Centre No.						Surname	Initial(s)
Candidate No.						Signature	

Paper Reference(s)

4400/3H

London Examinations IGCSE

Mathematics

Paper 3H

Higher Tier

Thursday 17 May 2007 – Morning

Time: 2 hours

Examiner's use only

Team Leader's use only

Page Number	Leave Blank
3	
4	
5	
6	
7	
8	
9	
10	
11	
12	
13	
14	
15	
16	
17	
18	
19	
20	
Total	

Materials required for examination

Ruler graduated in centimetres and millimetres, protractor, compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.

Items included with question papers

Nil

Instructions to Candidates

In the boxes above, write your centre number, candidate number, your surname, initial(s) and signature.
Check that you have the correct question paper.
Answer ALL the questions in the spaces provided in this question paper.
You must NOT write on the formulae page. Anything you write on the formulae page will gain NO credit.
If you need more space to complete your answer to any question, use additional answer sheets.

Information for Candidates

The marks for individual questions and the parts of questions are shown in round brackets: e.g. **(2)**.
There are 19 questions in this question paper. The total mark for this paper is 100.
There are 20 pages in this question paper. Any blank pages are indicated.
You may use a calculator.

Advice to Candidates

Write your answers neatly and in good English.

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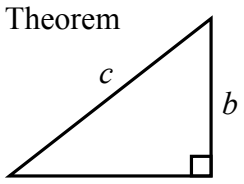
IGCSE MATHEMATICS 4400
FORMULA SHEET – HIGHER TIER

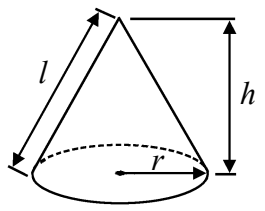
Pythagoras' Theorem



$a^2 + b^2 = c^2$

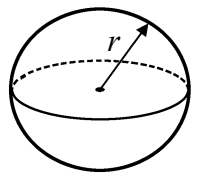
Volume of cone = $\frac{1}{3}\pi r^2 h$

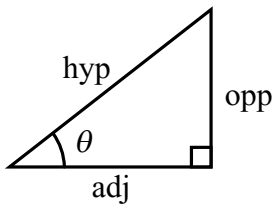
Curved surface area of cone = $\pi r l$



Volume of sphere = $\frac{4}{3}\pi r^3$

Surface area of sphere = $4\pi r^2$





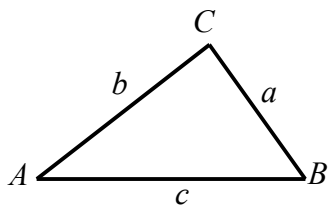
adj = hyp × cos θ
opp = hyp × sin θ
opp = adj × tan θ

or $\sin\theta = \frac{\text{opp}}{\text{hyp}}$

$\cos\theta = \frac{\text{adj}}{\text{hyp}}$

$\tan\theta = \frac{\text{opp}}{\text{adj}}$

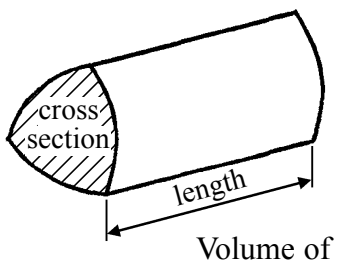
In any triangle ABC



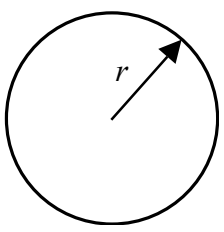
Sine rule: $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

Cosine rule: $a^2 = b^2 + c^2 - 2bc\cos A$

Area of triangle = $\frac{1}{2}ab\sin C$



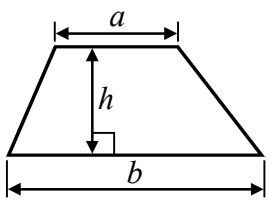
Volume of prism = area of cross section × length

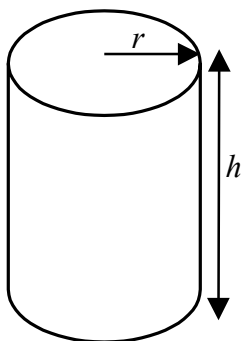


Circumference of circle = $2\pi r$

Area of circle = πr^2

Area of a trapezium = $\frac{1}{2}(a + b)h$





Volume of cylinder = $\pi r^2 h$

Curved surface area of cylinder = $2\pi r h$

The Quadratic Equation
The solutions of $ax^2 + bx + c = 0$, where $a \neq 0$, are given by

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Leave blank

Answer ALL NINETEEN questions.

