CANDIDATE
NAME

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NUMBER

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MATHEMATICS (US) **0444/31**

Paper 3 (Core) **May/June 2012**

2 hours

Candidates answer on the Question Paper.

Additional Materials: Geometrical instruments
Electronic calculator

READ THESE INSTRUCTIONS FIRST

Write your Center number, candidate number and name on all the work you hand in.
Write in dark blue or black pen.
You may use a pencil for any diagrams or graphs.
Do not use staples, paper clips, highlighters, glue or correction fluid.
DO **NOT** WRITE IN ANY BARCODES.

Answer **all** questions.
If work is needed for any question it must be shown in the space provided.
Electronic calculators should be used.
If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant digits. Give answers in degrees to one decimal place.
For π, use either your calculator value or 3.142.

The number of points is given in parentheses [ ] at the end of each question or part question.
The total of the points for this paper is 104.

Write your calculator model in the box below.

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International Examinations

[Turn over

Formula List

Area, A, of triangle, base b, height h. $\qquad\qquad A = \dfrac{1}{2}bh$

Area, A, of circle, radius r. $\qquad\qquad A = \pi r^2$

Circumference, C, of circle, radius r. $\qquad\qquad C = 2\pi r$

Lateral surface area, A, of cylinder of radius r, height h. $\qquad\qquad A = 2\pi rh$

Surface area, A, of sphere of radius r. $\qquad\qquad A = 4\pi r^2$

Volume, V, of prism, cross-sectional area A, length l. $\qquad\qquad V = Al$

Volume, V, of cylinder of radius r, height h. $\qquad\qquad V = \pi r^2 h$

Volume, V, of sphere of radius r. $\qquad\qquad V = \dfrac{4}{3}\pi r^3$

1 **(a)** Vince and Wendy share $2000 in the ratio   Vince : Wendy = 19 : 21.

Calculate the amount of money that Vince receives.

Answer(a) $ .... [2]

(b) Wendy has $265 to spend on some chairs.
The chairs cost $37 each.

Work out the largest number of chairs she can buy.

Answer(b) .... [2]

(c) Wendy shares $200 between her three children Jake, Karl and Lana.

She gives 27% of the money to Jake and $\frac{2}{5}$ of the money to Karl.

Work out the amount of money she gives to Lana.
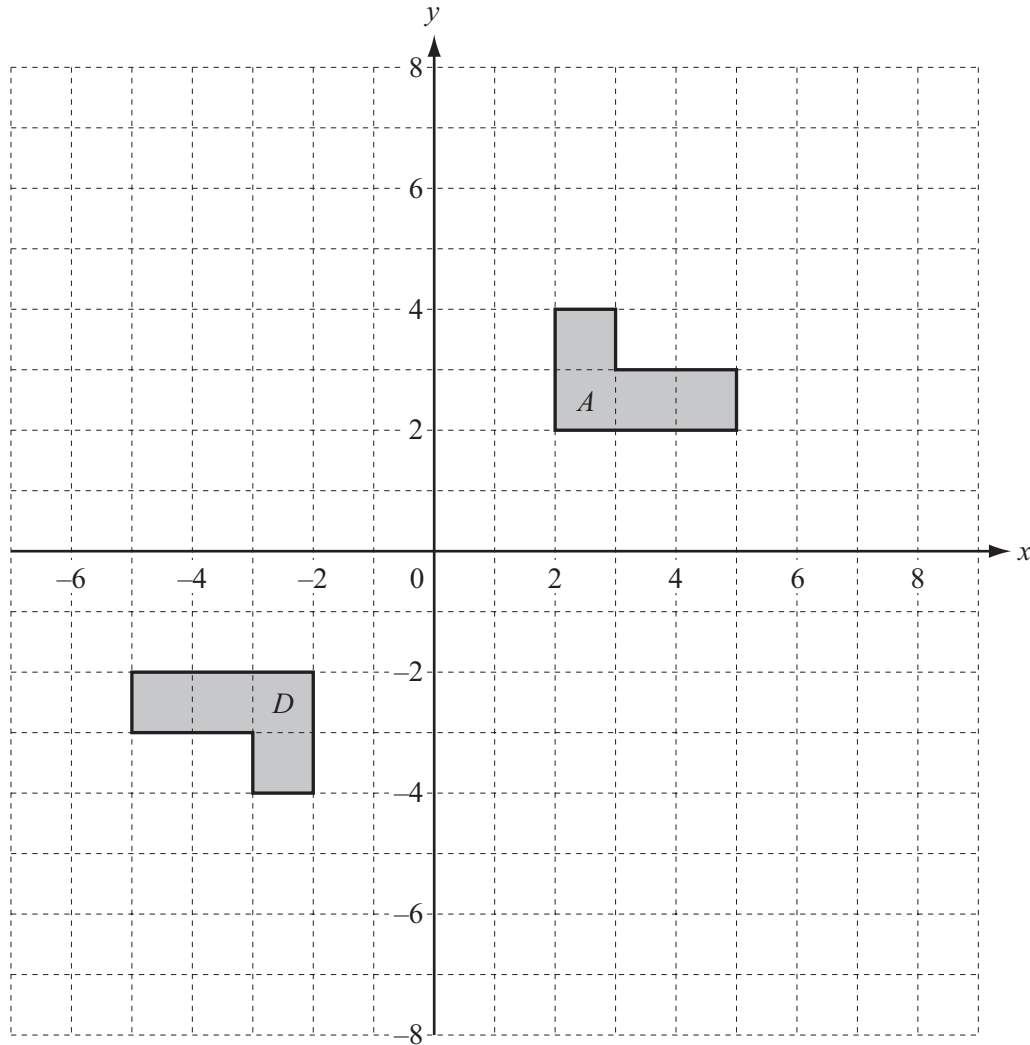
Answer(c) $ .... [3]

(d) Wendy invests $500 at a rate of 4% per year **compound** interest.

Calculate the total amount of **interest** she receives at the end of 2 years.
Give your answer correct to the nearest dollar.

Answer(d) $ .... [4]

2

Two shapes *A* and *D* are shown on the grid.

(a) **(i)** Reflect **shape *A*** in the line $x = 0$. Label this image ***B***. [2]

   (ii) Rotate **shape *A*** through 180° about (2, 4). Label this image ***C***. [2]

   (iii) Enlarge **shape *A*** with scale factor 2 and centre (3, 7). Label this image ***E***. [2]

(b) Describe fully the **single** transformation that maps **shape *D*** onto
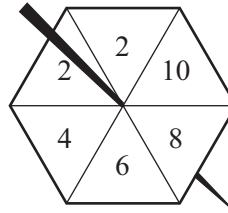
    (i) **shape *B*,**

       Answer(b)(i) .... [2]

   (ii) **shape *C*.**

       Answer(b)(ii) .... [2]

3 **(a)** Jon spins this 6-sided spinner.

The probability that the spinner lands on any of the six sides is equally likely.

Write down the probability that the spinner lands on

    (i) the number 6,

                        Answer(a)(i) .... [1]

   (ii) a prime number,

                        Answer(a)(ii) .... [1]

  (iii) a number less than 11.

                        Answer(a)(iii) .... [1]
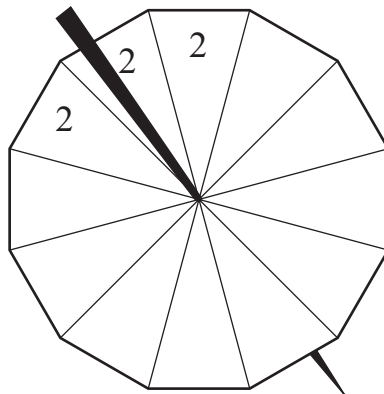
(b) Felix has a 12-sided spinner with the numbers 2, 4, 5, 7 and 9 written on it.
It is equally likely to land on any side.
The table shows the probability of the spinner landing on each number.

Number on spinner	2	4	5	7	9
Probability	$\frac{1}{4}$	$\frac{1}{3}$	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{12}$

The diagram of the spinner has been completed for the number 2.

Complete the diagram for the numbers 4, 5, 7 and 9.

                                                          [3]

(c) Felix says that his spinner is more likely to land on a 2 than Jon's spinner.
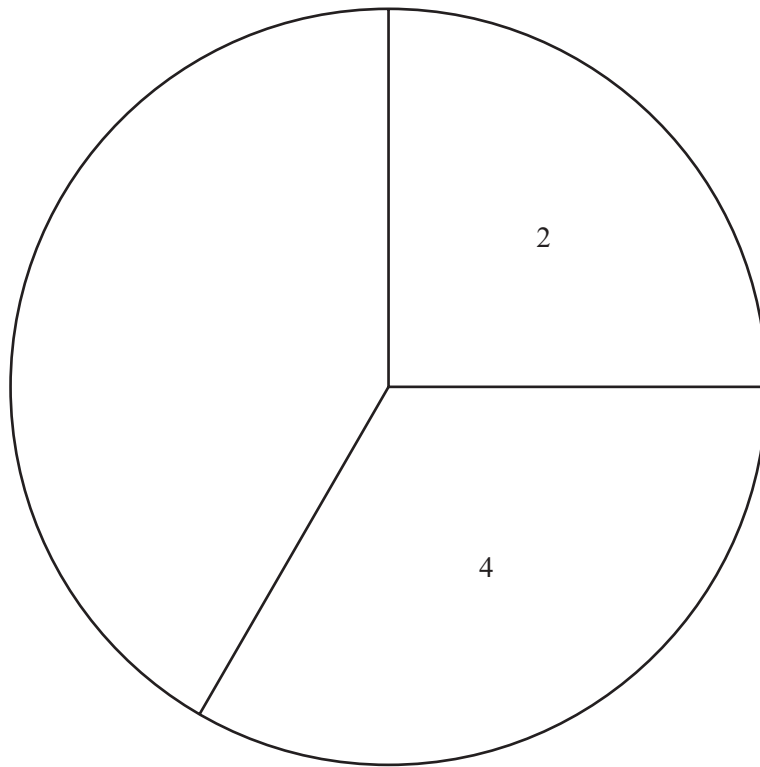
    Explain why he is wrong.

    Answer(c) ....

    .... [1]

(d) Felix spins his 12-sided spinner 60 times and records the results.

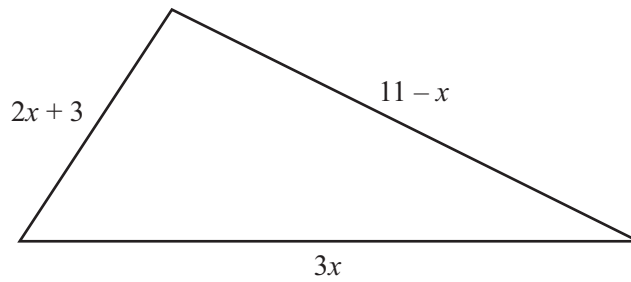| Number on spinner	Frequency	Pie chart sector angle
2	15	90°
4	20	120°
5	5	30°
7	12	
9	8	

(i) Complete the table by working out the sector angles for the numbers 7 and 9 . [3]

(ii) Complete the pie chart.

[2]

4 In this question all the measurements are in centimetres.

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The diagram shows a triangle with sides of length $2x + 3$, $11 - x$ and $3x$.

(a) Explain why x must be less than 11.

Answer(a) ....

.... [1]

(b) Write down an expression, in terms of x, for the perimeter of the triangle.
Give your answer in its simplest possible form.

Answer(b) .... [2]

(c) The perimeter of the triangle is 32 cm.

    (i) Write down an equation in terms of x and solve it.

Answer(c)(i) $x =$ .... [3]

    (ii) Work out the length of the shortest side of the triangle.

Answer(c)(ii) .... cm [2]

5

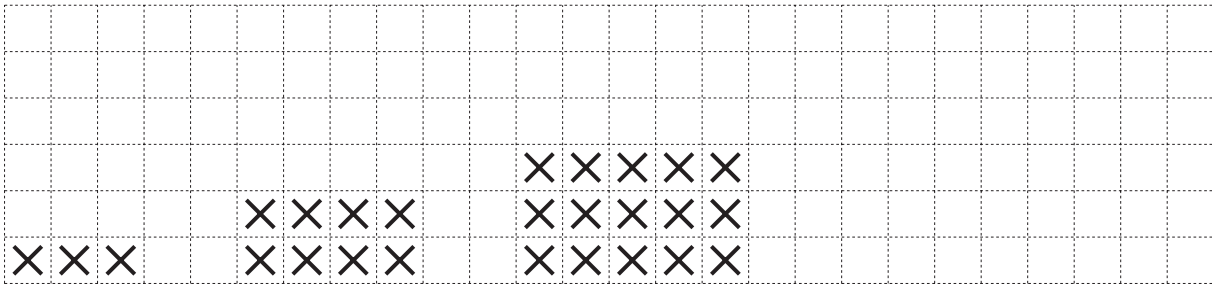Diagram 1   Diagram 2   Diagram 3   Diagram 4

The number of crosses in each Diagram forms a sequence.

(a) On the grid draw Diagram 4. [1]

(b) Write down the number of crosses needed to draw Diagram 5.

Answer(b) .... [1]

(c) Diagram 1 has 1 row of 3 crosses.
Diagram 2 has 2 rows of 4 crosses.
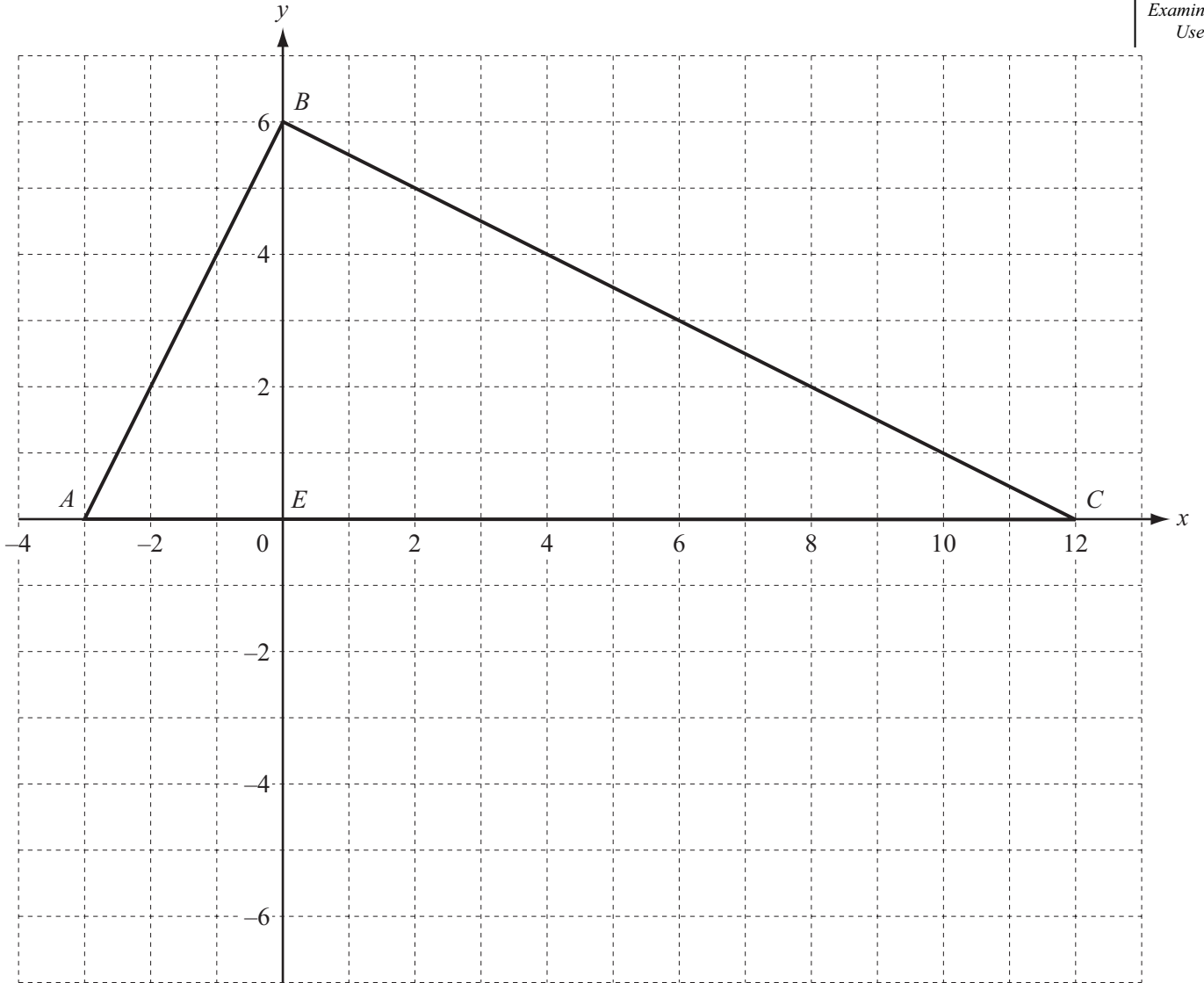
(i) Complete this statement for Diagram *n*.

Diagram *n* has *n* rows of .... crosses. [1]

(ii) Write down, in terms of *n*, how many crosses are needed to draw Diagram *n*.

Answer(c)(ii) .... [1]

(iii) Find the number of crosses needed to draw Diagram 20.

Answer(c)(iii) .... [1]

6

Triangle *ABC* is drawn on a 1cm^2 grid.
E is the point (0, 0).

(a) Calculate the slope of the line *AB*.

Answer(a) .... [2]

(b) The slope of *BC* is -0.5.

Write down the equation of the line *BC* in the form $y = mx + b$.

Answer(b) y = ... [2]

(c) Write down the ratio *AE* : *EC*.
Give your answer in its simplest form.

Answer(c) .... : .... [2]

(d) Measure angle *ABE*.

Answer(d) Angle *ABE* = ... [1]

(e) Triangle *ABE* is **similar** to triangle *BCE*.

Explain what the word **similar** tells you about the triangles *ABE* and *BCE*.

Answer(e) ....

.... [2]

(f) Calculate the area of triangle *ABC*.

Answer(f) .... cm^2 [3]

(g) *ABCD* is a rectangle.

  (i) Mark point *D* on the grid. [1]

  (ii) Write down the co-ordinates of *D*.

Answer(g)(ii) (............ , ...) [1]

