

Mark Scheme (Results)

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme.

Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.

- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

• Types of mark

- M marks: method marks
- A marks: accuracy marks
- B marks: unconditional accuracy marks (independent of M marks)

• Abbreviations

- o cao correct answer only
- csa correct solution only
- o ft follow through
- isw ignore subsequent working
- SC special case
- oe or equivalent (and appropriate)
- dep dependent
- o indep independent
- eeoo each error or omission
- awrt answer rounding to

No working

If no working is shown then correct answers normally score full marks

If no working is shown then incorrect (even though nearly correct) answers score no marks.

• With working

If there is a wrong answer indicated always check the working in the body of the script and award any marks appropriate from the mark scheme.

If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks.

If a candidate misreads a number from the question. Eg. Uses 252 instead of 255; method marks may be awarded provided the question has not been simplified. Examiners should send any instance of a suspected misread to review. If working is crossed out and still legible, then it should be given any appropriate marks, as long as it has not been replaced by alternative work.

If there are multiple attempts shown, then all attempts should be marked and the highest score on a single attempt should be awarded.

• Follow through marks

Follow through marks which involve a single stage calculation can be awarded without working since you can check the answer yourself, but if ambiguous do not award.

Follow through marks which involve more than one stage of calculation can only be awarded on sight of the relevant working, even if it appears obvious that there is only one way you could get the answer given.

• Ignoring subsequent work

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. Incorrect cancelling of a fraction that would otherwise be correct.

It is not appropriate to ignore subsequent work when the additional work essentially shows that the candidate did not understand the demand of the question.

• Linear equations

Full marks can be gained if the solution alone is given, or otherwise unambiguously indicated in working (without contradiction elsewhere). Where the correct solution only is shown substituted, but not identified as the solution, the accuracy mark is lost but any method marks can be awarded.

• Parts of questions

Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded in another.

Question	Working	Answer	Mark	Notes
1 (a)	180×8	1440 g (cao)	2	M1 A1
(b)	0.84×180 OR $(180 - 180 \times 0.16)$	151 kg, 151.2 kg	2	M1 A1

Question	Working	Answer	Mark	Notes
2	(3x-2)(x-1) = (x+5)(x+7) OR $(3x-2)(x-1) - (x+5)(x+7)$		7	M1 Missing brackets can only be condoned if the related expansions are correct
	$3x^{2} - 5x + 2 = x^{2} + 12x + 35$ OR $3x^{2} - 5x + 2 - (x^{2} + 12x + 35) \text{ (oe)}$			M1 (DEP) one term can be incorrect
	$2x^2 - 17x - 33 (= 0)$	cao		A1
	$x = \frac{17 \pm \sqrt{(-17)^2 - 4 \times 2 \times (-33)}}{2 \times 2}$ (no errors on candidates'	Cu o		M1 (INDEP) for solving their trinomial quadratic equation
	quadratic)			SC M1(INDEP) for factorisation of their trinomial quadratic producing 2 of the 3 terms of their quadratic
	$\sqrt{553}$ (= 23.515) (candidate must have a seen +ve discriminant)			M1 (DEP) on previous M1 and can only be implied by seen correct answer(s).
		x = 10.1 x = -1.63		A1 A1 Both cao
	NB: Some correct working must be seen for obtaining the quadratic and only then can the following M1(INDEP) M1(DEP) be obtained if their answers correspond to their quadratic.			

