PAKTURK 8th National Interschool Maths Olympiad, 2013

 Solution:

 Solution:

 Solution:

 (
$$\frac{\sqrt{0.09} - \sqrt{0.01}}{\sqrt{0.09} + \sqrt{0.01}}$$
) ($\sqrt{4} \times \sqrt{16}$)

 Solution:

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 ($\frac{0.3 - 0.1}{0.3 + 0.1}$) (2×4) = $\frac{0.2}{0.4} \times 8 = \frac{1}{2} \times 8 = 4$

 Colspan="2">Colspan="2">Solution:

 ($\frac{0.3 - 0.1}{0.3 + 0.1}$) (2×4) = $\frac{0.2}{0.4} \times 8 = \frac{1}{2} \times 8 = 4$
 Answer: C

 Q4: Evaluate $\frac{0.00a}{0.0a} + \frac{0.bc}{0.a} - \frac{abc}{abc}$
 Answer: B

 Q2: Find the value of h in the equation

 $12\frac{1}{5} = h + 7\frac{4}{5}$
 Old $\frac{27}{5}$
 D) $\frac{33}{5}$

 Solution:

 Answer: B

 $\frac{d}{2} \times \frac{d}{5} \times \frac{d}{10\frac{d}{2}} + \frac{d}{10\frac{d}{2}} + \frac{d}{10\frac{d}{2}} - \frac{d}{10\frac{d}{2}\frac{d}{10\frac{d}{2}}} + \frac{d}{10\frac{d}{d}} + \frac{d}{10\frac{d}} + \frac{d}{10\frac{d}{d}} + \frac{d}{10\frac{d}{d}} + \frac{d}{$

C) 2 D) 1

√B) 3

A) 4

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Q6: Find the multiplicative inverse of *a* if

$$\frac{\left(1+\frac{1}{2}\right)\cdot\left(1+\frac{1}{3}\right)\cdot\left(1+\frac{1}{4}\right)\dots\left(1+\frac{1}{18}\right)}{\left(1-\frac{1}{2}\right)\cdot\left(1-\frac{1}{3}\right)\cdot\left(1-\frac{1}{4}\right)\dots\left(1-\frac{1}{8}\right)} = a$$

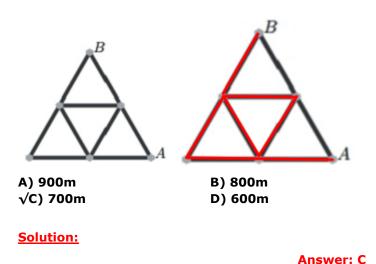
A) 76 \sqrt{B}) 1/76 C) 1/78 D) 78

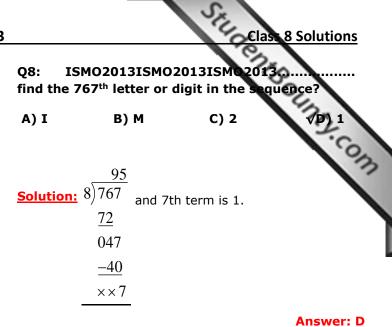
$$\frac{\left(1+\frac{1}{2}\right)\cdot\left(1+\frac{1}{3}\right)\cdot\left(1+\frac{1}{4}\right)\dots\left(1+\frac{1}{18}\right)}{\left(1-\frac{1}{2}\right)\cdot\left(1-\frac{1}{3}\right)\cdot\left(1-\frac{1}{4}\right)\dots\left(1-\frac{1}{8}\right)} = a$$

Solution:
$$\frac{\frac{\cancel{3}}{2} \cdot \frac{\cancel{4}}{\cancel{3}} \cdot \frac{\cancel{3}}{\cancel{4}} \dots \frac{\cancel{19}}{\cancel{18}}}{\frac{1}{\cancel{2}} \cdot \frac{\cancel{2}}{\cancel{3}} \frac{\cancel{3}}{\cancel{4}} \dots \frac{\cancel{7}}{\cancel{8}}} = \frac{19}{\cancel{2}} \cdot \frac{\cancel{3}}{\cancel{1}} = 19 \times 4 = 76 = a$$
$$\frac{1}{a} = \frac{1}{76}$$

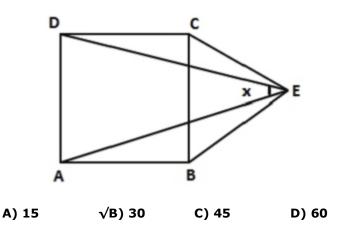
Answer: B

Q7: Each of the nine paths in a park is 100 m long. Ann wants to go from A to B without going along any path more than once. What is the length of the longest route she can choose?