7
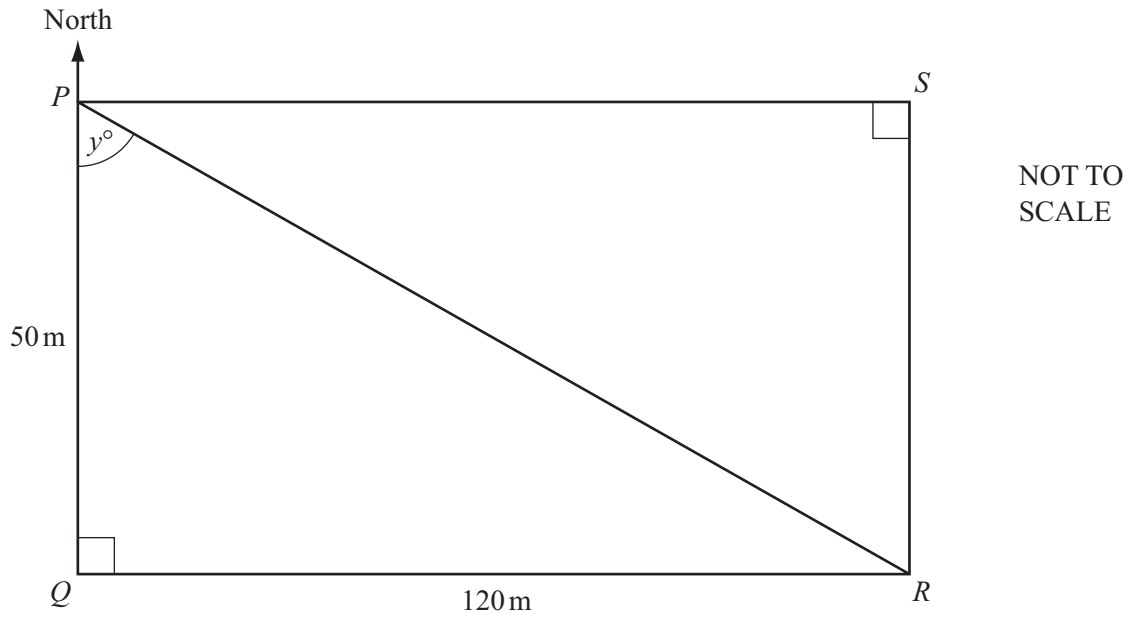
North

The diagram shows a rectangular field, *PQRS*.
QR = 120 m, *PQ* = 50 m and *P* is due North of *Q*.

Bill and Said run from *P* to *R*.
Bill runs along the sides *PQ* and *QR*.
Said runs directly from *P* to *R*.

(a) Calculate how far

   (i) Bill runs,

Answer(a)(i) .... m [1]

   (ii) Said runs.

Answer(a)(ii) .... m [2]

(b) Bill takes 34 seconds to reach *R*.

Calculate Bill's average speed.

Answer(b) .... m/s [1]

(c) Said runs at $4\,\text{m/s}$.

Who arrives at R first and by how many seconds?

Answer(c) .... arrives at R first by .... seconds. [3]

(d) (i) Use trigonometry to calculate the size of the angle marked y.

Answer(d)(i) .... [2]

(ii) Find the bearing of R from P.

Answer(d)(ii) .... [1]

(e) Calculate the area of the field in **square kilometres**.
Give your answer in scientific form.

Answer(e) .... km^2 [4]

8 **(a)**

3 cm

8 cm
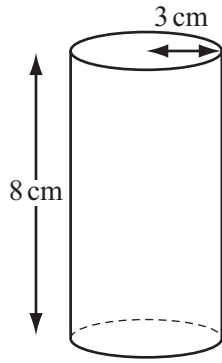
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A cylindrical drinking glass has radius 3 cm and height 8 cm.

(i) Calculate the volume of water the glass holds when it is filled to the top.
Give the units of your answer.

Answer(a)(i) .... [3]

(ii) Water is poured into a number of these glasses from a jug containing 1.5 litres.
Each glass has a horizontal line 2 cm from the top.
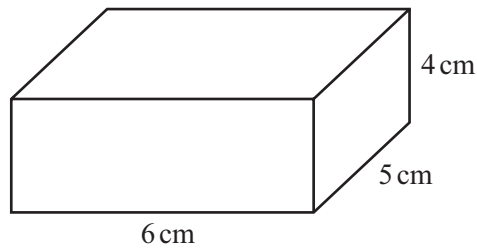
Calculate how many of these glasses can be filled up to the line from the jug.

