# Mark Scheme (Results) November 2007 

## IGCSE

IGCSE Mathematics (4400_4H)

## 4400 IGCSE Mathematics

November 2007
Paper 4H

| Q | Working | Answer | Mark | Notes |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1. | $\frac{1.6}{2.5}$ |  | 2 | M1 | for 1.6 or 2.5 seen or for 2.430 ... |
|  |  | 0.64 |  | A1 | Accept $\frac{16}{25}$ |
|  |  |  |  |  | Total 2 marks |


| 2. | (a) |  | $5(x-4)$ | $\mathbf{1}$ | B1 | cao |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | (b) |  | $y(y+6)$ | $\mathbf{2}$ | B2 | B1 for factors, which, when expanded and <br> simplified, give two terms, one of which is <br> correct except $(y+6)(y-6)$ and similar <br> SC B1 for $y(y+6 y)$ |
|  |  |  |  |  |  |  |


| 3. |  | $630 \times 1.45 \div 2.61$ |  | $\mathbf{2}$ | M1 | for $\frac{630}{2.61}$ or 241.38 or better or 241.37 <br> or $630 \times 1.45$ or 913.5 or $0.55 \ldots$ seen <br> or 1.8 seen |
| :---: | :---: | :---: | :---: | :---: | :---: | :--- |
|  |  |  |  | 350 |  | A1 |
|  |  |  | Accept 349.99 or 350 |  |  |  |


| 4. |  | Reflection in $x=4$ |  | $\mathbf{2}$ | B1 | for reflection, reflect |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  | B1 | for $x=4$ stated or eg 'in dotted line' |
|  |  |  |  |  |  |  |


| 5. |  | $72 \div 6$ or 12 seen |  | $\mathbf{2}$ | M1 |  |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  | 84 |  | A1 | cao |
|  |  |  |  |  |  |  |


| 6. | (a)(i) | 57 | 2 | B1 | cao |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (ii) | alternate angles |  | B1 |  | Do not accept Z angles or F angles |
|  | (b) | corresponding angles and sum of angles on a straight line is $180^{\circ}$ or allied or co-interior angles and (vertically) opposite angles or alternate angles and sum of angles on a straight line is $180^{\circ}$ | 2 | B1 | for one pair |  |
|  |  | 71 |  | B1 | cao |  |
|  |  |  |  |  |  | Total |


| 7. | (a) | $\frac{55}{150} \times 60$ |  | 3 | B1 M1 | for $\frac{55}{150}$ oe or $\frac{60}{150}$ oe seen for $\frac{55}{150} \times 60$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 22 |  | A1 | cao |
|  | (b) | $\begin{aligned} & 68 \times 48+58 \times 35 \\ & =3264+2030 \end{aligned}$ |  | 3 | M1 | 2 products $m \times f$ where $m$ is within each interval and consistent (inc end points) |
|  |  |  |  |  | M1 | (dep) for use of halfway values |
|  |  |  | 5294 |  | A1 | Accept 5300 or 5290 if M1 + M1 scored |
|  | (C) | eg no upper limit for extra large, no lower limit for small, don't know midpoints for XL, S |  | 1 | B1 |  |
|  |  |  |  |  |  | Total 7 marks |


| 8. | (a) |  | 2 | B2 | B1 for either open circle at -2 or solid circle at 3 |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | (b) | $-101023$ | 2 | B2 | B1 for all correct + 1 wrong or for four correct and none wrong |
|  |  |  |  |  | Total 4 marks |


| 9. |  | arc centre B cutting AB and AC at (say) P and Q | $\mathbf{2}$ | B1 |  |
| :--- | :--- | ---: | ---: | ---: | ---: |
|  |  | arcs centre P and Q of equal radii which intersect at |  |  |  |
|  |  | $R$ (say) and BR joined |  | B1 | (dep) bisector within tolerance |
|  |  |  |  |  |  |


| 10. | (a) | 7 |  | 2 | B2 | B1 for 4 correct |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (b) |  | graph | 2 | B2 | B1 for 5 points plotted correctly $\pm 1 / 2$ sq ft from (a) if at least B1 scored B1 for correct curve or, if there are 1 or 2 errors in (a) and no plotting errors, award for a curve passing through the 7 points from their table. |
|  |  |  |  |  |  | Total 4 marks |
|  |  |  |  |  |  |  |
| 11. |  | $420 \times \frac{100}{56}$ |  | 3 | M1 | for $420 \div 56$ or 7.5 seen |
|  |  |  |  |  | M1 | (dep) for $\times 100$ |
|  |  |  | 750 |  | A1 | cao |
|  |  |  |  |  |  | Total 3 marks |


| 12. | $4.9^{2}+16.8^{2}$ or $24.01+282.24$ <br> or 306.25 |  | $\mathbf{3}$ | M1 | for squaring and adding |  |
| :--- | :--- | :--- | :--- | :---: | :---: | :--- |
|  | $\sqrt{4.9^{2}+16.8^{2}}$ |  |  | M1 | (dep) for square root |  |
|  |  |  | 17.5 |  | A1 | cao |
|  |  |  |  |  |  |  |

