

	-	RSITY OF CAMBRIDGE I tional General Certificate o	NTERNATIONAL EXAMINATI	MAN HIEMER BADE IS COL
CANDIDATE NAME				
CENTRE NUMBER			CANDIDATE NUMBER	
MATHEMATIC	s			0581/43
Paper 4 (Extended)			Oct	ober/November 2013
				2 hours 30 minutes
Candidates and	swer on th	e Question Paper.		
Additional Mate	erials:	Electronic calculator Tracing paper (optional)	Geometrical instrume	ents

## **READ THESE INSTRUCTIONS FIRST**

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

## Answer all questions.

If working is needed for any question it must be shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place. For  $\pi$ , use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together. The number of marks is given in brackets [] at the end of each question or part question. The total of the marks for this paper is 130.



For (a) (i) In a camera magazine, 63 pages are used for adverts. Examiner's number of pages of adverts: number of pages of reviews = 7:5. The ratio Use Calculate the number of pages used for reviews. (ii) In another copy of the magazine, 56 pages are used for reviews and for photographs. number of pages of reviews: number of pages of photographs = 9:5. The ratio Calculate the number of pages used for photographs. (iii) One copy of the magazine costs \$4.90. An annual subscription costs \$48.80 for 13 copies. Calculate the percentage discount by having an annual subscription. Answer(a)(iii) ...... % [3]

(b) In a car magazine, 25% of the pages are used for selling second-hand cars,  $62\frac{1}{2}$ % of the **remaining** pages are used for features, and the other 36 pages are used for reviews.

Work out the total number of pages in the magazine.

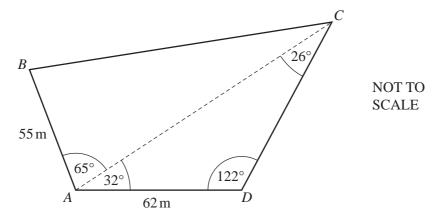
*Answer(b)* ..... [4]

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2 A field, *ABCD*, is in the shape of a quadrilateral. A footpath crosses the field from *A* to *C*.



(a) Use the sine rule to calculate the distance AC and show that it rounds to 119.9 m, correct to 1 decimal place.

Answer(a)

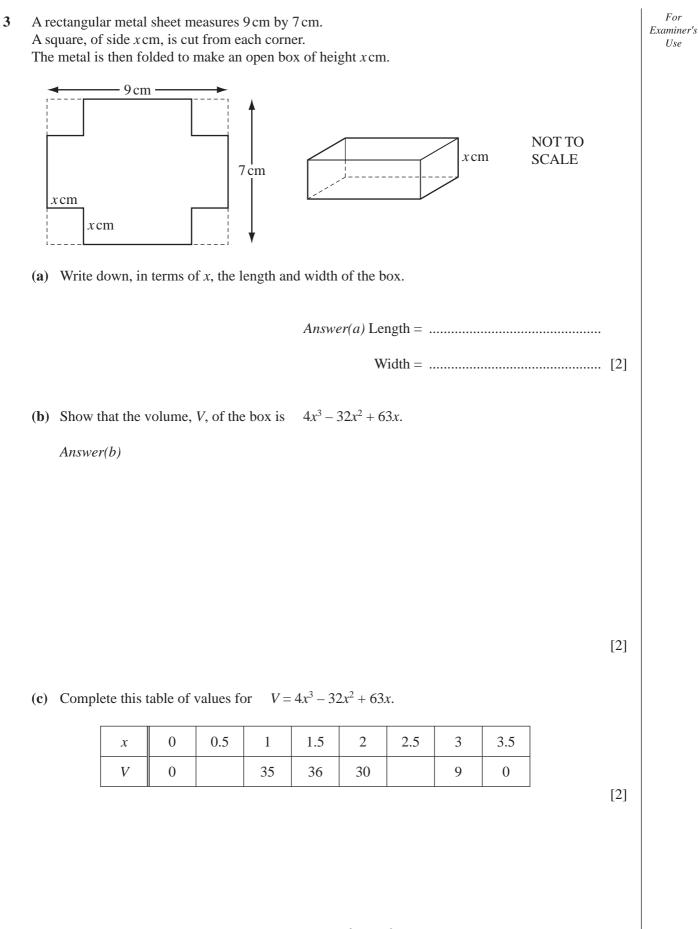
(**b**) Calculate the length of *BC*.