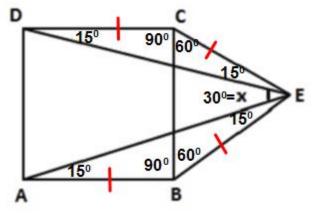




Q9: ABCD is a square and $\triangle BCE$ is an equilateral triangle. Find x^0







Answer: B

Q10: Which of the following is always an even number where n is a positive integer?

A) 7(n+2)√B) 7(2n+2)C) 7(3n+2)D) 7(7n+2)

Solution: $7(2n+2) = 7 \times 2 \times (n+1) = 14(n+1)$

Answer: B

Q11: If
$$3^x = \frac{1}{16}$$
 and $3^y = 32$ than $\frac{x}{y} = ?$

A)
$$\frac{5}{4}$$
 B) $\frac{1}{5}$ \sqrt{C} $-\frac{4}{5}$ **D)** $-\frac{5}{4}$

$$3^{x} = \frac{1}{16} \Longrightarrow 3 = \left(\frac{1}{16}\right)^{\frac{1}{x}} = 16^{-\frac{1}{x}} \Longrightarrow$$

Solution:
$$3^y = 32 \Rightarrow \left(16^{-\frac{1}{x}}\right)^y = 32 \Rightarrow 2^{-\frac{4y}{x}} = 2^{\frac{5}{x}}$$

$$\frac{-4y}{x} = 5 \Longrightarrow -\frac{4}{5} = \frac{x}{y}$$

Answer: C

Q12: If Farhan leaves now and drive at 80km/h, he can be in Lahore in time for his appointment. On the other hand, if he eats first and leaves in half an hour, he will have to drive at 100 km/h to make his appointment. How far is he to Lahore?

A) 100km	√B) 200km
C) 250km	D) 150km

Solution:

$$d = 80t = 100(t - 0.5) \Longrightarrow 80t = 100t - 50 \Longrightarrow$$

$$100t - 80t = 50 \Longrightarrow 20t = 50 \Longrightarrow t = \frac{50}{20} = 2.5hrs$$

 $d = 80t = 80 \times 2.5 = 200 km$

Q13: Evaluate
$$\left(1-\frac{1}{3}-\frac{1}{1+\frac{1}{2}}\right)$$
; $\left(\frac{1}{3}-\frac{1}{1+\frac{1}{4}}\right)$
 \sqrt{A} 0 B) 1 C) $\frac{3}{4}$ D) $\frac{4}{3}$
Solution:
 $\left(1-\frac{1}{3}-\frac{1}{1+\frac{1}{2}}\right)$; $\left(\frac{1-\frac{1}{1+\frac{1}{2}}}{3-\frac{1}{1+\frac{1}{4}}}\right) = \left(1-\frac{1}{3}-\frac{2}{3}\right)$; $\left(\frac{1-\frac{2}{3}}{3-\frac{4}{5}}\right)$

$$\left(\frac{3-1-2}{3}\right) \div \left(\frac{\frac{1}{3}}{\frac{11}{5}}\right) = 0 \div \frac{5}{33} = 0$$