$\left.\begin{array}{|l|l|l|l|l|l|l|}\hline \text { 13. } & & \frac{20805}{1.14} \text { or } 20805 \times \frac{100}{114} & & \text { 3 } & \text { M2 } & \text { for } \frac{20805}{1.14} \text { or } 20805 \times \frac{100}{114} \\ \text { M1 for } \frac{20805}{114}, 114 \%=20805 \\ \text { or } 182.5 \text { seen }\end{array}\right]$

| 14. | (a) |  | $6 n^{2}$ | $\mathbf{1}$ | B1 | cao |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | (b) | $3 x^{3} y^{2}$ | $\mathbf{2}$ | B2 | B1 for $x^{3}$ or $\mathrm{y}^{2}$ |  |
|  | (c) |  | $\mathrm{t}^{12}$ | $\mathbf{1}$ | B1 | cao |
|  | (d) |  | $\frac{\mathrm{p}^{6}}{8}$ | $\mathbf{2}$ | B2 | B1 for $\frac{1}{8}$ oe or for $\mathrm{p}^{6}$ |
|  |  |  |  |  |  |  |


| 15. | (a) | $6.8 \times \frac{15}{10}$ |  | 2 | M1 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | 10.2 |  | A1 | cao |
|  | (b) | $12.3 \times \frac{10}{15}$ |  | 2 | M1 |  |
|  |  |  | 8.2 |  | A1 | cao |
|  | (c) | $\frac{15}{10}$ or 1.5 oe |  | 2 | M1 | for $\frac{15}{10}$ or 1.5 oe <br> or for $\left(\frac{10}{15}\right)^{2}$ or $\frac{4}{9}$ or $0 . \dot{4}$ oe <br> or for correct expression which, if accurately evaluated, gives the correct answer <br> or for the area of one of the triangles evaluated correctly <br> Area $\triangle \mathrm{ABC}$ rounds to 62.3 (62.2700...) <br> NOT 62.73 <br> Area $\Delta$ CDE rounds to 27.7 (27.6755...) <br> NOT 27.88 <br> Note: the angles of the triangle are $42.5^{\circ}, 54.5^{\circ}$ and $83.1^{\circ}$. |
|  |  |  | 2.25 oe |  | A1 | for 2.25 or $21 / 4$ or ${ }^{9} / 4$ or for answer rounding to 2.25 <br> Even if M1 awarded, do not award A1 for a correct answer, if there are any errors in the working. |
|  |  |  |  |  |  | Total 6 marks |


| 16. | (a)(i) |  | 15 | $\mathbf{2}$ | B1 | cao |
| :---: | :---: | :--- | ---: | :---: | :---: | :---: |
|  | (ii) |  | 7 or 8 |  | B1 |  |
|  | (b) | 26 or $261 / 2$ |  | $\mathbf{2}$ | M1 | may be stated or indicated on graph |
|  |  |  | $54-55$ inc |  | A1 |  |
|  |  |  |  |  |  |  |


| 17. | (a) | $72=2^{3} \times 3^{2}$ and $90=2 \times 3^{2} \times 5$ <br> or $2 \times 3^{2}$ <br> or $1,2,3,4,6,8,9,12,18,24,36,72$ <br> and $1,2,3,5,6,9,10,15,18,30,45,90$ |  | $\mathbf{M 1}$ | Need not be products of powers; <br> accept products or lists ie 2,2,2,3,3 <br> and 2,3,3,5 <br> Prime factors may be shown as factor <br> trees |  |
| :---: | :---: | :--- | :--- | :--- | :---: | :--- |
|  |  |  | 18 |  | A1 | cao |
|  | (b) | $2^{3} \times 3^{2} \times 5$ <br> or $72,144,216,288,360$ <br> and $90,180,270,360$ |  | $\mathbf{2}$ | $M 1$ |  |
|  |  |  | 360 |  | A1 | cao |
|  |  |  |  |  |  |  |


| 18. | (a) | $2 y=6-x$ |  | 3 | M1 | for $2 \mathrm{y}=6-\mathrm{x}$ or for stating coordinates of 2 points on line |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $y=3-\frac{x}{2} \text { or } y=\frac{6-x}{2}$ |  |  | M1 | for correct rearrangement of equation with y as subject or for attempt to find gradient of line joining two stated points |
|  |  |  | -1/2 |  | A1 | for $-1 / 2$ oe dep only on first M1 SC if M0, award B1 for correct ft from incorrect rearrangement |
|  | (b) |  | $\begin{array}{r} y=-1 / 2 x+5 \\ \text { oe } \end{array}$ | 1 | B1 | correct answer or ft from (a) Equivalent equations include $x+2 y=10$ |
|  |  |  |  |  |  | Total 4 marks |