Question	Working	Answer	Mark	Notes
3 (a)		$\frac{-1}{2} \begin{pmatrix} 1 & 2 \\ 4 & 6 \end{pmatrix} (\text{oe})$	2	B2 (-1 eeoo)
				NB: Allow ISW
(b)	$\binom{-1}{2} \begin{pmatrix} 1 & 2 \\ 4 & 6 \end{pmatrix}, \binom{6}{-4} \begin{pmatrix} -2 \\ -4 & 1 \end{pmatrix} \binom{x}{y} = \binom{-1}{2} \begin{pmatrix} 1 & 2 \\ 4 & 6 \end{pmatrix}, \binom{5}{-3} (\text{oe})$		4	M1
	$\binom{x}{y} = \frac{-1}{2} \binom{-1}{2}$ (oe), ie 2x1 matrix	$\begin{array}{l} x = 0.5 \\ y = -1 \end{array}$		M1 (DEP)
		y I		A1 A1
	\mathbf{OR} $6x - 2y = 5 \qquad (no slips, oe)$			(M1)
	-4x + y = -3 Correct equation in <i>x</i> or <i>y</i> seen (Allow 1 alg/numeric slip)	$\begin{array}{l} x = 0.5 \\ y = -1 \end{array}$		(M1 DEP) (A1) (A1) SC: $\begin{pmatrix} 0.5\\ -1 \end{pmatrix}$ collects A1 A1

Question	Working	Answer	Mark	Notes
4 (a)	$p \times 2 + q = -1$ (oe) $p \times 5 + q = 11$ (oe)		2	B1 B1
(b)	Rearranging their equations so coefficient of p is the same in both equations OR isolating p or q then adding or subtracting equations OR substitute expressions for p or q to obtain q or p		3	M1 (No slips)
		p = 4 $q = -9$		A1 A1
(c)	(4(4x-9)-9)''	$\mathrm{ff}: x\mapsto 16x-45$	2	M1 A1 ft NB: (Answer must be in correct form)
(d)	" $4x - 9$ " = " $16x - 45$ " OR $x = "4x - 9$ "	<i>x</i> = 3 (cao)	2	M1 A1

Qu	estion	Working	Answer	Mar k		Notes
5	(a)(i)		4 a	1	B1	
	(ii)		4 b – 6 a	1	B 1	oe
	(b)	$\overrightarrow{CD} = \overrightarrow{CO} + \overrightarrow{OD} = -4\mathbf{a} + \lambda \times 4\mathbf{b}$	$\overrightarrow{DB} = \frac{4}{2}\mathbf{b}$	4	M1	
		$\overrightarrow{AB} = -6\mathbf{a} + 4\mathbf{b} \therefore \lambda = \frac{2}{3}$	$DB = \frac{1}{3}D$		M 1	(DEP) for using \overrightarrow{CD} is parallel to
		5				\overrightarrow{AB}
		$\overrightarrow{DB} = \overrightarrow{OB} - \overrightarrow{OD} = 4\mathbf{b} - \frac{8}{2}\mathbf{b}$			M1	(DEP) complete method to find \overrightarrow{DP}
		3			A1	\overrightarrow{DB} fully correct solution
		Alternatives for 5(b):				
		OR $\overrightarrow{CD} = \lambda \overrightarrow{AB} = \lambda (-6\mathbf{a} + 4\mathbf{b})$			M 1	
		$\overrightarrow{DB} = \mu \overrightarrow{OB} = 4\mu \mathbf{b} = \overrightarrow{DC} + \overrightarrow{CA} + \overrightarrow{AB} = (6\lambda - 4)\mathbf{a} + (4 - 4\lambda)\mathbf{b}$			M1	(dep)
		OR just				
		$\overrightarrow{OD} = \overrightarrow{OC} + \overrightarrow{CD} = 4\mathbf{a} + \lambda (4\mathbf{b} - 6\mathbf{a}) = (4 - 6\lambda)\mathbf{a} + 4\lambda\mathbf{b}$			2.64	
		Equating coefs: $6\lambda - 4 = 0$ and $4 - 4\lambda = 4\mu$			M1	(dep)
		OR just $4-6\lambda = 0$			M1 A1	(dep)
		$\overrightarrow{DB} = \frac{4}{3}\mathbf{b}$				
		OR $\overrightarrow{OD} = "4\mathbf{a}" + \frac{2}{3}"4\mathbf{b} - 6\mathbf{a}"$ (oe) OR $\overrightarrow{OD} = \frac{2}{3} \times 4\mathbf{b}$			M1	
		$\overrightarrow{OD} = \frac{8\mathbf{b}}{3}$			M1	(dep)
		$\overrightarrow{DB} = \overrightarrow{OB} - \overrightarrow{OD} = 4\mathbf{b} - "\frac{8}{3}\mathbf{b}"$			M1	(dep)

