StudentBounty.com ROLL NO. Subject: MATHEMATICS Code: AE01/AC01/AT01 AMIETE - ET/CS/IT (OLD SCHEME) **JUNE 2012** Time: 3 Hours PLEASE WRITE YOUR ROLL NO. AT THE SPACE PROVIDED ON EACH PAGE IMMEDIATELY AFTER RECEIVING THE QUESTION PAPER. NOTE: There are 9 Questions in all. • Question 1 is compulsory and carries 20 marks. Answer to Q.1 must be written in the space provided for it in the answer book supplied and nowhere else. • The answer sheet for the Q.1 will be collected by the invigilator after 45 Minutes of the commencement of the examination. • Out of the remaining EIGHT Questions answer any FIVE Questions. Each question carries 16 marks. • Any required data not explicitly given, may be suitably assumed and stated. (2×10) Q.1 Choose the correct or the best alternative in the following: $\lim_{(x,y)\to(0,0)}\frac{x}{\sqrt{x^2+y^2}}$ is equal to a. **(A)** 0 **(B)** 1 **(C)** ∞ (D) does not exist b. If $u = \frac{y^3 - x^3}{v^2 + x^2}$, then $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y}$ is equal to (A) x **(B)** y (**C**) u (D) none of these The value of the integral $\iint dxdy$ over the triangle with vertices (0,0), (2, 0) c. (0,2) is **(A)** 1 **(B)** 2 (**D**) none of these **(C)** 3 d. $(x^3 + y)dx + (ax + by^3)dy = 0$ is exact if (A) a = 1**(B)** b = 2(C) a = 2, b = 3(**D**) None of these e. The general solution of $\frac{d^2y}{dx^2} - 2\frac{dy}{dx} - 3y = e^x$ is (A) $y = c_1 e^{-x} + c_2 e^{-3x} - \frac{1}{4} e^x$ (B) $y = c_1 e^{-x} + c_2 e^{3x} - \frac{1}{4} e^x$ (C) $y = c_1 e^{-x} + c_2 e^{-3x} + \frac{1}{4} e^x$ (D) $y = c_1 e^{-x} + c_2 e^{3x} + \frac{1}{4} e^x$

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Each Question carries 16 marks.

Q.2 a. If u = f(x, y) and x and y are functions of t, show that $\frac{du}{dt} = \frac{\partial u}{\partial x}\frac{dx}{dt} + \frac{\partial u}{\partial y}\frac{dy}{dt}$ (8)

b. If
$$u = x^{2} \tan^{-1}\left(\frac{y}{x}\right) - y^{2} \tan^{-1}\left(\frac{x}{y}\right), x > 0, y > 0$$
, evaluate

$$x^{2} \frac{\partial^{2} u}{\partial x^{2}} + 2xy \frac{\partial^{2} u}{\partial x \partial y} + y^{2} \frac{\partial^{2} u}{\partial y^{2}}$$
(8)

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StudentBounty.com a. Obtain Taylor's series expansion of $f(x, y) = \tan^{-1} \frac{y}{y}$ in powers of (x Q.3 and (y-1) upto second degree terms. b. Change the order of integration and then evaluate $\int_{-\infty}^{1} \int_{-\infty}^{y^{1/3}} e^{x^{2}} dx dy$ (2+6)a. Find the volume of the solid which is bounded by the cylinder $x^2 + y^2 = 1$ **Q.4** and the planes y + z = 1 and z = 0. (8) b. Solve the differential equation $xdx + ydy + 2(x^2 + y^2)dy = 0$ (8) a. Use method of variation of parameters to solve $\frac{d^2y}{dx^2} + 6\frac{dy}{dx} + 9y = \frac{e^{-3x}}{x}$ (8) Q.5 b. Solve the differential equation $\frac{d^2y}{dx^2} + 4y = x^2 + \cos 2x$ (8) a. Solve the differential equation $x^3 \frac{d^3y}{dx^3} + 5x^2 \frac{d^2y}{dx^2} + 5x \frac{dy}{dx} + y = x^2 + \log x$ (8) Q.6 b. If A is a non-singular matrix and if $I + A + A^2 + A^3 + \dots + A^n = 0$. Show that $A^{-1} = A^n$. (8) a. Use elementary row transformations to find inverse of $\begin{vmatrix} 1 & 1 & 1 \\ 1 & 2 & 3 \\ 1 & 3 & 4 \end{vmatrix}$ **0.7** (8) b. If the system of equations x + ay + az = 0, bx + y + bz = 0, cx + cy + z = 0where a,b,c are non-zero and non-unity, has a non-trivial solution, show that $\frac{a}{1-a} + \frac{b}{1-b} + \frac{c}{1-c} = -1$ (8) a. Find eigen values and eigen vectors of $\begin{vmatrix} 1 & 0 & 0 \\ 0 & 2 & 1 \\ 2 & 0 & 3 \end{vmatrix}$ **Q.8** (8)

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