Diplete – Et/CS (NEW SCHEME) – Code: DE51 / DC5

## Subject: ENGINEERING MATHEMATICS - I

Time: 3 Hours

# DECEMBER 2011

1 / DC5 Max. Marks: 100

 $(2 \times 10)$ 

**ROLL NO.** 

### **NOTE: There are 9 Questions in all.**

- Please write your Roll No. at the space provided on each page immediately after receiving the Question Paper.
- Question 1 is compulsory and carries 20 marks. Answer to Q.1 must be written in the space provided for it in the answer book supplied and nowhere else.
- The answer sheet for the Q.1 will be collected by the invigilator after 45 Minutes of the commencement of the examination.
- Out of the remaining EIGHT Questions answer any FIVE Questions. Each question carries 16 marks.
- Any required data not explicitly given, may be suitably assumed and stated.

## Q.1 Choose the correct or the best alternative in the following:

a.  $\ell t \frac{\sin 5x + 2x}{3x + \sin 3x}$  is: (A)  $\frac{7}{6}$  (B)  $\frac{6}{7}$ (C)  $\frac{5}{6}$  (D)  $\frac{6}{5}$ 

b. If 
$$y = \frac{x^3 \cos x}{\sin x}$$
, then  $\frac{dy}{dx}$  is  
(A)  $x^3 \csc^2 x + 3x^2 \cot x$  (B)  
(C)  $-x^3 \csc^2 x - 3x^2 \cot x$  (D)

(B) 
$$3x^3 \csc^2 x - x^2 \cot x$$
  
(D)  $-x^3 \csc^2 x + 3x^2 \cot x$ 

c. 
$$\int \frac{x^2}{a^6 - x^6} dx \text{ is}$$
  
(A) 
$$\frac{1}{6a^3} \log \left| \frac{a^3 + x^3}{x^3 - a^3} \right| + C$$
  
(B) 
$$\frac{1}{6a^3} \log \left| \frac{a^3 + x^3}{a^3 - x^3} \right| + C$$
  
(C) 
$$\frac{1}{6a^3} \log \left| \frac{a^3 - x^3}{a^3 + x^3} \right| + C$$
  
(D) 
$$\frac{1}{6a^3} \left| \frac{x^3 - a^3}{x^3 + a^3} \right| + C$$

d. If 
$$X + Y = \begin{bmatrix} 7 & 0 \\ 2 & 5 \end{bmatrix}$$
 and  $X - Y = \begin{bmatrix} 3 & 0 \\ 0 & 3 \end{bmatrix}$ , then X & Y is  
(A)  $X = \begin{bmatrix} 5 & 0 \\ 1 & 4 \end{bmatrix}, Y = \begin{bmatrix} 2 & 0 \\ 1 & 1 \end{bmatrix}$ 
(B)  $X = \begin{bmatrix} 5 & 1 \\ 4 & 0 \end{bmatrix}, Y = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$   
(C)  $X = \begin{bmatrix} 0 & 5 \\ 1 & 4 \end{bmatrix}, Y = \begin{bmatrix} 0 & 2 \\ 1 & 1 \end{bmatrix}$ 
(D)  $X = \begin{bmatrix} 4 & 1 \\ 0 & 5 \end{bmatrix}, Y = \begin{bmatrix} 1 & 0 \\ 2 & 1 \end{bmatrix}$ 

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StudentBounty.com  $\omega^2$  $\omega \omega^2$ 1 e. If  $\Delta = \begin{bmatrix} 1 \\ \omega \\ \omega^2 \end{bmatrix}$ 1 and  $\omega$  is a cube root of unity, then the value of  $\Delta$  is 1 ω ( ) 1

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$$\begin{array}{c} (A) & 1 \\ (C) & 0 \\ \end{array} \tag{B} 3 \\ (D) 2 \\ \end{array}$$

f. The coefficient of  $x^5$  in the expansion of  $\left(x + \frac{1}{x^3}\right)^{17}$  is

g. The solution of the differential equation  $\frac{dy}{dx} = e^{y+x} + e^{y-x}$  is

$(\mathbf{A}) \ \mathbf{y} = \mathbf{e}^{\mathbf{x}} \left( \mathbf{x} + 1 \right)$	<b>(B)</b> $y = e^{x}(x+1)+1$
(C) $y = e^{x}(x-1)+1$	( <b>D</b> ) none of these

h. If  $A + B = 45^{\circ}$ , then the value of  $(\cot A - 1)(\cot B - 1)$  is

( <b>A</b> ) 1	<b>(B)</b> -2
( <b>C</b> ) 2	( <b>D</b> ) -1

i. The area of the quadrilateral whose vertices, taken in order, are (1,1), (3,4), (5,-2) & (4,-7) is

(A) 
$$\frac{43}{2}$$
 sq.units  
(B)  $\frac{41}{2}$  sq.units  
(C)  $\frac{45}{2}$  sq.units  
(D)  $\frac{47}{2}$  sq.units

j. Three consecutive vertices of a parallelogram ABCD are A(3,0), B(5,2), C(-2,6). Then the fourth vertex D is

(A) $(4,-4)$	<b>(B)</b> $(4,4)$
(C) (3,-4)	<b>(D)</b> $(-4,4)$

### Answer any FIVE Questions out of EIGHT Questions. Each question carries 16 marks.

Q.2	a.	If $y = x^{(x^x)}$ , then find $\frac{dy}{dx}$	(8)
	b.	Find the equations of the tangent and the normal to the curve $(at^2, 2at)$ .	$y^2 = 4ax$ at (8)
Q.3	a.	$\int e^{2x} \sin 5x dx$	(8)
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b. 
$$\int_{1}^{3} \frac{1}{(x+1)(x+2)(x+3)} dx$$

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**B**. 
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b. Whether the system is consistent or inconsistent also find the solution, by Cramer's Rule, if exists x - y + 3z = 6

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$$x + 3y - 3z = -4$$
  
5x + 3y + 3z = 10 (8)

**Q.5** a. Solve 
$$(x^2 - y^2)dx = 2xydy$$
 (8)

b. Solve 
$$(1 + y^2)dx = (\tan^{-1} y - x)dy$$
 (8)

a. Show that the middle term in the expansion of  $(1+x)^{2n}$ is 0.6  $\frac{1.3.5....(2n-1)}{n!}2^{n}.x^{n}$ (8)

b. Find four numbers in A.P. whose sum is 20 and the sum of whose squares is 120. (8)

- Q.7 a. If A, B, C are the angles of a triangle, then prove that :  $\sin 2A + \sin 2B + \sin 2C = 4 \sin A \sin B \sin C$ (8)
  - b. Prove that  $\sin^2 A + \sin^2 (60^\circ + A) + \sin^2 (60^\circ - A) = \frac{3}{2}$ (8)

**Q.8** a. Find the equation of a straight line passing through the point (3, 4) and inclined to positive direction of x-axis at an angle of  $\frac{3\pi}{4}$ . Find also the coordinates of two points on it, on opposite side of (3, 4) and at a distance of  $\sqrt{2}$ from it. (8)

- b. Find the distance between the lines 9x + 40y - 20 = 0 and 9x + 40y + 21 = 0(8)
- **Q.9** a. Find the equation of the circle of radius 5 whose centre lies on y- axis passes through (3, 2). (8)

b. Find the vertex, focus and directrix of the parabola  $4y^2 + 12x - 12y + 39 = 0$ (8)

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