (2, 4)
		(-) -

Part (a)	10 marks			Att 4	
Find th2 mean of the five numbers 6,	8,	12,	15,	19	

Part (a)	10 marks	Att 4
	$Mean = \frac{6+8+12+15+19}{12} = 12$	
	5	

#### Blunders(-3)

- B1 Incorrect numerator
- B2 Incorrect denominator
- B3 No division indicated

### Slips(-1)

S1 Numerical errors

### Attempts(4)

- A1 Defines mean
- A2 Picks a number between 6 and 19

### Part (b)

# 25 (5, 10, 5, 5) marks

# Att (2, 4, 2, 2)

The table below is a record of the number of days each of 80 students was absent during a school year.

Number of days absent	0 - 5	6 - 10	11 – 15	16 - 20	21 - 25
Number of students	8	12	30	24	6

Copy and complete the following cumulative frequency table.

Number of days absent	≤5	≤10	≤15	≤20	≤25
Number of students					

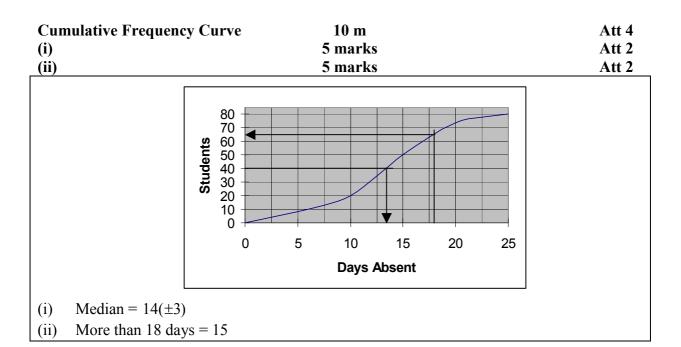
Draw the cumulative frequency curve.

Put the number of students on the vertical axis.

Use your curve to estimate

- (i) the median number of days absent
- (ii) the number of students who missed more than 18 days.

Table	5m Att 2				Att 2		
	Number of days absent	≤5	≤10	≤15	≤20	≤25	]
	Number of students	8	20	50	74	80	



- B1 Plot on mid-points
- B2 Error in scales one blunder
- B3 Points not joined
- B4 Uses incorrect axis for median

### Slips(-1)

- S1 Each incorrect or omitted value in table
- S2 Median not specified
- S3 Each incorrectly plotted point
- S4 Reverses axes
- S5 Joins points with straight lines

### Attempts(2,4,2)

- A1 Draws axes only
- A2 Copies table

Part(c)

Att (2, 4)

Find the mean and the standard deviation of the numbers 4, 6, 11, 15

correct to two places of decimals.

Mean Standard	l Deviation		5 marks 10 marks		Att 2 Att 4
	x	Mean	d	$d^2$	
	4	9	5	25	
	6	9	3	9	
	11	9	2	4	
	15	9	6	36	
	$\Sigma x = 36$			$\Sigma d^2 = 74$	
<i>Mean</i> = $\frac{\sum x}{n} = \frac{36}{4} = 9$ , Standard Deviation = $\sqrt{\frac{74}{4}} = 4 \cdot 3011 = 4 \cdot 30$					

\* Calculates mean merits 5, standard deviation merits 10

\* Accept correct answer without work

\* Any error in structure of SD merits attempt only

Blunders(-3)

B1 4+6+11+15=36 only

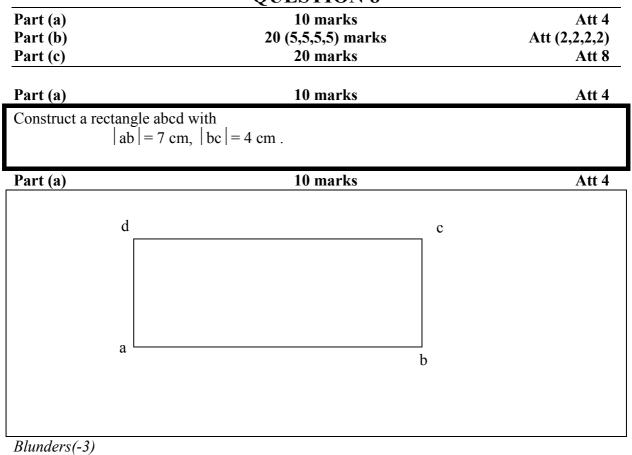
B2 Incorrect or no round off

Slips(-1)

