

THE INSTITUTION OF ENGINEERS, SRI LANKA
IESL ENGINEERING COURSE PART I EXAMINATION – 2009

104 ELECTROTECHNIQUES

This paper consists of ten questions. Answer **any six (6)** questions.
 All questions carry equal marks.
 Time allowed : 3 hours

Electric space constant	ϵ_0	$= 8.854 \times 10^{-12} \text{ Fm}^{-1}$
Magnetic space constant	μ_0	$= 4\pi \times 10^{-7} \text{ Hm}^{-1}$
Gravitational constant	G	$= 6.672 \times 10^{-11} \text{ Nm}^2\text{kg}^{-2}$
Gravitational acceleration	g	$= 9.81 \text{ ms}^{-2}$
Electron rest mass	m_e	$= 9.11 \times 10^{-31} \text{ kg}$
Electron charge	e	$= 1.602 \times 10^{-19} \text{ C}$

- Q1.** (i) State Coulomb's Law
- (ii) A thin charged rod of length L is placed on the x -axis, with one end at the origin. The charge per unit length, λ , is constant. Determine the force on a positive point charge q_0 , located at a position $x = a$, where
- a) $0 > a > L$ b) $a > L$ and c) $a \gg L$
- (iii) Calculate the force on a point charge of $5 \mu\text{C}$, where $L = 12 \text{ cm}$, $a = 8 \text{ cm}$, and $\lambda = 5 \mu\text{C/cm}$.

- Q2.** (i) Describe the behaviour of capacitors connected in series and parallel.
- (ii) A $1 \mu\text{F}$ capacitor and a $2 \mu\text{F}$ are connected in series across a 1200 V supply line.
- a) Find the charge on each capacitor.
 b) Find the voltage across each capacitor.

The charged capacitors are now disconnected from the supply line and each other, and re-connected to each other so that the terminals of like charges are together.

- c) Find the final charge on each capacitor.
 d) Find the change in electric energy of the system.
- Q3.** (i) State the condition for two elements to be connected in
- a) series; b) parallel; in an electronic circuit.

- (ii) Twelve identical $1\ \Omega$ resistors are connected into a circuit as shown in Figure Q3.

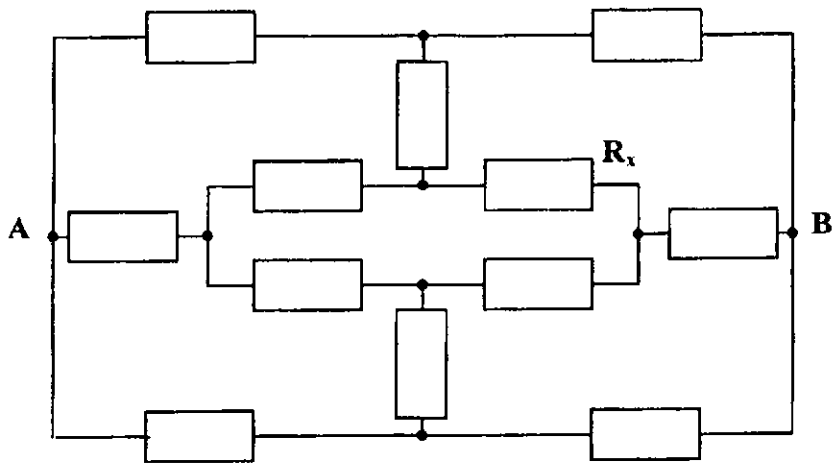


Figure Q3

Calculate the equivalent resistance of this circuit, when measured between points A and B. Write all assumptions you make.

- (iii) What will be the current through the resistor R_x when a source of 36 V is connected across AB?

Q4. (i) Describe briefly the two Kirchhoff's Laws of electric circuits.

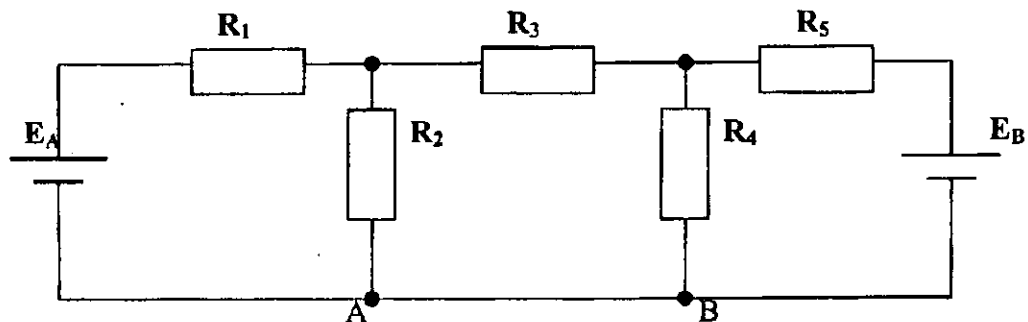


Figure Q4

- (ii) Calculate the value of E_B in the circuit of Figure Q4, given that $R_1 = 12\ \text{k}\Omega$; $R_2 = 6\ \text{k}\Omega$; $R_3 = 2\ \text{k}\Omega$; $R_4 = R_5 = 10\ \text{k}\Omega$ and $E_A = 12\text{V}$, no current flow between points A and B.