$\overrightarrow{DB} = \frac{4}{3}\mathbf{b}$	A1
NB: Any method for \overrightarrow{OD}	M1M1 (dep)
but $\therefore \overline{DB} = \frac{1}{2} "\overline{OD}"$ scores	M0A0
whilst $\overrightarrow{DB} = \overrightarrow{OB} - \overrightarrow{OD} = 4\mathbf{b} - \frac{8}{3}\mathbf{b} = \frac{4}{3}\mathbf{b}$ will score M1	
A1 since a vector method has been used.	
(NB: The question does not say "using only vector methods throughout".)	
OR $\overrightarrow{CD} = \frac{2}{3}\overrightarrow{AB} = \frac{2}{3}$ "4b - 6a" (oe)	M1
$\overrightarrow{CA} = 2\mathbf{a}$	M1 (dep)
$\overrightarrow{DB} = \overrightarrow{DC} + \overrightarrow{CA} + \overrightarrow{AB} = "-\frac{2}{3}(4\mathbf{b} - 6\mathbf{a})" + 2\mathbf{a} + "4\mathbf{b} - 6\mathbf{a}"$	M1 (dep)
$\overrightarrow{DB} = \frac{4}{3}\mathbf{b}$	A1

(Question	Working	Answer	Mark	Notes
6	(a)(i)	$3 \times 4t^2 - 2 \times 18t + 5$	2	2	M1 at least 2 terms correct
			$12t^2 - 36t + 5$		A1 cao
	(ii)	"2×12 <i>t</i> – 36"		2	M1 at least 1 term correct
		Note: ft from (a) (i) provided there are two terms	24t - 36		A1 ft
	(b)	24t - 36 > 0		2	M1 Must be a linear expression which
	(-)		<i>t</i> > 1.5		can involve = , \geq and >
		Note: ft from (a) (ii) provided "1.5" is positive			A1 ft, oe, must be $t > \dots$

Question	Workin	g	Answer	Mark		Notes
7 (a)			65	1	B1	
(b)	5 bars drawn		Heights 3.5, 4.2, 0.8, 3, 4	5	B5	-1eeoo Penalise a maximum
	Note: Gaps between bars is one error of	only				of one error for each bar
					SC	If B0 but all correct frequency densities calculated then B1.
(c)	$\frac{4}{15}$ or $\frac{11}{15}$ or $\frac{18}{20}$ or $\frac{2}{20}$	Using frequency density of 3 or 3.5		4	M1	
	70 × $\frac{18}{20}$ (= 63) or 70 × $\frac{2}{20}$ (= 7) or 45 × $\frac{4}{15}$ (= 12) or 45 × $\frac{11}{15}$ (= 33)	$(34-30) \times 3 (= 12)$ or $(20-2) \times 3.5 (= 63)$ or $(20-18) \times 3.5 (= 7)$ $(45-34) \times 3 (= 33)$			M1	(DEP)
	"7" + 21 + 4 + "12" (= 44) or 160 - "		44 11		M1	(DEP)
			$\frac{44}{160}$, $\frac{11}{40}$, 0.275		A1	