Write your answers in the spaces provided.

You must write down all stages in your working.

1. (a) Use your calculator to work out the value of

$$\frac{(3.7+4.6)^2}{2.8+6.3}$$

Write down all the figures on your calculator display.

.....

(2)

(b) Give your answer to part (a) correct to 2 decimal places.

.....

(1)

(Total 3 marks)

Q1

2. (a) Work out the value of $x^2 - 5x$ when $x = -3$

.....

(2)

(b) Factorise $x^2 - 5x$

.....

(2)

(Total 4 marks)

Q2

Leave blank

3. Hajra counted the numbers of sweets in 20 packets.
The table shows information about her results.

Number of sweets	Frequency
46	3
47	6
48	3
49	5
50	2
51	1

Work out the mean number of sweets in the 20 packets.

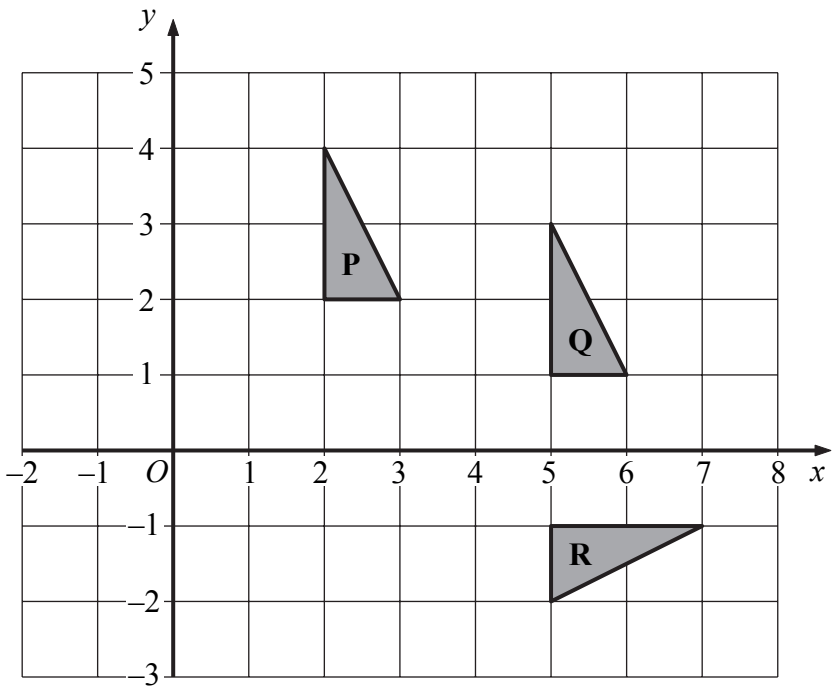
.....

(Total 3 marks)

Q3

Leave blank

4.



(a) Describe fully the single transformation which maps triangle **P** onto triangle **Q**.

.....

.....

(2)

(b) Describe fully the single transformation which maps triangle **P** onto triangle **R**.

.....

.....

(3)

Q4

(Total 5 marks)

Turn over

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5. (a) Simplify, leaving your answers in index form,

(i) $7^5 \times 7^3$

.....

(ii) $5^9 \div 5^3$

.....

(2)

(b) Solve $\frac{2^9 \times 2^4}{2^n} = 2^8$

$n =$ .....

(2)

Q5

(Total 4 marks)

6. (a) Expand and simplify $3(4x - 5) - 4(2x + 1)$

.....

(2)

(b) Expand and simplify $(y + 8)(y + 3)$

.....

(2)

(c) Expand $p(5p^2 + 4)$

.....

(2)

Q6

(Total 6 marks)

Leave blank

7. A tunnel is 38.5 km long.

(a) A train travels the 38.5 km in 21 minutes.

Work out the average speed of the train.
Give your answer in km/h.

..... km/h
(3)

(b) To make the tunnel, a cylindrical hole 38.5 km long was drilled.
The radius of the cylindrical hole was 4.19 m.

Work out the volume of earth, in m^3, which was removed to make the hole.
Give your answer correct to 3 significant figures.

