Diplete – Et/CS (NEW SCHEME) – Code: DE55 / DC

Subject: ENGINEERING MATHEMATICS - II

Time: 3 Hours

DECEMBER 2010

5 / DCs Max. Marks: 100

 (2×10)

NOTE: There are 9 Questions in all.

- Question 1 is compulsory and carries 20 marks. Answer to Q.1 must be written in the space provided for it in the answer book supplied and nowhere else.
- The answer sheet for the Q.1 will be collected by the invigilator after half an hour of the commencement of the examination.
- Out of the remaining EIGHT Questions answer any FIVE Questions. Each question carries 16 marks.
- Any required data not explicitly given, may be suitably assumed and stated.

Choose the correct or the best alternative in the following: Q.1 a. The value of the limit $\lim_{x \to 0} \frac{8^x - 2^x}{x}$ is equal to (A) log 4 **(B)** log 2 (**C**) log 3 **(D)** log 5 b. The value of definite integral $\int |\cos x| dx$ is equal to **(A)** 0 **(B)** 2 (C) 1 (D) ∞ c. The solution of $(1+\cos x) dy = (1-\cos x) dx$ is (A) $2 \tan x/2 - 2x + c$ **(B)** $2 \tan x/2 - x/2 + c$ (C) $2 \tan x/2 - x + c$ **(D)** $2 \tan x/2 + x + c$ d. If |z+i| = |z-i|, then the value of z is equal to **(A)** 1 **(B)** 0 **(C)** ∞ **(D)** x e. The power factor is equal to (**B**) $\frac{V}{R}$ (A) I.R (C) $\frac{|\mathbf{Z}|}{\mathbf{D}}$ **(D)**

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- f. The Laplace transform of e^{-3t} . (cos4t + 3sin4t) is
- **(B)** $\frac{s+12}{s^2+3s+6}$ (A) $\frac{s+4}{s^2+2s+4}$ (C) $\frac{s+15}{s^2+6s+25}$ **(D)** $\frac{s+15}{s^2+6s+15}$ g. The L⁻¹ $\left(\frac{s}{\left(s^2-1\right)^2}\right)$ is equal to
 - (A) $\frac{t}{2}$ cosh **(B)** $\frac{t}{2}$ sinh t (C) 2t sinh (**D**) 2t cosh t
- h. If \overrightarrow{a} and \overrightarrow{b} are two vectors such that $\left|\overrightarrow{a}\right| = 2$, $\left|\overrightarrow{b}\right| = 3$ and $\overrightarrow{a} \cdot \overrightarrow{b} = 3$, then the angle

between the vectors is equal to

(A) 30°	(B) 45°
(C) 60°	(D) 90°

i. The area of parallelogram. Whose adjacent sides are i-2j+3k and 2i+j-4k, is

(A) $5\sqrt{6}$ sq.unit	(B) $2\sqrt{3}$ sq.unit
(C) $3\sqrt{2}$ sq.unit	(D) None of above

j. If the voltage and current of a circuit are given by the complex numbers 70+20j and 20-6j respectively then the admittance in the form of complex number is equal to

(A) 3.56 + 2.23J	(B) 2.35 + 1.25j
(C) 1.57 + 2.56j	(D) 2.94 + 1.88j

Answer any FIVE Questions out of EIGHT Questions. Each question carries 16 marks.

a. Evaluate $\lim_{x \to 0} \frac{\tan x - \sin x}{x^3}$ **O.2** (8) b. The loop of the curve $ay^2 = x (x-a)^2$ revolves about the x-axis. Find the volume of the solid so generated. (8) 2

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- a. Separate $\sin^{-1}(\alpha + i\beta)$ into real and imaginary parts. Q.3
- StudentBounty.com ^ ^ ^ ^ ^ b. The forces 2i+7j, 2i-5j+6k, -i+2j-k act on a point P whose position vector is 4i-3j-2k. Find the vector moment of the resultants of three forces acting at P about the point Q, whose position vector is 6i + j - 3k.
- a. A condensor of the capacity c is discharged through an inductance L and a **Q.4** resistance R, in the series and the charge Q at the time t satisfies the equation $L\frac{d^2Q}{dt^2} + R\frac{dQ}{dt} + \frac{Q}{c} = 0$ given that L = 0.25 H, R = 250 ohms, and c = 2×10^{-6} farad and that when

t = 0, the charge Q is 0.002 coulomb and the current $\frac{dQ}{dt} = 0$, obtain the value of Q in the terms of t. (8)

b. Find the Fourier series of the function (8) $\begin{bmatrix} 0 & \text{when } -2 < t < -1 \end{bmatrix}$

$$f(t) = \begin{cases} 0 & \text{when} & 2 < t < 1 \\ k & \text{when} & -1 < t < 1 \\ 0 & \text{when} & 1 < t < 2 \end{cases}$$

a. Find the Laplace transform of $\frac{1-\cos 2t}{t}$. **Q.5** (6)

b. Evaluate
$$L^{-1}\left[\frac{s+4}{s(s-1)(s^2+4)}\right]$$
 (10)

a. Verify Rolle's Theorem for the function $f(x) = x (x+2) e^{-x/2}$ in the interval **Q.6** (-2,0)(8)

b. Find the Laplace Transform of the periodic function (saw tooth wave) $f(t) = \frac{kt}{t}$ for 0 < t < T, f(t+T) = f(t)(8)

Q.7 a. Solve the equation
$$\frac{d^2 y}{dt^2} + 2\frac{dy}{dt} + 2y = 5\sin t$$

if $y(0) = y'(0) = 0$ (8)

b. Solve the equation
$$\frac{d^2y}{dx^2} + 3\frac{dy}{dx} + 2y = \sin 2x$$
 (8)

Q.8 a. Find the Fourier series representing,
$$f(x) = x, 0 < x < 2\pi$$
 (8)

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- StudentBounts.com b. A resistance of 20 ohms, an inductance of 0.2 H and a capacitance of N micro farad are connected in series across 220 volts, 50 cycles/sec mains Determine (i) Impedance (ii) Current (iii) Voltage across L, R and C.
- Q.9 a. Find the area of the triangle formed by the points whose position vectors are 3i+j, 5i +2j +k, i-2j +3k.
 - b. Verify Langrage's Mean-value theorem for $f(x) = \log_e x$ in the interval [1,e]

(8)

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