Question	Working	Answer	Mark	Notes
	Penalise nc ONCE only and at the first occurrent	l		
8 (a)	$\cos 23 = \frac{9}{OA} (oe)$	<i>OA</i> = 9.78	2	M1
(b)	$\begin{vmatrix} OC^2 + 9^2 = \\ "9.78"^2 \\ (OC = \\ 3.81965 \end{vmatrix} \sin 23 = \frac{OC}{"9.78"} \tan 23 = \frac{OC}{9} \\ (OC = 3.82) \end{vmatrix} (OC = 3.82)$		3	A1 M1 correct first step of a method to find <i>OC</i>
	$\therefore AP = "9.78" - "3.82"$ OR Secant Tangent Theorem: <i>POQ</i> is a diameter of the circle then <i>PQ</i> = 2 <i>OC</i>			M1(DEP) complete method to find <i>AP</i>
	$AP(AP+2OC) = 9^2$			(M1)
	$AP^2 + 2 \times "3.82" - 81 = 0$			(M1DEP)
		AP = 5.95 (Pyth.), 5.96		A1
(c)	$\Delta OBP: BP^{2} = "3.82"^{2} + "3.82"^{2} - 2 \times (3.82" \times 3.82" \times \cos(180 - 23 - 90))$	5.90	3	M1
	$BP = \sqrt{"17.783"}$ (= 4.217)			M1 (DEP)
	OR $\triangle ABP: BP^2 = 9^2 + "5.96"^2 - 2 \times 9 \times$ "5.96" × cos 23			(M1)
	OR $\frac{BP}{\sin 67} = \frac{"OP"}{\sin 56.5}$ BP = $\sqrt{"17.783"}$ (= 4.217)	DD 400		(M1 DEP)
	OR $BP = \frac{"OP" \times \sin 67}{\sin 56.5}$	<i>BP</i> = 4.22, 4.23		

	OR $\frac{1}{2}\Delta OBP: \qquad \angle BOP = 180 - 23 - BP = 2 \times "3.82" \times \sin\left(\frac{"67"}{2}\right)$	90 (= 67)			(M1) (M1 DEP)
(d)	"5.96" ⁼ "4.22" (180 NB: comp	$CP = 90 - \frac{1}{2} \times 0 - \frac{67}{2}$ Must see a plete method $\angle ACP$		2	A1 M1
	$"5.96"^{2} = "4.22"^{2} + 9^{2} - 2 \times "4.22"^{2}$		∠ <i>ACP</i> = 33.3, 33.4, 33.5, 33.6		A1
(e)	$\Delta OBA = 9 \times "3.82" \div 2 \qquad \text{OR}$ $\frac{1}{2} \times 9 \times "OA" \times \sin 23 \ (= 17.19)$ $\text{Sector } OBP = \pi \times "3.82"^2 \times \frac{67}{360} \ (= \Delta OBA - \text{Sector } OBP = "17.19" - "$	= 8.53)		4	M1 M1 M1 (DEP) DEP on <i>both</i> M1s
	8.658)		8.62, 8.63, 8.64, 8.65, 8.66, 8.67		A1

Question	Working	Answer	Mark		Notes
	Penalise missing labels only ONCE in the ques	stion, the first time it occu		-	
9 (a)		Translation	2	B1	
		$\binom{6}{}$		B1	
		(-2)		NB:	Only ONE transformation can be mentioned otherwise B0 B0
(b)	$ \begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix} \begin{pmatrix} 1 & 1 & 3 \\ 2 & 5 & 5 \end{pmatrix} $	C drawn and labelled	3	M1	
	<i>C</i> has coordinates (-2, -1), (-5, -1), (-5, -3)			A2	-leeoo
	Note: If matrix product not seen, then it can be implied from a correct <i>C</i> .				
(c)	D has coordinates (5, 3), (5, 9), (9, 9)	D drawn and labelled	3	B3	-1eeoo
(d)	<i>E</i> has coordinates (2, -1), (5, -1), (5, -3)	<i>E</i> drawn and labelled	2	B2ft	-1eeoo
(e)	Note: Must be consistent with their diagram and their triangle <i>E</i> must be a rotation of triangle <i>A</i> to achieve any marks	Rotation 90° clockwise (-4, -2)	3	B1 B1 B1	Rotation 90° clockwise (-4, -2)
	NB: More than ONE translation given scores B0 B0 B0				