S1 Numerical errors

Attempts(2,4)

A1 Any addition



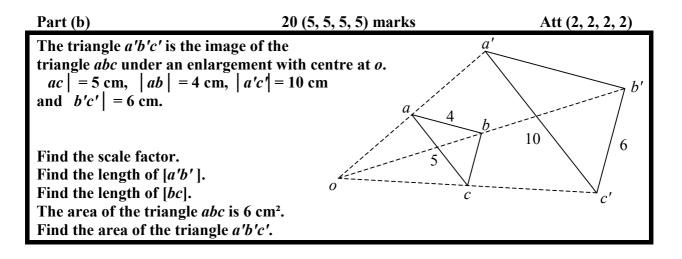
- B1 No two sides perpendicular
- B2 One or two sides left out

### Slips(-1)

- S1 Each side outside tolerance  $\pm 1cm$
- S2 each angle outside tolerance of  $\pm 5^{\circ}$

### Att(4)

A1 Any straight line



(i)	5 marks	Att 2
	Scale Factor = $\frac{10}{5} = 2$	

- B1 Inverts fraction
- B2 Incorrect numerator or denominator
- B3 Multiplies lengths

### Slips(-!)

S1 Numerical errors

(ii)	5 marks	Att 2
	$ a'b'  = 4 \times 2 = 8$	

### Blunders(-3)

B1 Makes no use of scale factor or uses incorrectly

#### Slips(-1)

- S1 Division for multiplication
- S2 Numerical once only

(iii)	5 marks	Att 2
	$ bc  = \frac{6}{2} = 3$	

### *Blunders(-3)*

B1 Makes no use of scale factor or uses incorrectly

### Slips(-1)

S1 Multiplication for division

(iv)	5 marks	Att 2
	$a'b'c' = 6 \times 2^2 = 24$	
	or	
	$a'b'c' = \frac{1}{2}(6) \times (8) = 24$	

### *Blunders(-3)*

- B1 Does not square scale factor
- B2 Error in area formula

### Slips(-1)

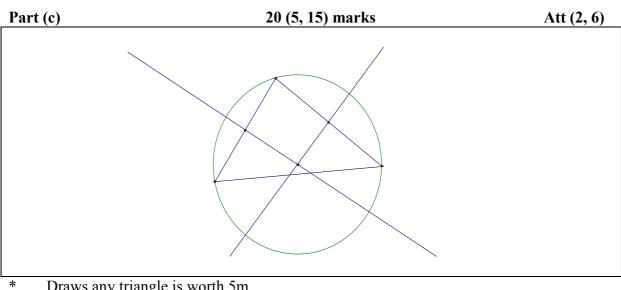
- S1 Division for multiplication
- S2 Numerical error

### Part (c)

### 20 (5, 15) marks

Att (2, 6)

Construct any triangle in your answerbook. Construct the circumscribed circle of the triangle. Show all construction lines clearly.



Draws any triangle is worth 5m

### Blunders(-3)

- Omits bisectors each time B1
- Draws bisectors only, no circle B2

## Slips(-1)

Circle does not pass through vertices, each time **S**1

## BONUS MARKS FOR ANSWERING THROUGH IRISH

Bonus marks are applied separately to each paper as follows:

If the mark achieved is less than 226, the bonus is 5% of the mark obtained, rounding *down*. (e.g. 198 marks  $\times$  5% = 9.9  $\Rightarrow$  bonus = 9 marks.)

Marks obtained	Bonus
226 - 231	11
232 - 238	10
239 - 245	9
246 - 251	8
252 - 258	7
259 - 265	6
266 - 271	5
272 - 278	4
279 – 285	3
286 - 291	2
292 - 298	1
299 - 300	0

If the mark awarded is 226 or above, the following table applies: