

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS  
International General Certificate of Secondary Education

**MARK SCHEME for the October/November 2011 question paper  
for the guidance of teachers**

**0581 MATHEMATICS**

**0581/41**

Paper 4 (Extended), maximum raw mark 130

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### Abbreviations

cao	correct answer only
cso	correct solution only
dep	dependent
ft	follow through after error
isw	ignore subsequent working
oe	or equivalent
SC	Special Case
www	without wrong working
art	anything rounding to
soi	seen or implied

Qu.	Answers	Mark	Part Marks
<b>1</b>	<b>(a) (i)</b> 4950	<b>2</b>	<b>M1</b> for $9000 \times 0.55$ oe
	<b>(ii)</b> 9 : 11	<b>1</b>	Accept 1 : 1.22 or 0.818 : 1 After 4050 in <b>(a)(i)</b> allow <b>SC1</b> for 11 : 9 etc
<b>(b)</b>	1504	<b>1</b>	
	564	<b>1</b>	
	188	<b>1</b>	After 0 scored <b>M1</b> for $2256 \div (8 + 3 + 1)$ soi
<b>(c) (i)</b>	6847.99 or 6848 or 6850	<b>3</b>	<b>M2</b> for $15000 \times 0.77^3$ oe (6847. (..)ww imp <b>M2</b> ) or <b>M1</b> for $15000 \times 0.77^2$ oe soi (8893.5) After 0 scored <b>SC1</b> for art 27913 or 27910 or 27900
	<b>(ii)</b> 54.3 (54.33 to 54.35)	<b>3ft</b>	ft their $(15000 - \text{their } \mathbf{(c)(i)}) / 15000 \times 100$ to 3sf or better <b>but not</b> for negative answer or from 4650 in <b>(c)(i)</b> leading to 69% <b>M2</b> for $1 - 0.77^3$ (0.543..) or their $(15000 - \text{their } \mathbf{(c)(i)}) / 15000 (\times 100)$ or <b>SC2ft</b> their $\mathbf{(c)(i)} / 15000 \times 100$ correctly evaluated (45.65 to 45.67 or 45.7) or <b>M1</b> for $0.77^3$ (0.4565..) or their $\mathbf{(c)(i)} / 15000$

