

# THE INSTITUTION OF ENGINEERS, SRI LANKA

PART I EXAMINATION – APRIL 2009

## 103 PROPERTIES & STRENGTH OF MATERIALS

Time Allowed: 3 hours

Answer **Five (5)** questions selecting at least two (02) from each of the two sections **A and B**.

**Use Separate answer books for each section.**

### SECTION A

- (1)
- a. Sketch the Fe-Fe<sub>3</sub>C equilibrium phase diagram. [10 marks]
  - b. Sketch and name the microstructures expected at room temperature in the following cases:
    - I. Fe + 0.02%C alloy slowly cooled from 950°C
    - II. Fe + 0.4%C alloy slowly cooled from 950°C
    - III. Fe + 0.8%C alloy slowly cooled from 900°C
    - IV. Fe + 0.4%C alloy rapidly quenched from 950°C [08 marks]
  - c. Calculate the relative proportions of the phases obtained in part b(II) above. [02 marks]
- 2)
- a. For a radioactive isotope, show that the product of radioactive decay constant ( $\lambda$ ) and the half-life (T) will be 0.69315. [04 marks]
  - b. Activity of a radioactive isotope falls to 25% of its original value in 50 days. How long would it take for the activity to fall to 5% of its original value? When will be the activity becomes zero? [08 marks]
  - c. Calculate the amount of energy released by 1kg of deuterium due to the fusion of deuterium nuclei to form He-3 nuclei. Relative atomic masses of deuterium, neutron and helium are 2.015, 1.009, and 3.017 respectively. Assume that destruction of 1g of mass produces  $931 \times 6.023 \times 10^{23}$  MeV of energy.  
Take  $1\text{eV} = 1.6 \times 10^{-19}$  J [06 marks]
  - d. State the major difference between *fissile isotopes* and *fertile isotopes*. [02 marks]

3)

- a. Sketch the unit cells of BCC and FCC crystal structures. [02 marks]
- b. Show the atomic arrangements of the planes having the closest packing in BCC and FCC lattices. [04 marks]
- c. An X-ray diffractometer recorder chart for an element which has a cubic structure (simple cubic, bcc or fcc) shows diffraction peaks at the angles of deviation of  $40^\circ$ ,  $46.5^\circ$ ,  $68^\circ$ ,  $82^\circ$ ,  $86^\circ$  and  $104^\circ$ . The wavelength of the X-ray is 0.15nm. Determine the crystal structure and lattice parameter of the element used. [14 marks]

4)

- a. Describe the tensile test. [06 marks]
- b. Sketch the tensile stress-strain diagram for pure copper and explain how you would determine the elastic modulus, yield strength, ductility and toughness of the material from the diagram. [06 marks]
- c. Give a detailed description of the mechanism of fatigue using an example of your choice. [08 marks]

SECTION B

(5) Figure Q.5 shows a beam ABCD of length  $L$ , with supports at B and C, positioned at a distance  $\alpha L$  from the ends of the beam. The beam is subjected to a uniformly distributed load of  $w$  per unit length.

- Calculate the reactions at B and C due to this load. [2 marks]
- Sketch a shear force and a bending moment diagram for the case  $\alpha = 0.25$ , indicating salient values. [6 marks]
- Show by adding dashed lines to your plots from (b) the effects of decreasing  $\alpha$  to 0.2, and the effect of increasing  $\alpha$  to 0.3. (Salient values are not required). [5 marks]
- Derive expressions for the bending moment in the beam as a function of  $x$  and  $\alpha$ :
  - for AB,  $0 \leq x \leq \alpha L$ ,  $0 \leq \alpha \leq 0.5$ ;
  - for BC,  $\alpha L \leq x \leq (1-\alpha)L$ ,  $0 \leq \alpha \leq 0.5$ . [4 marks]
- Show from your answers to (d) that the value of  $\alpha$  that minimises the maximum magnitude of the bending moment carried by the beam is  $\alpha = (\sqrt{2} - 1)/2$ . [3 marks]