Ques	stion	Working	Answer	Mark	Notes
10	(a)	$\mathbf{S} = 2 \times \pi r l + 2\pi r h$	$S = 2\pi r(h+l)$ cso	2	M1 A1
	(b)	$60 = 2\pi r(h+4)$	$h = \frac{30}{\pi r} - 4$ cso	2	M1 A1
	(c)	$V = 2 \times \frac{1}{2}\pi r^2 h + \pi r^2 h$		4	M1
		$V = 2 \times \frac{1}{3} \pi r^2 h + \pi r^2 h$ $V = 2 \times \frac{1}{3} \pi r^2 \left(\frac{30}{\pi r} - 4\right) + \pi r^2 \left(\frac{30}{\pi r} - 4\right) \qquad \text{subst. } h$			M1 (DEP)
		OR			
		$V = \frac{5\pi r^2}{3}h$ $V = 20r - \frac{8}{3}\pi r^2 + 30r - 4\pi r^2$ eliminating <i>r</i> denominators			M1 (DEP)
		OR			Must have completely correct
		$V = \frac{5\pi r^2}{3} \left(\frac{30}{\pi r} - 4\right) \qquad \text{(oe)} \qquad \text{subst. } h$	$V = 50r - \frac{20}{3}\pi r^2 cso$		algebra throughout A1
	(d)	$\frac{dV}{dr} = 50 - \frac{40}{3}\pi r$		5	M1 one term correct
		$\frac{dV}{dr} = 50 - \frac{40}{3}\pi r$ 50 - $\frac{40}{3}\pi r = 0$			M1 (DEP) fully correct and equating to 0
		$r = \frac{15}{4\pi}, \ 1.19$ eg 50 × " $\frac{15}{4\pi}$ " - $\frac{20}{3}$ × π × $\left($ " $\frac{15}{4\pi}$ " $\right)^2$			A1
		eg 50 × " $\frac{15}{4\pi}$ " – $\frac{20}{3}$ × π × (" $\frac{15}{4\pi}$ ") ²			M1 (INDEP) for substituting <i>r</i> in <i>V</i>
			V = 29.8		A1 awrt 29.8

Questi	on	Working	Answer	Mark	Notes
11	(a)		-3	3	B1
			-4.5		B1
	(b)	-1 mark for straight line segments	27 Correct Curve	3	B1 B3 ft -1 eeoo
	(0)		Confect Curve	5	B3 It 1 6600
		Each point missed ($\pm \frac{1}{2}$ small square)			
		Each missed segment			
		Each point not plotted			
		Tramlines			
		Very poor curve			
		NB: ft on "-3", "-4.5" and "27"			
	(c)	$-5.186337289 \rightarrow -5.2 \pm 0.2$	-5.0,	1	B1 cao (-5 scores B0)
			-5.1, -5.2, -5.3,		
			-5.4		
	(d)	y = 4x - 7 drawn correctly	Line	1	B1
		Note: line must pass through any two of $(0, -7)$, $(1, -3)$, $(2, 1)$, $(3, 5)$			
		and drawn between $x=0.6$ to $x=2.2$ so that the intersections in (e) can be seen.			
	(e)	be seen.			
	(0)				
		Values must be read off their curve and straight line from (d)			B1 Critical pt value
			awrt 0.7, 0.8	4	B1 Critical pt value
			awrt 2.1		B1
			x > awrt 0.7, 0.8		B1
		Nata (1) Danaliza aquality signs (compat dimetion but	x < awrt 2.1		
		Note: (1) Penalise equality signs (correct direction but includes the equality) ONCE only.			
		(2) Answer for part (e) may be seen as one inequality			

Graph for Question 11