..... m^3
(3) **Q7**

(Total 6 marks)

Leave blank

8. (a) Shri invested 4500 dollars. After one year, he received 270 dollars interest.
Work out 270 as a percentage of 4500

..... %
(2)

(b) Kareena invested an amount of money at an interest rate of 4.5% per year.
After one year, she received 117 dollars interest.
Work out the amount of money Kareena invested.

..... dollars
(2)

(c) Ravi invested an amount of money at an interest rate of 4% per year.
At the end of one year, interest was added to his account and the total amount in his account was then 3328 dollars.
Work out the amount of money Ravi invested.

..... dollars
(3)

Q8

(Total 7 marks)

Leave blank

9. (a) Solve $5x - 4 = 2x + 7$

$x =$ .....

(2)

(b) Solve $\frac{7-2y}{4} = 2y + 3$

$y =$ .....

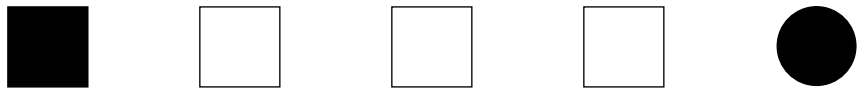
(4)

(Total 6 marks)

Q9

Leave blank

10. Here are five shapes.



Four of the shapes are squares and one of the shapes is a circle.
One square is black.
Three squares are white.
The circle is black.
The five shapes are put in a bag.

(a) Jasmine takes a shape at random from the bag 150 times.
She replaces the shape each time.

Work out an estimate for the number of times she will take a white square.

.....

(3)

(b) Alec takes a shape at random from the bag and does **not** replace it.
Bashir then takes a shape at random from the bag.

Work out the probability that

(i) they both take a square,

.....

(ii) they take shapes of the same colour.

.....

(5) **Q10**

(Total 8 marks)

Leave blank

11.

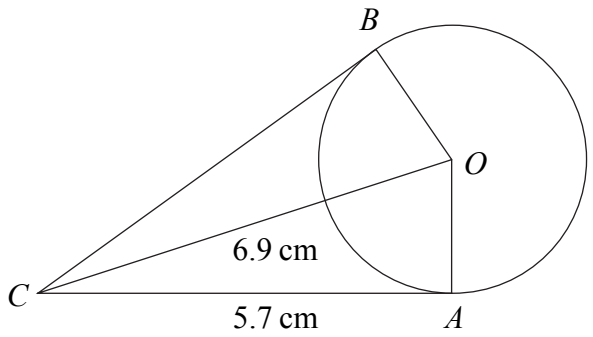


Diagram **NOT** accurately drawn

A and *B* are points on a circle, centre *O*.
The lines *CA* and *CB* are tangents to the circle.
CA = 5.7 cm.
CO = 6.9 cm.

(a) Give a reason why angle *CAO* = 90°.

.....

.....

(1)

(b) Calculate the perimeter of the kite *CAOB*.
Give your answer correct to 3 significant figures.

..... cm

(5)

Q11

(Total 6 marks)

Leave blank

12. The grouped frequency table gives information about the weights of 60 cows.

Weight (w kg)	**Frequency**
$100 < w \leqslant 200$	10
$200 < w \leqslant 300$	16
$300 < w \leqslant 400$	15
$400 < w \leqslant 500$	9
$500 < w \leqslant 600$	6
$600 < w \leqslant 700$	4