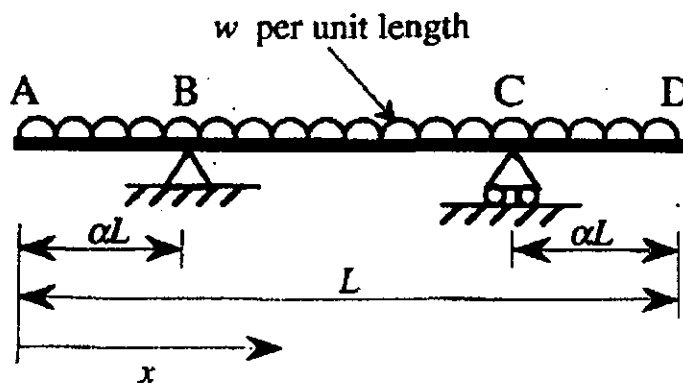
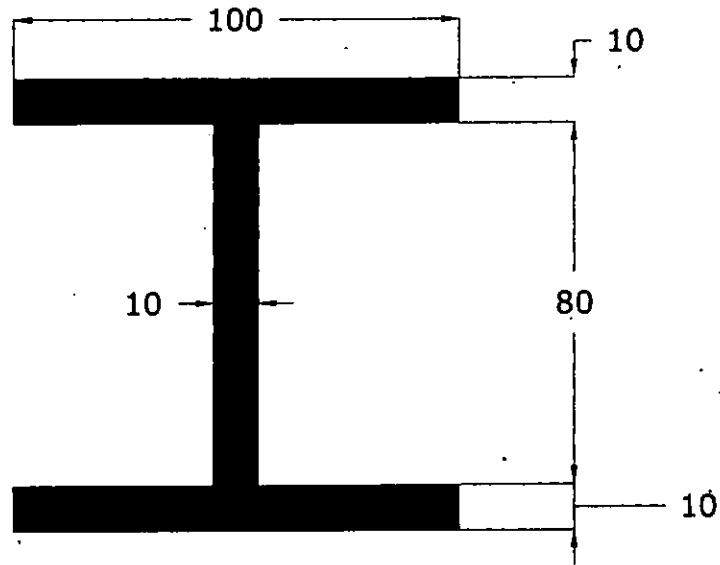


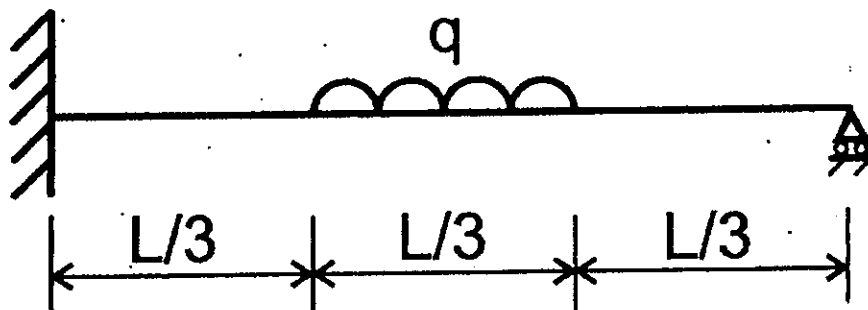
Figure Q.5

(6) Cross section of a steel I beam, which is simply supported over span of 5.0 m is shown in Figure Q.6. If the allowable stresses in tension and compression are limited to  $150 \text{ N/mm}^2$ , find the maximum weight of a point load that can be carried across the beam without exceeding the allowable stresses.



**Figure Q.6**  
(All dimensions are in millimetres)

(7) A propped cantilever, of length  $L$ , is loaded by a uniformly distributed load of intensity  $q$  kN/m over its central third, as shown in Figure Q.7. Show that the maximum deflection occurs at  $0.56L$  from the fixed end using Macaulay's method.



**Figure Q.7**

(8) An initially straight pin-ended strut is loaded by a force  $P$  applied at an eccentricity  $e$ , which represents a misalignment between the strut and the load it is designed to carry, as shown in Figure Q.8.

- Why a small error in the load position more important when dealing with struts and columns, and less important when dealing with beams loaded primarily in flexure? [4 marks]
- By considering a deflection of the strut,  $v$ , measured from the undeformed position, derive the governing differential equation for the deflection. [5 marks]
- Show that the solution of this differential equation takes the form

$$v = A \sin \alpha x + B \cos \alpha x + C$$

What are the coefficients  $A$ ,  $B$ ,  $C$  and  $\alpha$ ? [7 marks]

- A strut has an eccentricity  $e$  that is 1% of its length. If it is loaded by an axial force that is 50% of the Euler buckling load of the strut, determine the lateral displacement of the strut at its centre and hence determine its maximum bending moment. [4 marks]

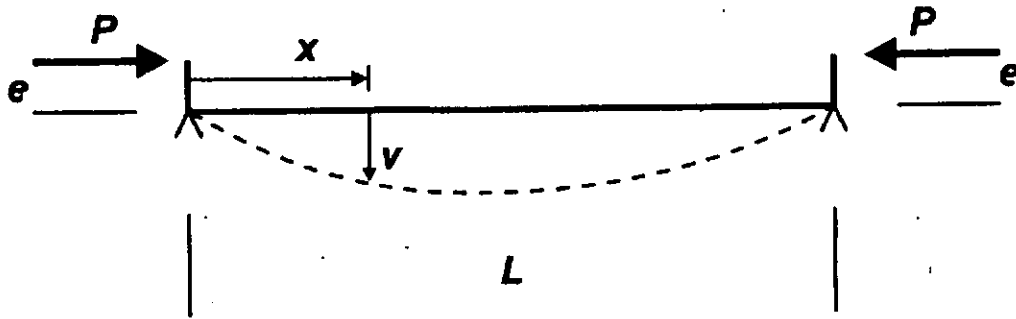


Figure Q.8