Answer: A

Q14: I think of a number, subtract 7 from it, divide the result by 4, and then add 13. If this gives a final result of 20, find the original number

$$\frac{x-7}{4} + 13 = 20 \Longrightarrow \frac{x-7}{4} = 7 \Longrightarrow$$

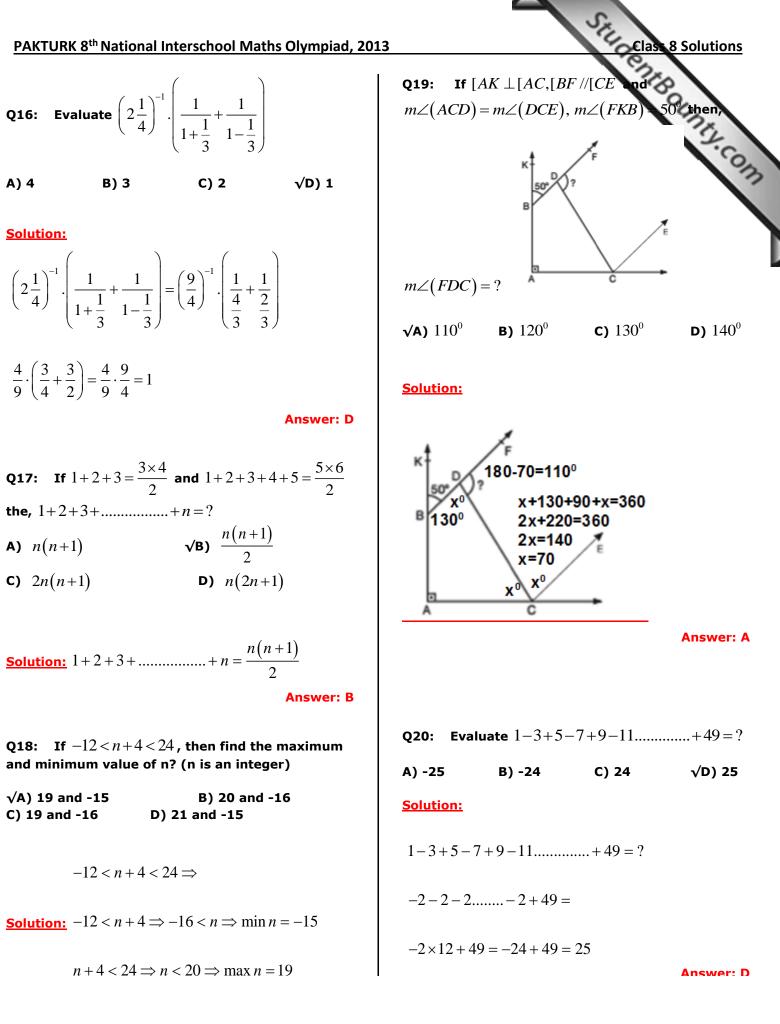
Solution:

$$x - 7 = 28 \Longrightarrow x = 35$$

Answer: C

Q15: A water tank can be filled by one pipe in 10 hours and it can be emptied by another pipe in 15 hours. If both pipes are open, how long will it take to fill the tank?

Solution: $\frac{1}{10} - \frac{1}{15} = \frac{3-2}{30} = \frac{1}{30} \Rightarrow 30hrs$



Q21: If $\frac{\sqrt{7}}{\sqrt{5}}$	$\frac{1}{2} = a$ then, which of the followings		
is the result of $\frac{\sqrt{7}+8}{\sqrt{5}+2}$ in terms of a			
A) $\frac{7}{a}$	B) $\frac{8}{a}$ C) $\frac{-49}{a}$ \sqrt{D}) $\frac{-57}{a}$		

Solution:

$$\frac{\sqrt{7}-8}{\sqrt{7}-8} \times \frac{\sqrt{7}+8}{\sqrt{5}+2} \times \frac{\sqrt{5}-2}{\sqrt{5}-2} = \frac{7-64}{\sqrt{7}-8} \times \frac{\sqrt{5}-2}{5-4}$$

$$\frac{-57}{1} \times \frac{\sqrt{5} - 2}{\sqrt{7} - 8} = -57 \times \frac{1}{a} = \frac{-57}{a}$$

Answer: D

Q22: Sibtain evaluates

$$\left(\frac{1}{x^2+y} + \frac{1}{x^2-y}\right) \cdot \frac{x^2y^2-y^3}{2xy}$$
 for $x = \frac{1}{5}$ and $y = \frac{1}{7}$

Which of the following expressions has the same

value when
$$x = \frac{1}{5}$$
 and $y = \frac{1}{7}$
 \sqrt{A}) $\frac{xy}{x^2 + y}$
B) $\frac{x}{x^2 - y}$
C) $\frac{y}{x + y}$
D) $\frac{2xy}{x - y}$