 $Answer(b) BC = \dots m [4]$ 

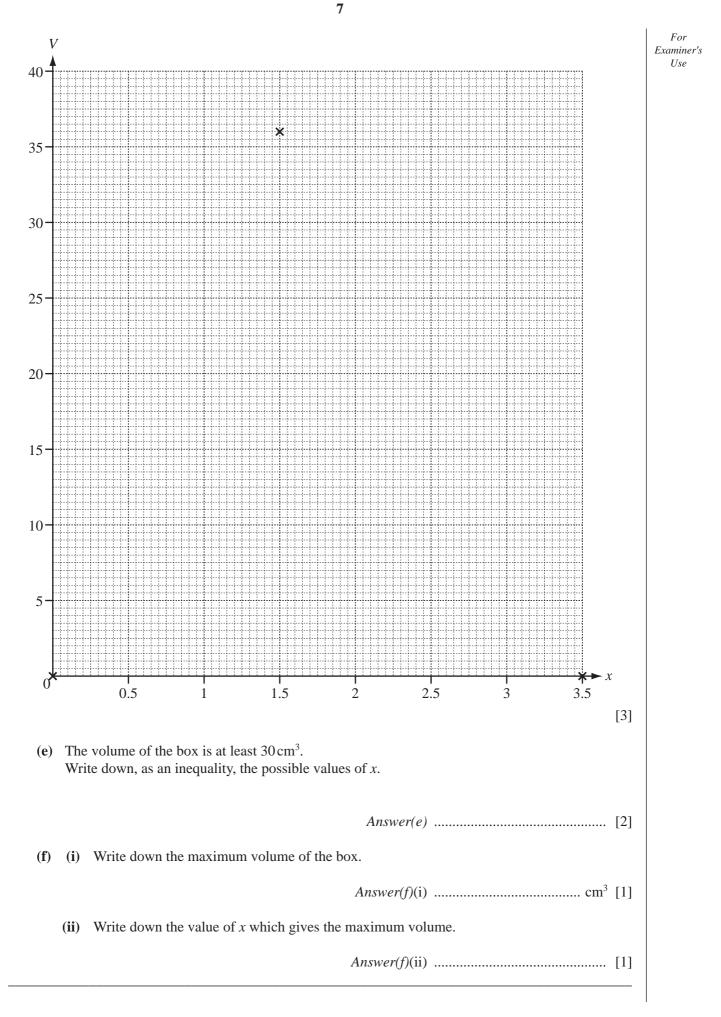
[3]

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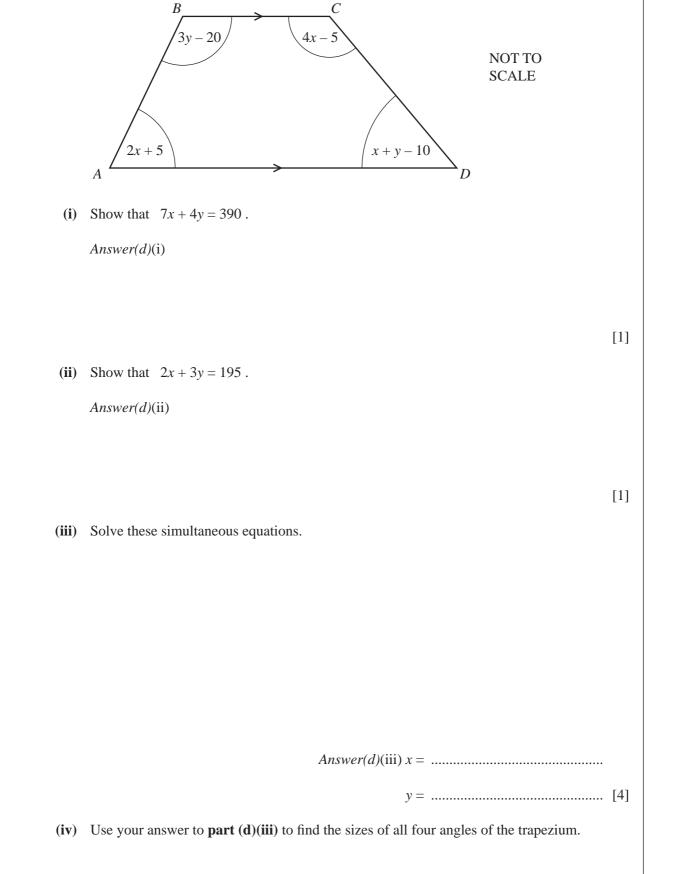
(0)	Calculate the area of triangle <i>ACD</i> .		For Examiner Use
		<i>Answer</i> ( <i>c</i> ) $m^2$ [2]	
( <b>d</b> )	The field is for sale at \$4.50 per square metre.		
	Calculate the cost of the field.		
		<i>Answer</i> ( <i>d</i> ) \$[3]	