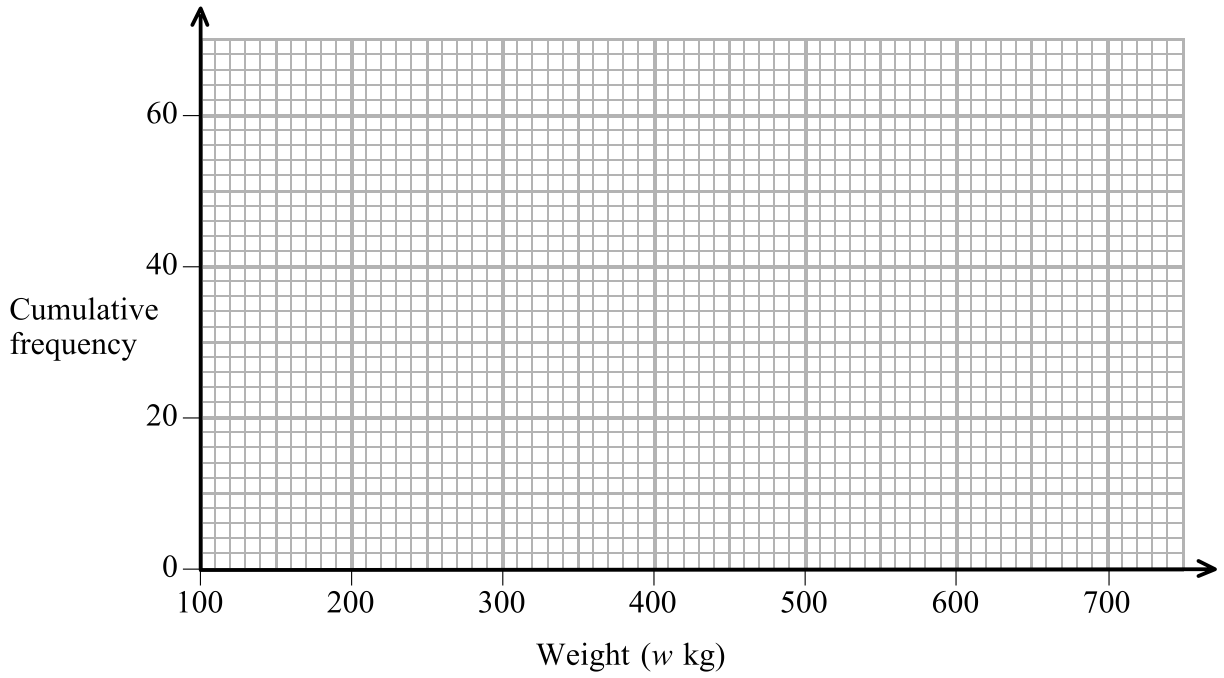
(a) Complete the cumulative frequency table.

Weight (w kg)	**Cumulative frequency**
$100 < w \leqslant 200$	
$100 < w \leqslant 300$	
$100 < w \leqslant 400$	
$100 < w \leqslant 500$	
$100 < w \leqslant 600$	
$100 < w \leqslant 700$	

(1)

Leave blank

(b) On the grid, draw the cumulative frequency graph for your table.



(2)

(c) Use your graph to find an estimate for the number of cows that weighed more than 430 kg.
Show your method clearly.

.....

(2) **Q12**

(Total 5 marks)

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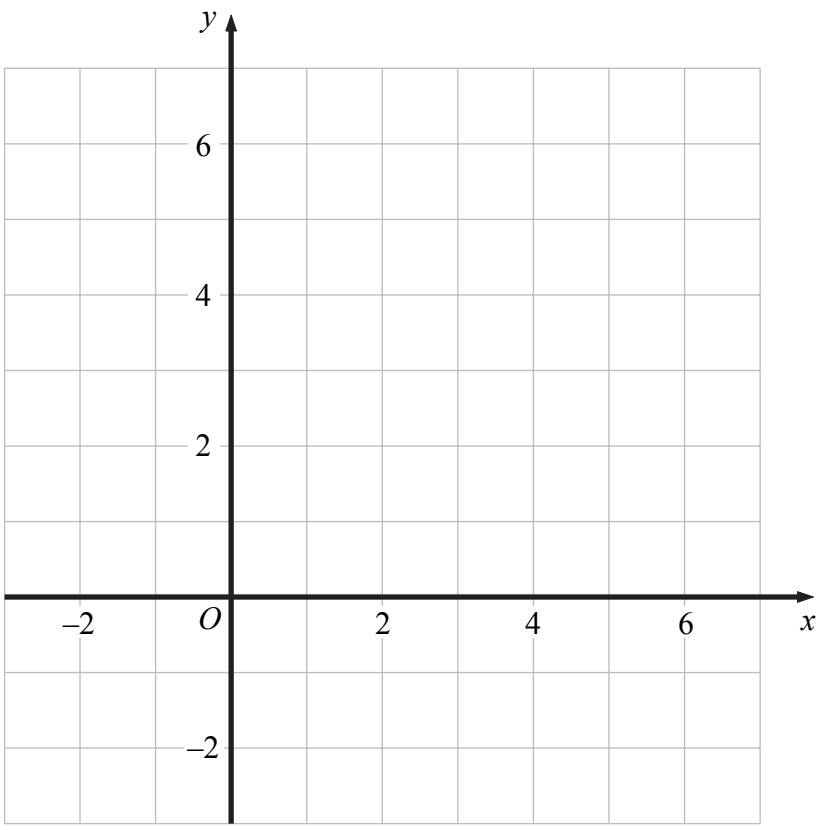
13. Show, by shading on the grid, the region which satisfies all three of these inequalities.

$$y \leqslant 5 \qquad y \leqslant 2x \qquad y \geqslant x + 1$$

Label your region **R**.