Solution:

$$\left(\frac{1}{x^2+y} + \frac{1}{x^2-y}\right) \cdot \frac{x^2y^2-y^3}{2xy} = \frac{x^2-y}{x^4-y^2} \cdot \frac{y^2(x^2-y)}{2xy}$$

$$\frac{\cancel{x}x^{\cancel{y}}}{(x^2+y)(x^2-y)} \times \frac{y^{\cancel{y}}(x^2-y)}{\cancel{x}} = \frac{xy}{x^2+y}$$

Answer: A

Q23: Information: The numbers which can be

Example: 1+2+3=6 or 1+2+3+4+

HBOUNKY.COM The numbers which are squares of nature numbers are called perfect squares. Which of the following numbers is neither a triangular nor a perfect square?

Example: 36 is square of 6

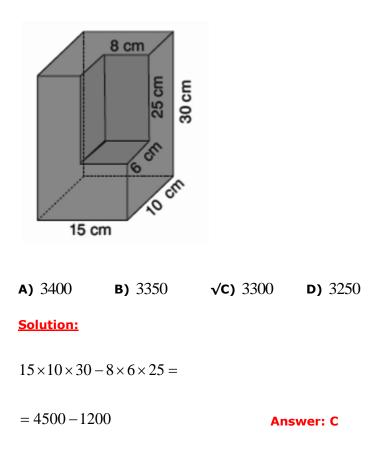
Solution:

A)
$$171 = \frac{18 \times 19}{2}$$

B) $300 = \frac{24 \times 25}{2}$
C) $289 = 17^2$
VD) 255

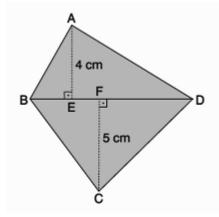
Answer: D

Q24: In the figure, a rectangular prism has been removed from a larger prism with dimensions 15 cm, 10 cm and 30 cm. Find the valume of the remaining solid in cubic centimeters



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Q25: Find the area of given figure if BD is 12 cm



A) 20 cm² B) 64cm² √C) 54cm² D) 56cm²

Solution:

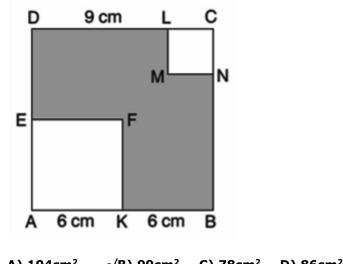
Area of
$$ABD = \frac{4 \times 12}{2} = 24 cm^2$$
,

Area of
$$BDC = \frac{5 \times 10^{\circ}}{12} = 30 cm^2$$
,

total area =
$$24cm^2 + 30cm^2 = 54cm^2$$
,

Answer: C

Q26: In the figure, ABCD, AKFE and LMNC are squares. Find the area of the shaded region



Solution:

THE Class & Solu. Area of $ABCD = 12 \times 12 = 144cm^2$,

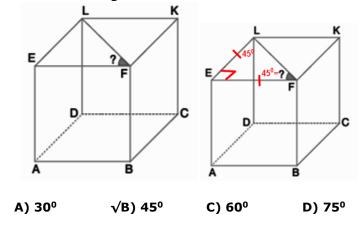
Area of $AKFE = 6 \times 6 = 36cm^2$,

Area of $LMNC = 3 \times 3 = 9cm^2$,

shaded area $=144 - 36 - 9 = 99cm^2$,

Answer: B

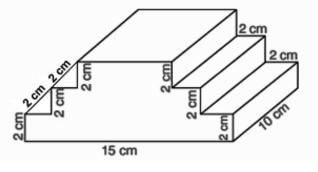
Q27: The figure shosw a cube. What is the measure of angle EFL?

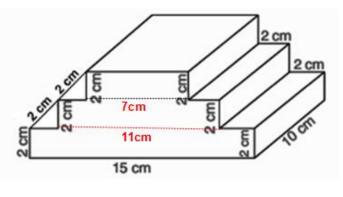


Solution:

Answer: B

Q28: Find the valume in cubic centimeters of the solid with the given dimensions.