(d) On the grid opposite, draw the graph of  $V = 4x^3 - 32x^2 + 63x$  for  $0 \le x \le 3.5$ . Three of the points have been plotted for you.



4	(a)	One angle of an isosceles triangle is 48°.	For Examiner's
		Write down the possible pairs of values for the remaining two angles.	Use
		<i>Answer(a)</i> and	
		and [2]	
	(b)	Calculate the sum of the interior angles of a pentagon.	
		Answer(b)	
	(c)	Calculate the sum of the angles <i>a</i> , <i>b</i> , <i>c</i> , <i>d</i> , <i>e</i> , <i>f</i> and <i>g</i> shown in this diagram.	
		a	
		NOT TO	
		<i>f</i> SCALE	
		$e^{-d}$	
		Answer(c)	



Answer(d)(iv) ...... , ...... , ...... , ...... [1]

(d) The trapezium, *ABCD*, has four angles as shown.

All the angles are in degrees.

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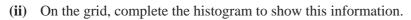
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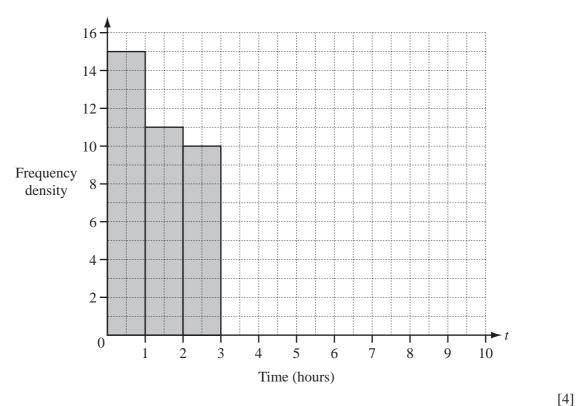
5 (a) 80 students were asked how much time they spent on the internet in one day. This table shows the results.