| 19. | (i) |  | 8 | $\mathbf{4}$ | B1 | cao |
| :---: | :---: | ---: | ---: | ---: | :--- | :--- |
|  | (ii) |  | 12 |  | B1 | cao |
|  | (iii) |  | 0 |  | B1 | cao |
|  | (iv) |  | 16 |  | B1 | cao |
|  |  |  |  |  |  |  |


| 20. | (a) | $\frac{\mathrm{d} y}{\mathrm{~d} x}=3 x^{2}-10 x+8$ |  | 4 | B2 | B1 for 2 correct terms |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $3 \times 2^{2}-10 \times 2+8$ |  |  | M1 | (dep on at least B1) for substituting $x=2$ |  |
|  |  |  | 0 |  | A1 | cao |  |
|  | (b) |  | (could be) turning point, max or min, <br> (is) stationary point tangent is parallel to the $\mathrm{x}=\mathrm{axis}$ | 1 | B1 |  |  |
|  |  |  |  |  |  |  | Total 5 marks |


| 21. | (a) | bar height 21 little squares | $\mathbf{2}$ | B1 | Allow $\pm 1 / 2 \mathrm{sq}$ |  |
| :--- | :--- | ---: | ---: | ---: | ---: | :--- |
|  |  |  | bar height 6 little squares |  | B1 | Allow $\pm 1 / 2 \mathrm{sq}$ |
|  | (b) |  |  | $\mathbf{8}$ | $\mathbf{1}$ | B1 |
|  |  | cao |  |  |  |  |


| 22. | (a)(i) |  | 38 | $\mathbf{2}$ | B1 | cao |
| ---: | ---: | :--- | :--- | :---: | :---: | :--- |
|  | (ii) |  | Angles in the same segment oe |  |  | B1 |
|  | (b) |  | Award if 'same segment' 'same arc' <br> or 'same chord' stated or implied |  |  |  |
|  |  |  |  | $\mathbf{2}$ | B2 | B1 for $\angle A D C=90^{\circ}$ or $\angle C O D=76{ }^{\circ}$ stated or <br> indicated on diagram |


| 23. | (a) | $3(2 x-5)+2$ or $6 x-15+2$ |  | 2 | M1 |  |
| :---: | :---: | :--- | :--- | :--- | :--- | :--- |
|  |  |  | $6 x-13$ |  | A1 |  |
|  | (b) | eg $\times 3 \rightarrow+2$ <br> $\div(3 \leftarrow-2$ <br> $x$ the subject of $y=3 x+2$ <br> or $x=3 y+2$ |  |  | M1 |  |
|  |  |  | $\frac{x-2}{3}$ oe |  | A1 |  |
|  |  |  |  |  |  |  |


| 24. | $\frac{3}{5} \times \frac{3}{4}+\frac{2}{5} \times \frac{2}{4}$ |  | $\mathbf{3}$ | M2 | for sum of both products <br> (M1 if one correct product seen) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\frac{13}{20}$ |  | A1 |  |
|  |  |  |  |  |  |  |


| 25. | (a) | $3 x+x(4-x)=11$ <br> or $4 x+x(3-x)=11$ <br> or $(4-x)(3-x)=1$ <br> or $12-(4-x)(3-x)=11$ |  | 2 | M1 |  | Award M1 A1 for $4 x+3 x-x^{2}=11$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $3 x+4 x-x^{2}=11$ <br> or $4 x+3 x-x^{2}=11$ <br> or $12-4 x-3 x+x^{2}=1$ <br> or $12-12+4 x+3 x-x^{2}=11$ |  |  | A1 |  |  |
|  | (b) | $\frac{7 \pm \sqrt{(-7)^{2}-4 \times 11}}{2}$ |  | 3 | M1 | for correct substitution Condone omission of brackets |  |
|  |  | $\frac{7 \pm \sqrt{5}}{2}$ |  |  | M1 | for correct simplification |  |
|  |  |  | 4.62, 2.38 |  | A1 | for 3 sf or better (4.61803... , 2.38196...) |  |
|  | (c)(i) |  | 2.38 | 2 | B1 | for 2.38 or better |  |
|  | (ii) |  | eg $x<3$ |  | B1 |  |  |
|  |  |  |  |  |  | Total 7 marks |  |


| 26. | (a) | $\frac{1}{3} \pi r^{2} \times r+\pi r^{2} \times r$ or $\frac{1}{3} \pi r^{3}+\pi r^{3}$ |  | $\mathbf{2}$ | M1 |  |
| :--- | :--- | :--- | :--- | :---: | :---: | :---: |
|  |  |  | $\frac{4}{3} \pi r^{3}$ |  | A1 | dep on M1 |
|  | (b) | $\pi r l+2 \pi r^{2}+\pi r^{2}$ oe |  | $\mathbf{3}$ | M1 |  |
|  |  | $1>$ r or $l=r \sqrt{2}$ oe |  |  | M1 |  |
|  |  |  | $>4 \pi r^{2}$ |  | A1 |  |
|  |  |  |  |  |  | Total 5 marks |