Answer(a)(ii) .... [4]

(b) A cylindrical pipe has a circumference of 16 cm.

Calculate the diameter of the pipe.

Answer(b) .... cm [2]

(c) A rectangular prism measures 6 cm by 5 cm by 4 cm.

4 cm

NOT TO SCALE

5 cm

6 cm

Work out the surface area of the rectangular prism.

Answer(c) .... cm^2 [3]

(d) 1m^3 of copper has a mass of *m* kg.
The volume of one copper sphere is *v* m^3.

Write down an expression for

(i) the mass, in kilograms, of one sphere,

Answer(d)(i) .... kg [1]

(ii) the mass, in kilograms, of *s* spheres,

Answer(d)(ii) .... kg [1]

(iii) the mass, in grams, of *s* spheres.

Answer(d)(iii) .... g [1]

9　**(a)**　**(i)**　The diagram shows the graph of $y = \text{f}(x)$.
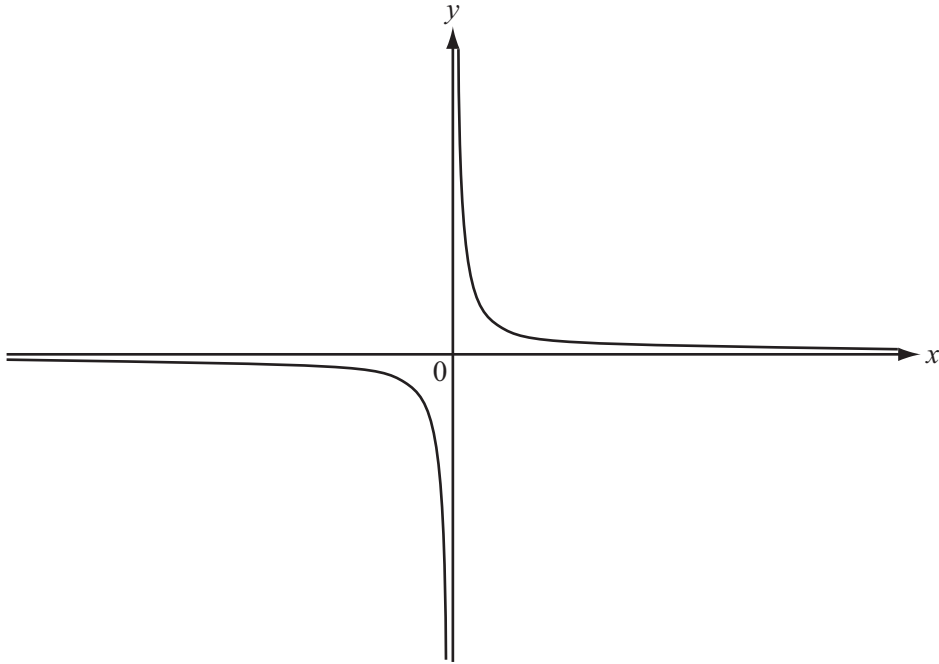
Write down a possible equation of the graph of $y = \text{f}(x)$.

Answer(a)(i) f(x) = ... [1]