Q13

(Total 4 marks)

Leave blank

14. (a) Make r the subject of the formula $A = \pi r^2$, where r is positive.

$r =$ .....

(2)

The area of a circle is 14 cm^2, correct to 2 significant figures.

(b) (i) Work out the lower bound for the radius of the circle.
Write down all the figures on your calculator display.

..... cm

(ii) Give the radius of the circle to an appropriate degree of accuracy.
You must show working to explain how you obtained your answer.

..... cm

(4)

Q14

(Total 6 marks)

Leave blank

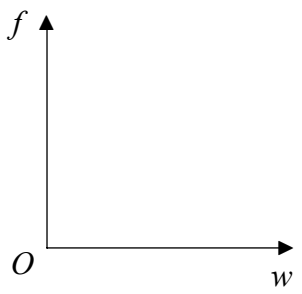
15. The frequency, f kilohertz, of a radio wave is inversely proportional to its wavelength, w metres.

When $w = 200$, $f = 1500$

(a) (i) Express f in terms of w.

$f =$ .....

(ii) On the axes, sketch the graph of f against w.



(4)

(b) The wavelength of a radio wave is 1250 m.
Calculate its frequency.

..... kilohertz

(2)

Q15

(Total 6 marks)

Leave blank

16. PQR is a triangle.
E is the point on PR such that $PR = 3PE$.
F is the point on QR such that $QR = 3QF$.

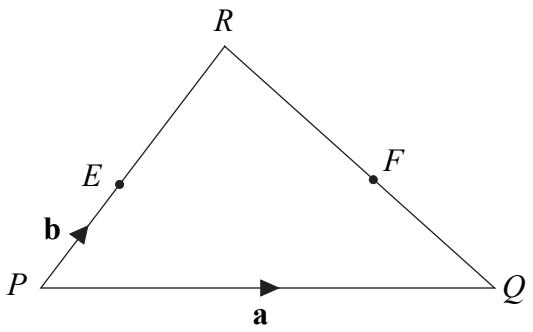


Diagram **NOT** accurately drawn

$\overrightarrow{PQ} = \mathbf{a}$, $\overrightarrow{PE} = \mathbf{b}$.

(a) Find, in terms of **a** and **b**,

(i) $\overrightarrow{PR}$

.....

(ii) $\overrightarrow{QR}$

.....

(iii) $\overrightarrow{PF}$

.....

(3)

(b) Show that $\overrightarrow{EF} = k\,\overrightarrow{PQ}$ where k is an integer.

(2)

Q16

(Total 5 marks)

Leave blank

17. A curve has equation $y = x^2 + \frac{16}{x}$

The curve has one turning point.

Find $\frac{dy}{dx}$ and use your answer to find the coordinates of this turning point.

.....

Q17

(Total 4 marks)

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18.

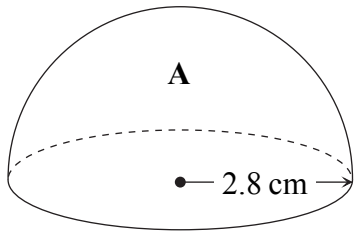

Diagram **NOT** accurately drawn

A solid hemisphere **A** has a radius of 2.8 cm.

(a) Calculate the **total** surface area of hemisphere **A**.
Give your answer correct to 3 significant figures.

..... cm^2
(3)

A larger solid hemisphere **B** has a **volume** which is 125 times the volume of hemisphere **A**.

(b) Calculate the **total** surface area of hemisphere **B**.
Give your answer correct to 3 significant figures.

..... cm^2
(3) **Q18**

(Total 6 marks)

PLEASE TURN OVER FOR QUESTION 19

Leave blank

19. Solve the simultaneous equations

$$y = 3x - 1$$

$$x^2 + y^2 = 5$$

.....

Q19

(Total 6 marks)

TOTAL FOR PAPER: 100 MARKS

END