√A) 660cm³ C) 700cm³ B) 680cm³ D) 720cm³

Solution:

 $V = 15 \times 2 \times 10 + 11 \times 2 \times 10 + 7 \times 2 \times 10$

 $=(15+11+7)\times 2\times 10=33\times 20=660cm^{3}$

Answer: A

Q29: What is the measurement of the angle between the hour-hand and the minute- hand at the time 05:20?

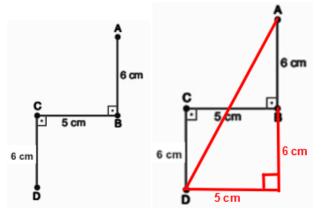
A) 36 [°]	√B) 40 ⁰	C) 44 ⁰	D) 48°

Solution:

Angle between 4 to 5 is 30° . If every 60 minutes it moves 30° then in 20 minutes it will move 10° . Total makes $30^{\circ}+10^{\circ}=40^{\circ}$.

Answer: B





Solution:

$$AD^2 = 5^2 + 12^2 = 25 + 144 = 169$$

$$AD^2 = 169 \Longrightarrow AD = 13cm$$

59 Class 8 Solu. 59 Answer: E

Q31: Simplify
$$\frac{2\left(1+\frac{1}{a}\right)}{1-\frac{1}{b}} \cdot \frac{b-1}{a+1} + 1$$

A)
$$\frac{2b}{a} - 1$$
 B) $\frac{2b}{a}$ **VC)** $1 + \frac{2b}{a}$ **D)** $\frac{a}{b}$

Solution:

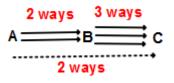
$$\frac{2\left(1+\frac{1}{a}\right)}{1-\frac{1}{b}}\cdot\frac{b-1}{a+1}+1=2\times\frac{a+1}{a}\times\frac{b}{b-1}\times\frac{b-1}{a+1}+1=\frac{2b}{a}+1$$

Answer: C

Q32: There are two different ways from the city A, to the city B. There are 3 different ways from the city B, to the city C. There are two different ways from the city A to the city C that are not passing through the city B. How many different ways are there from the city A to the cith C?

A) 6
$$\sqrt{B}$$
 8 C) 10 D) 12

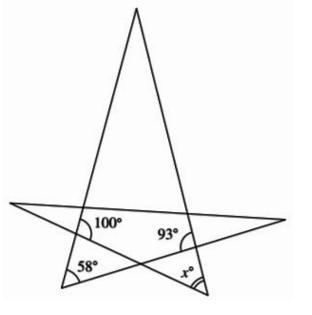
Solution:



A to C via B: 6 different ways A to C: 2 different ways Total A to C: 8 different ways

Answer: B

Q33: In the given figure, what is the value of angle x° ?

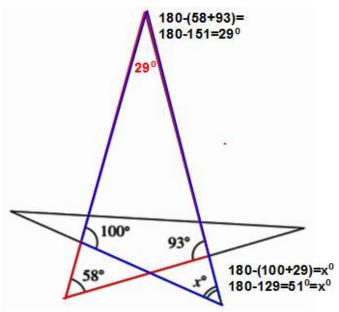


A) 49° \sqrt{B}) 51°

D) 47º

C) 41°

Solution:



Answer: B

Q34: The figure below shows 5 circular pools in a rectangular garden. The diameters of the circles are 6 m and 10 m and the side lengths of the garden are 20 m and 30 m. The rest of the garden is covered in grass. How much of the garden is

$$\sqrt{A}$$
) 417m²
C) 413m²
C) 413m²
C) 413m²
C) 413m²
C) 411m²
C) 411m²

Solution:

