

Time: 3 Hours

**DECEMBER 2012**

Max. Marks: 100

**PLEASE WRITE YOUR ROLL NO. AT THE SPACE PROVIDED ON EACH PAGE IMMEDIATELY AFTER RECEIVING THE QUESTION PAPER.**

**NOTE: There are 9 Questions in all.**

- Question 1 is compulsory and carries 20 marks. Answer to Q.1 must be written in the space provided for it in the answer book supplied and nowhere else.
- The answer sheet for the Q.1 will be collected by the invigilator after 45 minutes of the commencement of the examination.
- Out of the remaining EIGHT Questions answer any FIVE Questions. Each question carries 16 marks.
- Any required data not explicitly given, may be suitably assumed and stated.

**Q.1 Choose the correct or the best alternative in the following: (2×10)**

a. Down sampling by Lowpass filtering followed by compression is termed as

- (A) Interpolation (B) Aliasing  
(C) Decimation (D) None of these

b. The relationship between the quantized signal level and the full scale level of the A/D converter

- (A)  $\Delta = (X_m) / 2^B$  (B)  $\Delta = (2 X_m) / 2^B$   
(C)  $\Delta = (X_m) / 2^{B+1}$  (D)  $\Delta = (4 X_m) / 2^B$

c. Canonical form of structure is

- (A) Direct Form I (B) Direct Form II  
(C) Both (A) & (B) (D) None of these

d. If the continuous time system has poles only in the left half of the s-plane then the discrete time filter must have poles \_\_\_\_\_

- (A) Outside the unit circle only (B) Inside the unit circle only  
(C) Anywhere on z plane (D)  $2 < |Z| < 3$

e. The DFT values are equal to samples of Z transform and are at equally spaced points \_\_\_\_\_

- (A) Outside the unit circle (B) Inside the unit circle  
(C) On the unit circle (D) On entire z plane

f.  $W_N^{N/2}$  is equal to

- (A) 1 (B)  $j\omega$   
(C)  $-j\omega$  (D) -1

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Subject: DIGITAL SIGNAL PROCESSING

- g. Since Z Transform are analytic functions inside their ROC it means that
- (A) They have well defined derivative at every point inside the ROC
  - (B) Z - Transform and all its derivatives are continuous functions within ROC
  - (C) Both (A) & (B)
  - (D) None of these
- h. Relationships between real and imaginary parts of Z - Transform on a closed contour within ROC is referred to as \_\_\_\_\_
- (A) Poisson's formula in mathematical literature
  - (B) Hilbert Transform relations in system theory
  - (C) None of these
  - (D) Both (A) & (B)
- i. Effect of windowing on a signal's spectrum can be.
- (A) Reduced Resolution
  - (B) Leakage
  - (C) Both (A) & (B)
  - (D) None of these
- j. Out of all the windows available, the one which has the narrowest mainlobe for a given length is
- (A) Kaiser window
  - (B) Rectangular window
  - (C) Hamming window
  - (D) Hanning window

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**Answer any FIVE Questions out of EIGHT Questions.**  
**Each question carries 16 marks.**

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- Q.2** a. Explain discrete time processing of continuous time signals. (8)
- b. Derive the Frequency domain relationship between the input and output of an ideal Continuous to Discrete (C/D) Converter and assist it with spectrum diagrams. (8)
- Q.3** a. Consider the LTI system with input  $x[n]$  and output  $y[n]$  are related through the difference equation.
- $$y[n] + \frac{1}{4} y[n-1] = x[n] + \frac{1}{2} x[n-1]$$
- (i) Find the system function and its ROC (4)
  - (ii) Draw its pole-zero plot (2)
  - (iii) Comment on the causality and stability of this system (2)
- b. Explain Allpass systems. Obtain its frequency response and discuss the applications of Allpass system. (8)

**Q.4** a. (i) Obtain the direct form I and direct form II Realization of the system.

$$H(z) = \frac{(1 + 2z^{-1} + z^{-2})}{(1 - 0.75z^{-1} + 0.125z^{-2})} \quad (4)$$

(ii) Obtain the Linear phase Realization of system given by (4)

$$H(z) = \sum_{n=0}^5 z^{-n}$$

b. Explain Transposition. Give the transposed flow graph of (8)

$$H(z) = \frac{1}{(1 - az^{-1})}$$

**Q.5** a. Explain the design of optimum approximation of FIR filters. (8)

b. Differentiate between:

(i) IIR and FIR Filters

(ii) Butterworth filter and Chebyshev filter (8)

**Q.6** a. Compute the 4 point DFT of the sequence  $x[n] = \{1, j, -1, -j\}$ . (6)

b. Prove the statement “Circular Convolution is Linear Convolution with Aliasing” and obtain the Linear convolution of  $x_1(n) = \{1, 2, 3, 4\}$  and  $x_2(n) = \{1, -1, 1, -1\}$  using circular convolution. (10)

**Q.7** a. Explain DIF- FFT Algorithm using signal flow graphs for  $N=8$ . Compare its computational complexity with DFT. (8)

b. Write a short note on implementation of DFT using Convolution with the help of one example. (8)

**Q.8** a. Explain the processing steps in discrete time Fourier Analysis of a continuous time signal. (8)

b. Elaborate on the Time dependent Fourier Analysis of Non-stationary signals. (8)

**Q.9** a. Explain Hilbert Transform relationships mentioning how it eliminates the constraints on the Fourier Transform. (8)

b. Give the relationship between magnitude and phase of the Fourier transform of a sequence. (8)