

Code: AE73

Subject: INFORMATION THEORY & COMMUNICATIONS

AMIETE - ET

Time: 3 Hours

JUNE 2013

Max. Marks: 100

PLEASE WRITE YOUR ROLL NO. AT THE SPACE PROVIDED ON EACH PAGE IMMEDIATELY AFTER RECEIVING THE QUESTION PAPER.

NOTE: There are 9 Questions in all.

- Question 1 is compulsory and carries 20 marks. Answer to Q.1 must be written in the space provided for it in the answer book supplied and nowhere else.
- The answer sheet for the Q.1 will be collected by the invigilator after 45 minutes of the commencement of the examination.
- Out of the remaining EIGHT Questions answer any FIVE Questions. Each question carries 16 marks.
- Any required data not explicitly given, may be suitably assumed and stated.

Q.1 Choose the correct or the best alternative in the following: (2×10)

a. A probability density function is given by $P(x) = ke^{-x^2/2}$, $-\infty < x < \infty$. The value of k is

(A) $\frac{1}{\sqrt{2\pi}}$

(B) $\sqrt{\frac{2}{\pi}}$

(C) $\frac{1}{2\sqrt{\pi}}$

(D) $\frac{1}{\pi\sqrt{2}}$

b. The spectral density of real valued random process has

(A) an even symmetry

(B) an odd symmetry

(C) a conjugate symmetry

(D) no symmetry

c. The imaginary channel rejection in a superheterodyne receiver comes from

(A) IF stages only

(B) RF stages only

(C) Detector and RF stages

(D) Detector, RF & IF stages

d. If Y and Z are random variables obtained by sampling X(t) at $t = 2$ and $t = 4$ respectively and let $W = Y - Z$. The variance of W is

(A) 13.36

(B) 9.36

(C) 2.64

(D) 8.00

e. Auto correlation function of a random process is

(A) $R(t_1, t_2) = E(XY) = \iint xy p(x, y) dx dy$

(B) $E(XY) = \iint x^2 y^2 dx dy$

(C) $R(t_1, t_2) = \iint x^2 y^2 dx dy$

(D) None of these

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- f. The differential entropy of N_k as
- (A) $h(N_k) = \frac{1}{2} \log_2 [2\pi e(P + \sigma^2)]$ (B) $h(N_k) = \frac{1}{2} \log_2 (2\pi e\sigma^2)$
 (C) Both (A) & (B) (D) None of these
- g. In a SEC Hamming code, the number of message bits in a block is 26. The number of check bits in the block would be
- (A) 3 (B) 4
 (C) 5 (D) 7
- h. Maximum-Length codes are generated by polynomials of the form
- (A) $g(D) = h(D) \cdot (1 + D^n)$ (B) $g(D) = \frac{h(D)}{(1 + D^n)}$
 (C) $g(D) = \frac{1 + D^n}{h(D)}$ (D) None of these
- i. If the data unit is 111111 and divisor is 1010, then the dividend at the transmitter is
- (A) 1111111000 (B) 1111110000
 (C) 111111 (D) 111111000
- j. A source generates 4 messages. The entropy of source will be maximum when
- (A) All probabilities are equal
 (B) One of probabilities equal to 1 and others are zero
 (C) The probabilities are $\frac{1}{2}$, $\frac{1}{4}$ and $\frac{1}{2}$
 (D) Two probabilities are $\frac{1}{2}$ and others are zero

Answer any FIVE Questions out of EIGHT Questions.
Each question carries 16 marks.

- Q.2** a. Define the following terms:
- (i) Joint probability (ii) Conditional probability
 (iii) Probability mass function (iv) Statistical independence (8)
- b. The input of a binary communication systems denoted by random variable X, takes on one of the two values 0 or 1 with probabilities $\frac{3}{4}$ and $\frac{1}{4}$ respectively. Due to error caused by noise in the system, the output Y differs

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from the input X occasionally. The behaviour of the communication system is modelled by the conditional probabilities.

$$P(Y = 1|X = 1) = \frac{3}{4} \quad \& \quad P(Y = 0|X = 0) = \frac{7}{8}$$

Find

- (i) $P(Y = 1)$ and $P(Y=0)$
 (ii) $P(X = 1|Y = 1)$ (8)

Q.3 a. Explain the three models for continuous random variables. (8)

b. X and Y are two independent random variables, each having a Gaussian probability distribution function with a mean of zero and a variance of one.

- (i) Find $P(|X| > 3)$ using $Q(4)$ and also obtain an upper bound. Given that $Q(0) = \frac{1}{2}, Q(3) = 0.0013$.

- (ii) Find the joint PDF of $Z = \sqrt{x^2 + y^2}$ & $\omega = \tan^{-1}\left(\frac{y}{x}\right)$
 (iii) Find $P(z > 3)$ (8)

Q.4 a. Explain Markoff statistical model for information sources. (8)

b. A discrete source emits one of five symbols once every millisecond. The symbol probabilities are $\frac{1}{2}, \frac{1}{4}, \frac{1}{8}, \frac{1}{16}$ and $\frac{1}{16}$ respectively. Find the source entropy and information rate. (8)

Q.5 a. Explain briefly Huffman coding and prefix coding. (8)

b. A source produces one of four possible symbols during each interval having probabilities $P(x_1) = \frac{1}{2}, P(x_2) = \frac{1}{4}, P(x_3) = P(x_4) = \frac{1}{8}$. Obtain the information contents of each of these symbols. (8)

Q.6 a. Explain Discrete Memoryless channel. (8)

b. A discrete memoryless source X has four symbols x_1, x_2, x_3, x_4 with probabilities $P(x_1) = 0.4, P(x_2) = 0.3, P(x_3) = 0.2, P(x_4) = 0.1$
 (i) Calculate $H(X)$
 (ii) Find the amount of information contained in the message $x_1x_2x_1x_3$ and $x_4x_3x_3x_2$. (8)

Q.7 a. Explain the following terms:
 (i) Mutual information
 (ii) Channel capacity (8)

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b. Explain differential entropy and mutual information for continuous ensemble. (8)

Q.8 a. What is linear block code? Explain the steps for determination of all code words for a linear block code. (8)

b. The generator matrix for a (6, 3) block code is given as

$$G = \left[\begin{array}{ccc|ccc} 1 & 0 & 0 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 1 & 1 & 0 \end{array} \right]$$

Find all code vectors of this code. (8)

Q.9 a. Explain cyclic codes. Give their advantages and disadvantages. (8)

b. Obtain the convolutional coded output for the message '1100101'. The convolutional encoder is shown in Fig.1 (8)

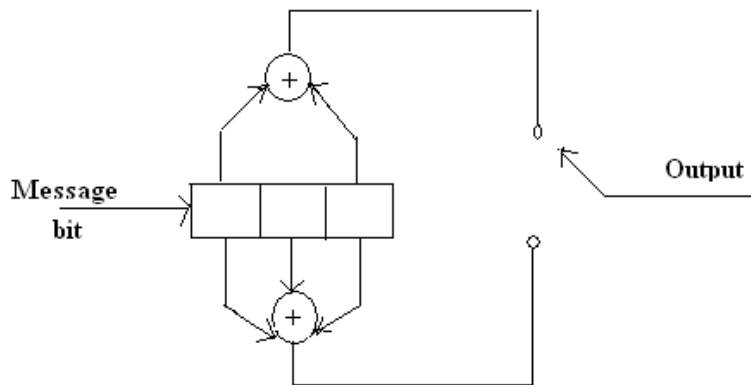


Fig.1