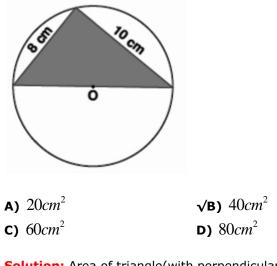
Area of Shaded Region=Area of Rectangle-(Area of 4 small circles+Area of 1 big circle)

$$= 20 \times 30 - (4 \times 3 \times 3^2 + 3 \times 5^2)$$

$$= 600 - (108 + 75) = 600 - 183 = 417 cm^2$$

Answer: A

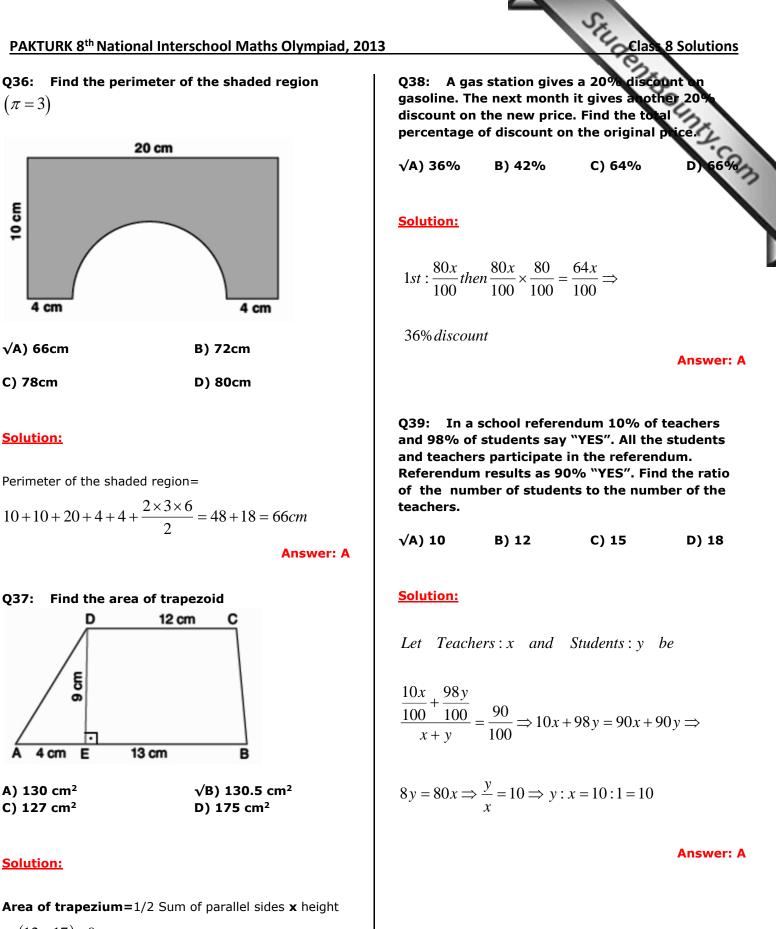
Q35: In the figure, O is the center of the circle. Find the area of the shaded region.



Solution: Area of triangle(with perpendicular sides)=

$$\frac{8 \times 10}{2} = \frac{80}{2} = 40 cm^2$$

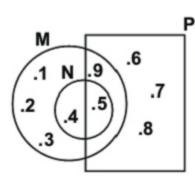
 $(\pi = 3)$



$$=\frac{(12+17)\times9}{2}=\frac{29\times9}{2}=\frac{261}{2}=130.5cm^2$$

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A) {1,2,3} √C) {1,2,3,4,9} B) {1,2,3,4}
D) {1,2,3,4,6,7,8,9}

Solution:

$$M \setminus (P \cap N) = \{1, 2, 3, 4, 5, 9\} \setminus \{5\} = \{1, 2, 3, 4, 9\}$$

Answer: C

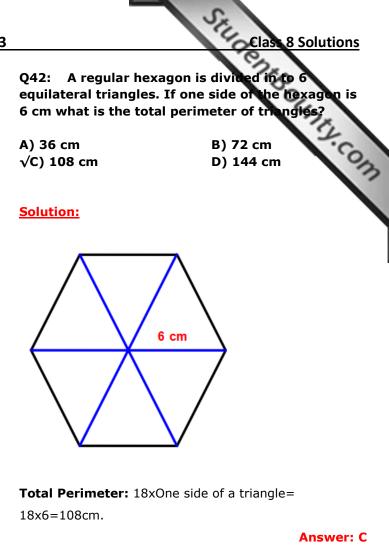
Q41: One of the students asks the age of Khwarizmi. His answer is : "When I was at your age you were 12 years old and when you are at my age, I will be 66 years old." Accordingly, what is the student's current age?

