

CAMBRIDGE INTERNATIONAL MATHEMATICS

Paper 6 (Extended) SPECIMEN MARK SCHEME 0607/06 For Examination from 2010

1 hour 30 minutes

MAXIMUM MARK: 40

This document consists of 5 printed pages and 1 blank page.



UNIVERSITY of CAMBRIDGE International Examinations

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TYPES OF MARK

- M marks are given for a correct method.
- A marks are given for an accurate answer following a correct method.
- **B** marks are given for a correct statement or step.
- **D** marks are given for clear and appropriately accurate drawing.
- **P** marks are given for accurate plotting of points.
- E marks are given for correctly explaining or establishing a given result.
- C marks are given for clear communication (Papers 5 and 6 only).
- **R** marks are given for appropriate reasoning (Papers 5 and 6 only).

ABBREVIATIONS

- ft Follow through
- oe Or equivalent
- soi Seen or implied
- www Without wrong working

A Investigation

1	(a)		$\frac{3}{24} + \frac{4}{24} = \frac{7}{24}$	AR1	(both accuracy required)	&	reasons	are
	(b)		$\frac{2}{12} + \frac{3}{12} = \frac{5}{12}$	AR1				
2	(a)		$\frac{1}{3} + \frac{1}{6} = \frac{2}{6} + \frac{1}{6} = \frac{3}{6} = \frac{1}{2}$	R1				
	(b)		$\frac{1}{3} = \frac{1}{4} + \frac{1}{12}$	B1				
	(c)		$\frac{1}{4} = \frac{1}{5} + \frac{1}{20}$	B2				
			$\frac{1}{5} = \frac{1}{6} + \frac{1}{30}$ $\frac{1}{6} = \frac{1}{7} + \frac{1}{42}$ $= \frac{1}{8} + \frac{1}{56}$	B1	for three correct			
	(d)		$\frac{1}{99} = \frac{1}{100} + \frac{1}{9900}$	B1				
	(e)		$\frac{1}{n} = \frac{1}{n+1} + \frac{1}{n(n+1)}$	B2	B1 for $\frac{1}{x} + \frac{1}{nx}$			
3	(a)		$\frac{2}{3} = 2 \times \frac{1}{3} = 2\left(\frac{1}{4} + \frac{1}{12}\right) = \frac{2}{4} + \frac{2}{12} = \frac{1}{2} + \frac{1}{6}$	R2				
	(b)	(i)	$\frac{2}{5} = 2\left(\frac{1}{6} + \frac{1}{30}\right) = \frac{1}{3} + \frac{1}{15}$	AR1				
		(ii)	$\frac{2}{7} = 2\left(\frac{1}{8} + \frac{1}{56}\right) = \frac{1}{4} + \frac{1}{28}$	AR1				
	(c)	(i)	$\frac{3}{8} = 3\left(\frac{1}{9} + \frac{1}{72}\right) = \frac{1}{3} + \frac{1}{24}$	AR1				
		(ii)	$\frac{4}{11} = 4\left(\frac{1}{12} + \frac{1}{132}\right) = \frac{1}{3} + \frac{1}{33}$	AR1				

4	(a)		Multiply $\frac{a}{xy} = \frac{1}{kx} + \frac{1}{ky}$ by kxy $\frac{akxy}{xy} = \frac{kxy}{x} + \frac{kxy}{y}$ (M1) $\Rightarrow ak = y + x$ $\Rightarrow k = \frac{x + y}{a}$	M1	
	(b)	(i)	$\frac{1}{6} + \frac{1}{10} = \frac{5}{30} + \frac{3}{30} = \frac{8}{30} = \frac{4}{15}$	C1	
		(ii)	x = 3 and $y = 5$ (or vice versa) in which case $k = \frac{5+3}{4} = 2$	B1	
		(iii)	x = 1 and $y = 15$ (or vice versa) in which case $k = \frac{15+1}{4} = 4$ and $\frac{4}{15} = 4$		
			$\frac{1}{4} + \frac{1}{60}$	B2	
5			Taking $x = 1$ and $y = 20$ gives $k = 7$ and $\frac{3}{20} = \frac{1}{7} + \frac{1}{140}$	B1	
			Taking $x = 2$ and $y = 10$ gives $k = 4$ and $\frac{3}{20} = \frac{1}{8} + \frac{1}{40}$	B1	
			Taking $x = 4$ and $y = 5$ gives $k = 3$ and $\frac{3}{20} = \frac{1}{12} + \frac{1}{15}$	B1	

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6	(a)	$1 = \frac{1}{2} + \frac{1}{2} = \frac{1}{2} + \frac{1}{3} + \frac{1}{6}$ using the pattern in part 2. $1 = \frac{1}{2} + \frac{1}{4} + \frac{1}{4}$	B1	
	(b)	In the first result, breaking down $\frac{1}{3}$	B1	no penalty if missing
		gives $1 = \frac{1}{2} + \frac{1}{4} + \frac{1}{12} + \frac{1}{6}$ breaking down $\frac{1}{6}$ gives $1 = \frac{1}{2} + \frac{1}{3} + \frac{1}{7} + \frac{1}{42}$	B1	
		OR	B1	
		$1 = \frac{1}{2} + \frac{1}{3} + \frac{1}{10} + \frac{1}{15}$ using the method in question 4, with $x = 2$ and $y = 3$. In the second result, breaking down $\frac{1}{4}$ gives $1 = \frac{1}{2} + \frac{1}{4} + \frac{1}{5} + \frac{1}{20}$	B1	
		For clear communication and reasoning throughout part A award C2		

Total: 31 marks scaled down to 25.

B Modelling

1			Suitable scales chosen Correct plots	D1D1 P2	P1 for 1 or 2 incorrect.
2	(a)		T = 40 is incorrect. It should be 36.	B1	
	(b)		T = 0.3 S	M1 A1	correct form
3			n = 2 $B = 0.01 S^2$	B1 A1	
4	(a)		$D = 0.3S + 0.01 S^2$	B1	
	(b)	(i)	40 metres	A1A1	(units required)
		(ii)	At 30 km/h $D = 18$ metres	A1	
			% reduction $=\frac{22}{40}=55\%$.	A1	(follow through)
5	(a)		braking distance = $180 - \text{thinking}$ distance at 100 km/h = $180 - 30 = 150$ metres. So $k \ 100^2 = 150 \Rightarrow k = 0.015$ $D = 0.3S + 0.015 \ S^2$	M1 A1	
	(b)		Solve $0.3S + 0.015 S^2 = 88$ 67.2 km/h using graphics calculator.	M1 A1	
			For clear communication and reasoning throughout part B award C2.		

Total: 20 marks scaled down to 15.

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