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<b>2</b>	<p>(a) 0, 1, 2, 3</p> <p>(b) <math>\frac{x-2}{x-5}</math> www final answer</p> <p>(c) (i) <math>5(x+1) + 2(x-3) = 3(x+1)(x-3)</math> oe <math>x^2 - 3x + x - 3</math> or better seen <math>3x^2 - 13x - 8 = 0</math></p> <p>(ii) <math>\frac{-(-13) \pm \sqrt{(-13)^2 - 4(3)(-8)}}{2(3)}</math></p> <p>4.88 and -0.55 cao</p>	<p><b>3</b> Additional values count as errors <b>B2</b> for one error/omission or <b>B1</b> for two errors/omissions After <b>B0</b>, <b>M2</b> for <math>-1 &lt; x \leq 3.5</math> seen, allow <math>7/2</math> for 3.5 or <b>M1</b> for <math>-1 &lt; x</math> or <math>x \leq 3.5</math> or <math>x = -1</math> <b>and</b> <math>x = 3.5</math> Allow <b>M2</b> for <math>0 \leq x &lt; 4</math> or <b>M1</b> for <math>x \geq 0</math> or <math>x &lt; 4</math></p> <p><b>4</b> <b>M3</b> for <math>\frac{(x+5)(x-2)}{(x+5)(x-5)}</math> or <b>M2</b> for <math>(x+5)(x-2)</math> seen or <b>M1</b> for <math>(x+a)(x+b)</math> where <math>ab = -10</math> or <math>a + b = 3</math> and <b>M1</b> for <math>(x+5)(x-5)</math> seen</p> <p><b>M1</b> Allow if still over common denominator</p> <p><b>B1</b> Allow <math>x^2 - 2x - 3</math> seen or <math>3x^2 - 9x + 3x - 9</math> or better seen</p> <p><b>E1</b> With no errors seen and brackets correctly expanded on both sides</p> <p><b>B1</b> In square root <b>B1</b> for <math>(-13)^2 - 4(3)(-8)</math> or better (265)</p> <p>If in form <math>\frac{p + \sqrt{q}}{r}</math> or <math>\frac{p - \sqrt{q}}{r}</math>,</p> <p><b>B1</b> for <math>-(-13)</math> and <math>2(3)</math> or better</p> <p><b>B1B1</b> <b>SC1</b> for 4.88 and -0.55 seen or -0.5 and 4.9 or -0.546... and 4.879 to 4.880</p>
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<p><b>3</b></p>	<p>(a) (i) <math>1.6 &lt; h \leq 1.7</math></p> <p>(ii) <math>\{1.35 \times 4 + 1.45 \times 13 + 1.55 \times 33 + 1.65 \times 45 + 1.75 \times 19 + 1.85 \times 6\} \div 120</math></p> <p>1.62 or 1.616 to 1.617</p> <p>(b) (i) <math>\frac{6}{120}</math> oe</p> <p>(ii) <math>\frac{2147}{2380}</math> oe (0.902(1..))</p> <p>(c) (i) 95, 120</p> <p>(ii) Plots 7 points correctly exact or in correct square</p> <p>Curve or lines through 7 points</p> <p>(d) (i) 1.61 to 1.63</p> <p>(ii) 1.555 to 1.57</p>	<p><b>1</b></p> <p><b>M3</b></p> <p><b>A1</b></p> <p><b>1</b></p> <p><b>3</b></p> <p><b>1</b></p> <p><b>P2ft</b></p> <p><b>C1ft</b></p> <p><b>1ft</b></p> <p><b>1ft</b></p>	<p>Condone alt. notation used for class</p> <p>(194/120)</p> <p><b>M1</b> for mid-values soi (allow one slip) and <b>M1</b> for use of <math>\sum fx</math> with <math>x</math> in correct interval (allow one more slip) and <b>M1</b> depend on 2nd <b>M</b> for dividing by 120</p> <p>www4</p> <p>Accept dec/% to 3 sf or better but not ratio isw cancelling/conversion (also for (ii))</p> <p><b>M2</b> for <math>\frac{k}{120} \times \frac{k-1}{119}</math> where <math>\frac{k}{120}</math> is 1 – their (b)(i) or if <math>k = 114</math> or <b>M1</b> for 1 – their (b)(i) or for 114/120 seen After 0 scored <b>SC2</b> for ans 1/476 oe or <b>SC1</b> for <math>6/120 \times 5/119</math></p> <p><b>P1ft</b> for 5 or 6 correct plots</p> <p>ft their <b>increasing</b> curve within 1 mm of points</p> <p>ft their 60th reading on inc. curve to nearest 0.01</p> <p>ft their 36th reading on inc. curve</p>
<p><b>4</b></p>	<p>(a) (i) <math>2.7 \times \frac{20}{12}</math> oe = 4.5</p> <p>(ii) <math>1/3\pi \times 4.5^2 \times 20 - 1/3\pi \times 2.7^2 \times 12</math> or <math>(1 - (3/5)^3) \times 1/3\pi \times 4.5^2 \times 20</math> oe</p> <p>332.3 to 332.6 or 332 or 333</p> <p>(b) (i) <math>8^2 + (4.5 - 2.7)^2</math> oe</p> <p>sq root</p> <p>8.2</p> <p>(ii) 185 or 186 or 185.5 or 185.45 to 185.51</p>	<p><b>E2</b></p> <p><b>M3</b></p> <p><b>A1</b></p> <p><b>M1</b></p> <p><b>M1</b></p> <p><b>E1</b></p> <p><b>5</b></p>	<p><b>M1</b> for (SF =) 20/12 or 12/20 (but not from 2.7/4.5 or 4.5/2.7)</p> <p><b>M1</b> for <math>1/3\pi \times 4.5^2 \times 20</math> (424 ... or <math>135\pi</math>) and <b>M1</b> for <math>1/3\pi \times 2.7^2 \times 12</math> (91.6..or <math>29.16\pi</math>)</p> <p>e.g. Alt: <math>20^2 + 4.5^2</math> and <math>12^2 + 2.7^2</math></p> <p>Dep on 1st <b>M1</b> Alt: 20.5 – 12.3</p> <p>Other complete correct methods are <b>M2</b></p> <p>No errors seen</p> <p><b>M4</b> for <math>\pi \times 4.5 \times 20.5 - \pi \times 2.7 \times 12.3</math> or other complete correct method or <b>M3</b> for <math>\pi \times 4.5 \times 20.5</math> or <math>\pi \times 2.7 \times 12.3</math> (290 or <math>92.25\pi</math>) (104.3...or <math>33.21\pi</math>) or <b>B2</b> for (slant height of large cone =) 20.5 or (slant height of removed cone =) 12.3 or <b>M1</b> for <math>\sqrt{4.5^2 + 20^2}</math> or <math>\sqrt{2.7^2 + 12^2}</math> or <math>12/8 \times 8.2</math> oe or <math>20/8 \times 8.2</math> oe</p>

