

Code: AE07 Subject: NUMERICAL ANALYSIS & COMPUTER PROGRAMMING

- e. If A is a strictly diagonally dominant matrix, then consider the following statements:
 (i) The Jacobi iteration scheme converges for any initial starting vector.
 (ii) The Gauss-Seidel iteration scheme converges for any initial starting vector.
 Which of the above statements are correct?
- (A) (i) only (B) (ii) only
 (C) Both (i) & (ii) (D) None of these
- f. In which year "C" language was developed?
- (A) 1960 (B) 1965
 (C) 1968 (D) 1972
- g. When the same number of tabular points are used, all interpolating polynomials are
- (A) different (B) identical
 (C) approximately correct (D) truncated
- h. In interpolation methods, if the order of derivative increases then the error of approximation
- (A) increases (B) decreases
 (C) has no effect (D) None of these
- i. The approximate value of $\int_0^1 \frac{\sin x}{x} dx$ using two-point open-type rule is
- (A) 0.9589 (B) 0.9546
 (C) 0.9590 (D) 0.9545
- j. Runge-Kutta methods use
- (A) single slopes (B) weighted average of slopes
 (C) simple average of slopes (D) None of these

Answer any FIVE Questions out of EIGHT Questions.
 Each question carries 16 marks.

- Q.2 a. Write a program in C to find the inverse of a matrix

$$A = \begin{pmatrix} 1 & 1 & 1 \\ 4 & 3 & -1 \\ 3 & 5 & 3 \end{pmatrix}$$

using Gauss-Jordan method and verify your result. (8)

- b. Given the following equation $x - e^x = 0$, determine the initial approximations for finding the smallest positive root. Use these to find the root correct to three decimal places with secant method. (8)

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Q.3 a. Prove that Newton-Raphson method has quadratic rate of convergence. (8)

b. Solve the following system of equations using Gauss-seidel method (show upto 5 iterations)

$$6x_1 - 2x_2 + x_3 = 11$$

$$x_1 + 2x_2 - 5x_3 = -1 \quad (8)$$

$$-2x_1 + 7x_2 + 2x_3 = 5$$

Q.4 a. Describe the two ways of passing parameters to functions. When do you prefer to use each of them? (8)

b. Construct the divided difference table for the data:

$$x: \quad 0.5 \quad 1.5 \quad 3.0 \quad 5.0 \quad 6.5 \quad 8.0$$

$$f(x): \quad 1.625 \quad 5.875 \quad 31.0 \quad 131.0 \quad 282.125 \quad 521.0$$

Hence, find the interpolating polynomial and an approximation to the value of $f(7)$. (8)

Q.5 a. Obtain the least square polynomial approximation of degree 2 for $f(x) = x^{1/2}$ on $[0, 1]$. Hence, find $P(0.7)$. (8)

b. By use of repeated Richardson extrapolation, find $f'(1)$ from the following values:

$$x: \quad 0.6 \quad 0.8 \quad 0.9 \quad 1.0 \quad 1.1 \quad 1.2 \quad 1.4$$

$$f(x): \quad 0.707178 \quad 0.859892 \quad 0.925863 \quad 0.984007 \quad 1.033743 \quad 1.074575 \quad 1.127986$$

Apply the approximate formula

$$f'(x_0) = \frac{f(x_0 + h) - f(x_0 - h)}{2h}$$

with $h = 0.4, 0.2, 0.1$. (8)

Q.6 a. Evaluate the integral $I = \int_1^2 \frac{2x}{1+x^4} dx$, using Gauss-Legendre 3-points quadrature rule. (8)

b. Compute $I = \int_0^1 \frac{x}{x^3 + 10} dx$ using Simpson's rule taking eight intervals. (8)

Q.7 a. The following data for the function $f(x) = x^4$ is given

$$x: \quad 0.4 \quad 0.6 \quad 0.8$$

$$f(x): \quad 0.0256 \quad 0.1296 \quad 0.4096$$

Find $f'(0.8)$ and $f''(0.8)$ using quadratic interpolation. Compare with the exact solution. Obtain the bound on the truncation errors. (8)

- b. Given the initial value problem

$$\frac{du}{dt} = -2tu^2, u(0) = 1$$

with $h = 0.2$, use the fourth-order Runge-Kutta method to find $u(0.2)$ and $u(0.4)$. (8)

- Q.8** a. Solve the system of equations

$$x_1 + x_2 - x_3 = 2$$

$$2x_1 + 3x_2 + 5x_3 = -3$$

$$3x_1 + 2x_2 - 3x_3 = 6$$

by the LU decomposition method. (8)

- a. Write a simple program to illustrate the method of sending an entire structure as a parameter to a function. (8)

- Q.9** a. Find the inverse of the matrix

$$A = \begin{pmatrix} 2 & 1 & 1 & -2 \\ 4 & 0 & 2 & 1 \\ 3 & 2 & 2 & 0 \\ 1 & 3 & 2 & -1 \end{pmatrix}$$

using partition method. Hence, solve the system of equations $Ax = b$, where

$$b = (-10, 8, 7, -5)^T. \quad (8)$$

- b. Find the smaller root of the equation

$$x^2 - 400x + 1 = 0$$

using four digit arithmetic. (8)