A) 18 B) 24 \sqrt{C} 30 D) 36

Solution:

	<u>Past</u>	<u>Present</u>	<u>Future</u>	
Student	12	x-k	x	
Khwarizmi	x-k	х	x+k=66	
x-k=12+m and x-k+m=x then m=k,				
x-k=12+m and x-k=12+k,				
x-2k=12 and x+k=66 solutions x=48 and k=18 then				
Student's current age=x-k=48-18=30				

Answer: C



Q43:
$$-2[3+5(-2-3)]-4(10-3)-(3-10)=?$$

A) -17 B) 1 C) 12 \sqrt{D} 23

Solution:

$$-2[3+5(-2-3)]-4(10-3)-(3-10) =$$
$$-2[3+5(-5)]-4(7)-(-7) =$$
$$-2[3-25]-28+7 = -2(-22)-21 =$$
$$44-21 = 23$$

Answer: D

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Q44:

$$\begin{pmatrix} 1+\frac{1}{4} \end{pmatrix} \times \begin{pmatrix} 1-\frac{1}{5} \end{pmatrix} \times \begin{pmatrix} 1+\frac{1}{6} \end{pmatrix} \times \begin{pmatrix} 1-\frac{1}{7} \end{pmatrix} \dots \times \begin{pmatrix} 1+\frac{1}{99} \end{pmatrix} \times \begin{pmatrix} 1-\frac{1}{100} \end{pmatrix} = 0$$

$$\textbf{A)} \quad \frac{1}{100^2} \qquad \textbf{B)} \quad \frac{1}{10^2} \qquad \textbf{C)} \quad \frac{1}{10^1} \qquad \sqrt{\textbf{D}} \quad \frac{1}{10^0}$$

Solution:

$$\left(1+\frac{1}{4}\right)\times\left(1-\frac{1}{5}\right)\times\left(1+\frac{1}{6}\right)\times\left(1-\frac{1}{7}\right)\dots\times\left(1+\frac{1}{99}\right)\times\left(1-\frac{1}{100}\right)=$$

$$\frac{5}{4} \times \frac{4}{5} \times \frac{7}{6} \times \frac{6}{7} \dots \times \frac{100}{99} \times \frac{1}{100} = \frac{1}{10^{\circ}}$$

Answer: D

Q45: Onder, Taner and Serhat are planning to go to a trip. They share the cost of the trip in the ratio 4:5:6 respectively. If half of Serhat`s share is 600 Rs, how much less is Onder going to pay than Taner?

A) Rs. 100	√B) Rs. 200	
C) Rs. 300	D) Rs. 400	

Solution:

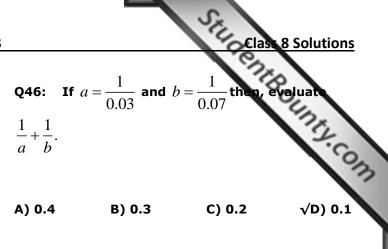
Serhat's share: 2x600=Rs.1200, Total share is:

Serhat's =
$$\frac{6Total}{15} = 1200 \implies Total = 15 \times 200 = Rs.3000$$

$$Onder's = \frac{4}{15} \times 3000 = Rs.800 \Longrightarrow$$

 $Taner's = \frac{5}{15} \times 3000 = Rs.1000 \Longrightarrow$

$$Taner's - Onder's = 1000 - 800 = Rs.200$$

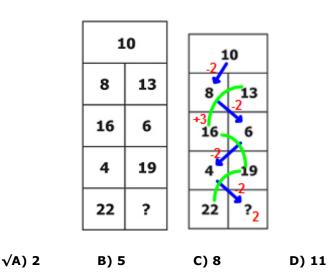


Solution:

$$\frac{1}{a} + \frac{1}{b} = \frac{1}{\frac{1}{0.03}} + \frac{1}{\frac{1}{0.07}} = 0.03 + 0.07 = 0.1$$

Answer: D

Q47: If the numbers in the figure are ordered with a rule then which number will come in place of question mark?



Solution:

Answer: A