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5	<p>(a) 1, -1, 3.5</p> <p>(b) 10 correct points plotted</p> <p>Smooth curve through at least 8 points and correct shape</p> <p>(c) (i) -2.2 to -2.1 -0.65 to -0.45 2.5 to 2.7</p> <p>(ii) (<math>k &lt;</math>) -4 to -3.7  (<math>k &gt;</math>) 1.7 to 2</p> <p>(d) (i) Ruled line gradient 3 and <math>y</math>-intercept -2 over the range -1 to 3.5</p> <p>(ii) (<math>a =</math>) -12, (<math>b =</math>) 2</p> <p>(iii) 0.1 to 0.2 and 3.3 to 3.4 cao</p>	<p>1,1,1</p> <p>P3ft</p> <p>C1ft</p> <p>1ft</p> <p>1ft</p> <p>1ft</p> <p>1ft</p> <p>3</p> <p>1,1</p> <p>1,1</p>	<p>P2ft for 8 or 9 correct P1ft for 6 or 7 correct Allow points to be implied from curve</p> <p>Correct cubic shape, not ruled</p> <p>Correct or ft their <math>x</math> values</p> <p>If ft and more than 3 solns then 2 marks maximum</p> <p>Correct or ft their graph for <math>y</math> values at max and min</p> <p>After 0 scored SC1 for both correct but reversed</p> <p>B2 for correct but freehand or short or M1 for a ruled line of gradient 3 or passes through (0, -2) (but not <math>y = -2</math>)</p> <p>After 0, M1 for <math>x^3 - 6x - 6x - 2 + 4 (=0)</math> or better</p>
6	<p>(a) <math>120^2 + 95^2 - 2 \times 120 \times 95 \times \cos 77</math> 135.26 ... or 135.3</p> <p>(b) <math>(\sin B) = \frac{\text{their } 135 \times \sin 26}{79}</math>  48.5 to 48.7 isw 131 or 131.3 to 131.5 www4</p> <p>(c) (Angle <math>A =</math>) 22.5 to 22.7  'Path' / 79 = sin (their <math>A</math>) oe 30.2 to 30.5 www3</p> <p>(d) <math>\frac{1}{2} \times 120 \times 95 \times \sin 77</math> oe  Their area <math>\div 180</math> 30.8 to 30.9  30</p>	<p>M2</p> <p>E2</p> <p>M2</p> <p>A1</p> <p>B1ft</p> <p>B1ft</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>B1ft</p>	<p>M1 for implicit version</p> <p>A1 for 18295 to 18297</p> <p>M1 for <math>\frac{\sin B}{\text{their } 135} = \frac{\sin 26}{79}</math> oe</p> <p>ft for 180 - their 48.5 to 48.7 dep on sine rule or sine used</p> <p>ft 154 - their (b), also accept angle <math>B = 67.3</math> to 67.5 (ft their (b) - 64)</p> <p>Dep on B1 and their <math>A &lt; 90</math> eg <math>79 \cos 67.4</math></p> <p>(5554)</p> <p>Dep on area attempt</p> <p>ft their 30.8 to 30.9 truncated dep on at least M1 earned After M2 answer 30 www scores A1B1 Answer 30 ww scores 0</p>