- Q5. (i) Describe Ampère's Law.
- (ii) A coaxial cable consists of an inner solid conductor of radius a , and an outer concentric (pipe like) conductor of inner radius b_i and outer radius b_o . The inner conductor carries a current I in the opposite direction to the current flow of the outer conductor, which also carries the same I amount of current. Assume that the current density within a conductor is uniform. Calculate the magnetic field for the regions
 a) $r < a$; b) $a < r < b_i$; c) $b_i < r < b_o$; and d) $b_o < r$

- (iii) For $I = 10 \text{ A}$, $a = 10 \text{ mm}$, $b_i = 16 \text{ mm}$ and $b_o = 20 \text{ mm}$, calculate magnetic field density at
 a) $r = 5 \text{ mm}$ and b) $r = 18 \text{ mm}$

- Q6.** An electron is projected into a uniform electric field of 5000 N/C , directed vertically upward. The initial velocity of the electron is 10^7 m/s , at an angle of 30° above the horizontal.
- a) Find the maximum distance the electron rises vertically above the initial elevation.
 b) After what horizontal distance does the electron return to the original elevation?

- Q7.** (i) Describe briefly the behaviour of
 a) a capacitor
 b) an inductor in a sinusoidal circuit.

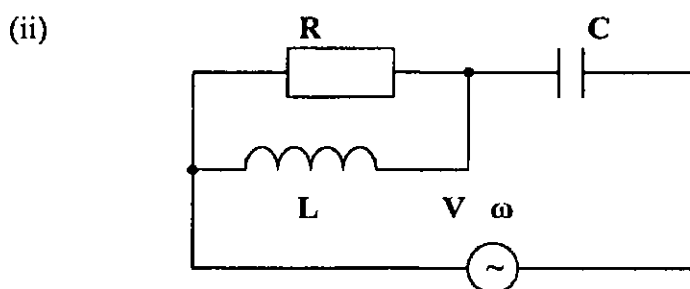


Figure Q7

In the above circuit rms value of V is 10 V . Given $R = 300 \Omega$, $L = 400 \text{ mH}$, $C = 2.5 \mu\text{F}$ and $\omega = 1000 \text{ rad/s}$;

- a) Calculate the currents through all components.
 b) Draw the phasor diagram to show all currents and voltages of the circuit.
- Q8.** (i) Describe the characteristic of a resonant circuit.

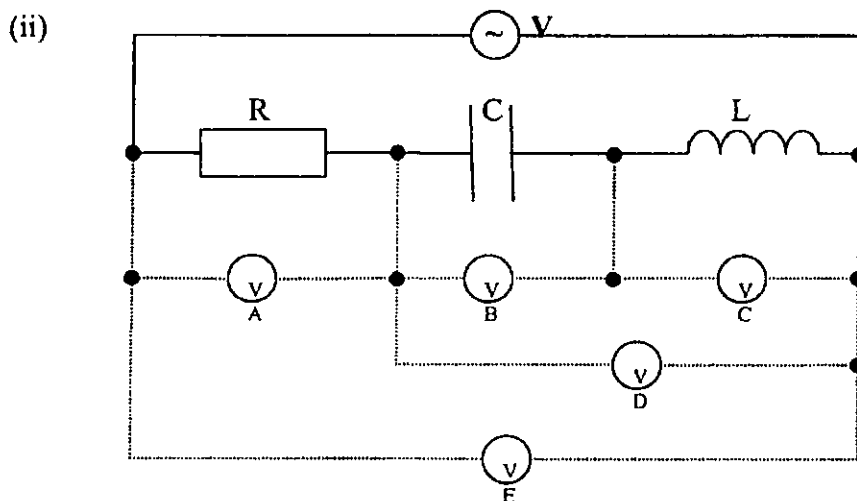


Figure Q8

The circuit in figure Q8 is tuned to resonance, and five AC voltmeters V_A - V_E are connected to it as shown. Give the reading of each voltmeter, if $R=300 \Omega$, $L=400 \text{ mH}$, $C=3 \mu\text{F}$, $v(t)=12 \sin \omega_0 t \text{ V}$, where ω_0 is the angular velocity at resonance.

- Q9. (i) Real ammeters and voltmeters may present problems when measuring very large, or very small loads. Show, and describe briefly how best to connect an ammeter and a voltmeter to accurately measure
- Voltage across a very large load
 - Current through a very small load.

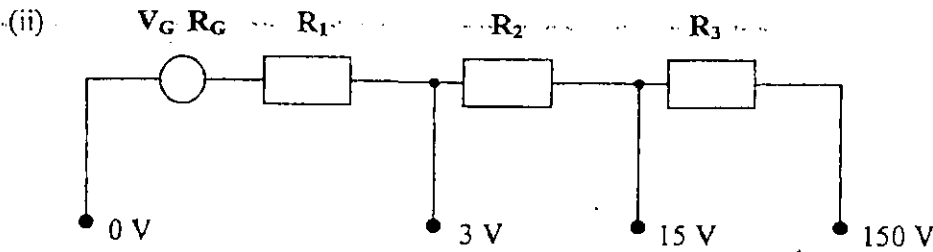


Figure Q9

In Figure Q9 the internal wiring of a 3-scale moving-coil voltmeter is shown with scales of +3 V, +15 V and +150 V. The resistance of the moving coil $R_G = 15 \Omega$, and a current of 1 mA causes it to deflect full-scale. Find the values of R_1 , R_2 , and R_3 .

- Q10. (i) Devise a 2-input NAND gate, using only the minimum number of 2-input NOR gates.
- (ii) The Boolean function F is defined as
- $$F = \overline{ABCD} + \overline{A}BCD + \overline{AB}C\overline{D} + \overline{A}B\overline{C}D + \overline{A}BC\overline{D} + \overline{A}B\overline{C}D + \overline{A}BCD$$
- Construct the truth table for function F .
 - Simplify function F using Boolean Algebra.
 - Find a simple equivalent expression for (original) function F using a suitable Karnaugh-map.