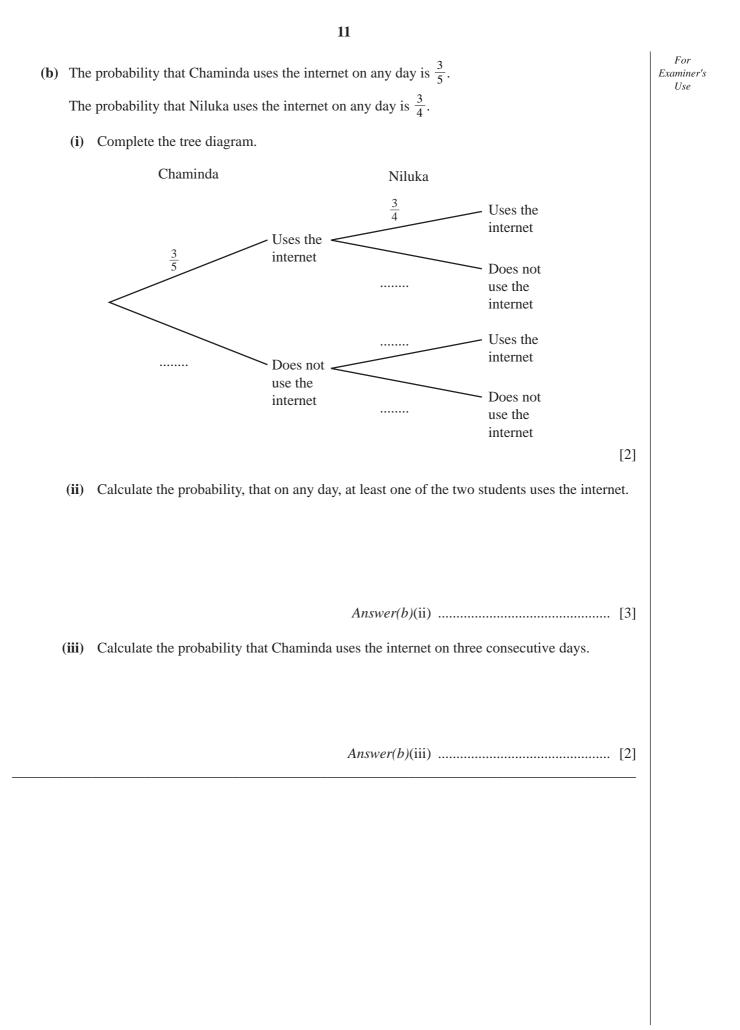
Time ( <i>t</i> hours)	$0 < t \le 1$	$1 < t \le 2$	$2 < t \le 3$	$3 < t \le 5$	$5 < t \le 7$	$7 < t \le 10$
Number of students	15	11	10	19	13	12

(i) Calculate an estimate of the mean time spent on the internet by the 80 students.



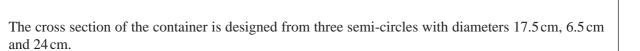


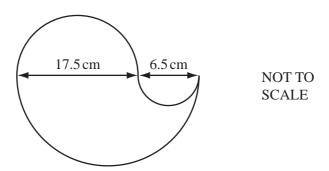




6 Sandra has designed this open container. The height of the container is 35 cm.

35 cm





(a) Calculate the area of the cross section of the container.

Answer(a) ......  $cm^2$  [3]

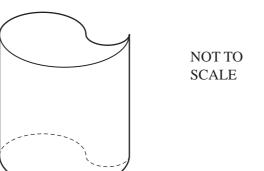
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(b) Calculate the external surface area of the container, including the base.

Answer(b) .....  $cm^2$  [4]



- 13 For (c) The container has a height of  $35 \,\mathrm{cm}$ . Examiner's UseCalculate the capacity of the container. Give your answer in litres. Answer(c) ..... litres [3] (d) Sandra's container is completely filled with water. All the water is then poured into another container in the shape of a cone. The cone has radius 20 cm and height 40 cm. 20 cm NOT TO **SCALE** 40 cm (i) The diagram shows the water in the cone. Show that  $r = \frac{h}{2}$ .
  - [1]

(ii) Find the height, *h*, of the water in the cone. [The volume, *V*, of a cone with radius *r* and height *h* is  $V = \frac{1}{3}\pi r^2 h$ .]

Answer(d)(ii)  $h = \dots$  cm [3]

Answer(d)(i)

			14	
7	(a) The	e co-ordinates of $P$ are $(-4, -4)$ and the co-	ordinates of $Q$ are (8, 14).	For Examiner's Use
	(i)	Find the gradient of the line <i>PQ</i> .		0.50
			A	1
	( <b>ii</b> )	Find the equation of the line PQ.	<i>Answer(a)</i> (i)	]
			Answer(a)(ii)	]
	(iii)	Write $\overrightarrow{PQ}$ as a column vector.		
			Answer(a)(iii) $\overrightarrow{PQ} = \begin{pmatrix} \\ \end{pmatrix}$ [1]	]
	(iv)	Find the magnitude of $\overrightarrow{PQ}$ .		
			<i>Answer(a)</i> (iv)	]