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<b>7 (a)</b>	<b>(a) (i)</b> Reflection only $y = -2$	<b>B1</b>	Spoilt if extras
	<b>(ii)</b> Enlargement only $\frac{1}{2}$ (1, 4)	<b>B1</b> <b>B1</b>	Spoilt if extras
	<b>(iii)</b> Rotation only 90° clockwise oe Around (1, -3)	<b>B1</b> <b>B1</b> <b>B1</b>	Spoilt if extras Accept -90° or (+)270°
	<b>(b) (i)</b> Triangle at (-4, 4), (-1, 4), (-1, 5)	<b>2</b>	<b>B1</b> for translation of $\begin{pmatrix} -5 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 2 \end{pmatrix}$  After <b>B0</b> , <b>SC1</b> for translation of 5 small squares to the left and 2 small squares up
	<b>(ii)</b> Triangle at (4, 4), (1, 4), (4, 6)	<b>3</b>	<b>B1</b> for each of (4, 4) or (4, 6) plotted If no/wrong plots allow <b>SC2</b> for 3 correct coordinates shown in working or <b>SC1</b> for any 2 correct coordinates shown or <b>M1</b> for $\begin{pmatrix} 1 & 0 \\ 0 & 2 \end{pmatrix} \begin{pmatrix} 1 & 4 & 4 \\ 2 & 2 & 3 \end{pmatrix}$ shown
	<b>(c)</b> Stretch only (Factor) 2 $x$ -axis oe invariant	<b>B1</b> <b>B1</b> <b>B1</b>	Spoilt if extras

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8	<p>(a) (i) There are up to 5 large coaches oe</p> <p>(ii) <math>50x + 30y \geq 300</math> oe</p> <p>(b)</p> <p><math>x = 5</math> ruled  <math>x + y = 10</math> ruled  <math>5x + 3y = 30</math> ruled</p> <p>Correct region indicated cao</p> <p>(c) (i) 5 2</p> <p>(ii) 2950</p>	<p>1</p> <p>E2</p> <p>L1</p> <p>L1</p> <p>L2</p> <p>R1</p> <p>1</p> <p>1</p> <p>1ft</p>	<p>E.g. can't hire more than 5 large coaches  The maximum is 5 large coaches  The large coaches are less than or equal to 5</p> <p>No errors  Allow in words provided clear  e.g. 50 in large coaches and 30 in small coaches  must equal 300 seats or more  <b>M1</b> for associating 50 with <math>x</math> or large coaches  and 30 with <math>y</math> or small coaches</p> <p>Freehand lines –1 pen once.  All lines must be long enough to make full  boundary of their region accept dashed or solid  lines</p> <p><b>L1</b> for ruled line with intercepts at (0, 10)  or (6, 0) within 2mm by eye at intercepts  (extend if line is short)</p> <p>Allow if slight inaccuracy(s) in diagonal lines  Allow any clear indication of region</p> <p>After 5 and 2 in working ignore attempts to  calculate costs</p> <p>ft their <math>5 \times 450 +</math> their <math>2 \times 350</math> provided positive  integers</p>
9	<p>(a) (i) <math>2 \times 3 \times 3 \times 7</math> oe</p> <p>(ii) 18</p> <p>(iii) 504</p> <p>(b) 3.028 or 3.029 cao</p> <p>(c) <math>\pi r^2</math> their <math>h =</math> their <math>V</math></p> <p><math>(r^2 =) \frac{\text{their } V}{\pi \times \text{their } h}</math></p> <p>Sq root  Selects 555 or 554.99.. and 11.5  3.919 cao</p>	<p>2</p> <p>1</p> <p>2</p> <p>4</p> <p>M1</p> <p>M1</p> <p>M1</p> <p>B1</p> <p>A1</p>	<p><b>M1</b> for prime factors of 2,3,3,7 shown condone  1('s) shown as well for method only</p> <p><b>M1</b> for other multiples of 504  or <math>2 \times 2 \times 2 \times 3 \times 3 \times 7</math> oe shown  If (ii) and (iii) both correct but reversed allow  <b>SC1</b></p> <p><b>B3</b> for 3.0289(85...)  or <b>M1</b> for their 105/their 34  (their 105 in range 104 to 106 and their 34 in  range 33 to 35)  and <b>B1</b> for 104.5 or 34.5 or 34.499.. selected</p> <p>Where <math>V</math> is in range 540 to 560 and <math>h</math> is in range  11 to 13</p> <p>Implies previous method (15.36 implies <b>M2</b>)  If using 545 and 12.5 then 13.88 (leading to 3.73)  If using 550 and 12 then 14.59 (leading to 3.82)</p> <p>Dep on <b>M2</b>, can be implied from answers</p> <p>Indep</p> <p>If trials then 5 or 0</p>