	15	
)		For Examiner's Use
	A NOT TO SCALE Aa O SCALE	
	In the diagram, $\overrightarrow{OA} = 4\mathbf{a}$ and $\overrightarrow{OB} = 3\mathbf{b}$ .	
	<i>R</i> lies on <i>AB</i> such that $\overrightarrow{OR} = \frac{1}{5}(12\mathbf{a} + 6\mathbf{b})$ .	
	T is the point such that $\overrightarrow{BT} = \frac{3}{2}\overrightarrow{OA}$ .	
	(i) Find the following in terms of <b>a</b> and <b>b</b> , giving each answer in its simplest form.	
	(a) $\overrightarrow{AB}$	
	Answer(b)(i)(a) $\overrightarrow{AB} = \dots$ [1]	
	(b) $\overrightarrow{AR}$	
	Answer(b)(i)(b) $\overrightarrow{AR} =$	
	(c) $\overrightarrow{OT}$	
	Answer(b)(i)(c) $\overrightarrow{OT} = \dots$ [1]	
(	(ii) Complete the following statement.	
	The points <i>O</i> , <i>R</i> and <i>T</i> are in a straight line because	
(	iii) Triangle <i>OAR</i> and triangle <i>TBR</i> are similar.	
	Find the value of $\frac{\text{area of triangle } TBR}{\text{area of triangle } OAR}$ .	

**(b**)

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8 (a) Rearrange  $s = ut + \frac{1}{2}at^2$  to make *a* the subject.

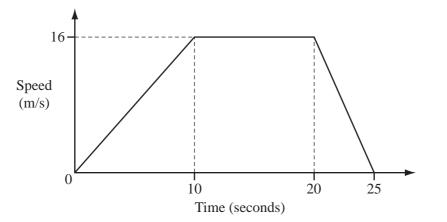
 $Answer(a) a = \dots [3]$ 

(b) The formula v = u + at can be used to calculate the speed, v, of a car.

u = 15, a = 2 and t = 8, each correct to the nearest integer.

Calculate the upper bound of the speed v.

(c) The diagram shows the speed-time graph for a car travelling between two sets of traffic lights.

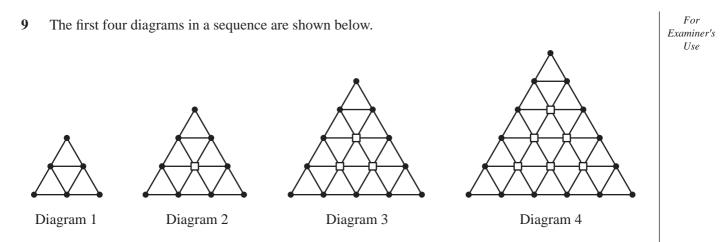


- (i) Calculate the deceleration of the car for the last 5 seconds of the journey.
  - *Answer*(*c*)(i) .....  $m/s^2$  [1]
- (ii) Calculate the average speed of the car between the two sets of traffic lights.

*Answer*(*c*)(ii) ..... m/s [4]

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The diagrams are made from dots  $(\bullet)$  and squares  $(\Box)$  joined by lines.

(a) Complete the table.

Diagram	1	2	3	4	5	n	
Number of dots	6	9	12				
Number of squares	0	1	3			$\frac{1}{2}n(n-1)$	
Number of triangles	4	9	16				
Number of lines	9	18	30	45	63	$\frac{3}{2}(n+1)(n+2)$	
	•						

(b) Which diagram has 360 lines?

- (c) The total number of lines in the first *n* diagrams is
  - $\frac{1}{2}n^3 + pn^2 + qn.$
  - (i) When n = 1, show that  $p + q = 8\frac{1}{2}$ .

Answer(c)(i)

[1]

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(ii) By choosing another value of n and using the equation in **part** (c)(i), find the values of p and q.

 $Answer(c)(ii) p = \dots$ 

Question 10 is printed on the next page.

					20					
)	(a)	Simplif	$\frac{x^2 - 3x}{x^2 - 9}$						i	
						Answer(a)		. [3]		
	(b)	Solve.	$\frac{15}{x} - \frac{20}{x+1} =$	2						

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