(ii)　The diagram shows the graph of $y = \text{g}(x)$.
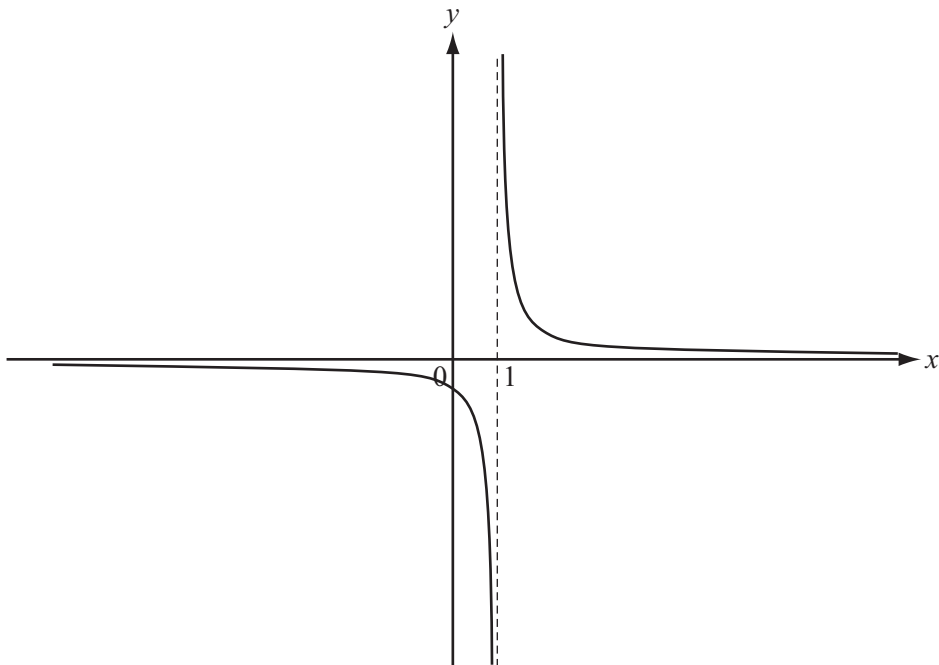
Complete the statement.

g(x) =f (............) [1]

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(b) (i) The diagram shows the graph of $y = \mathrm{h}(x)$.
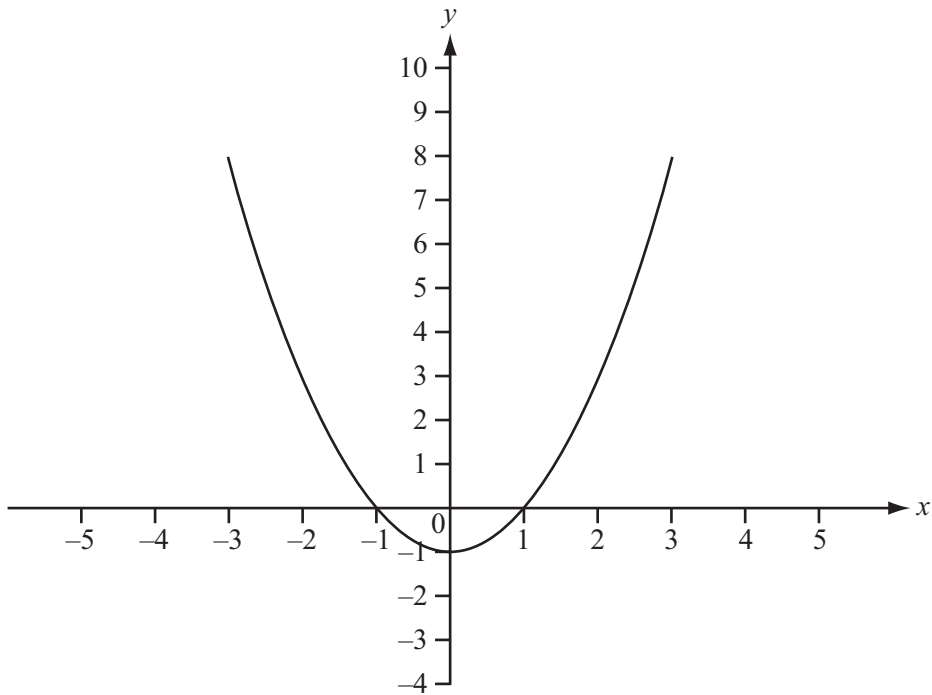
On the diagram above, draw the graph of $y = 2\mathrm{h}(x)$. [2]

(ii)
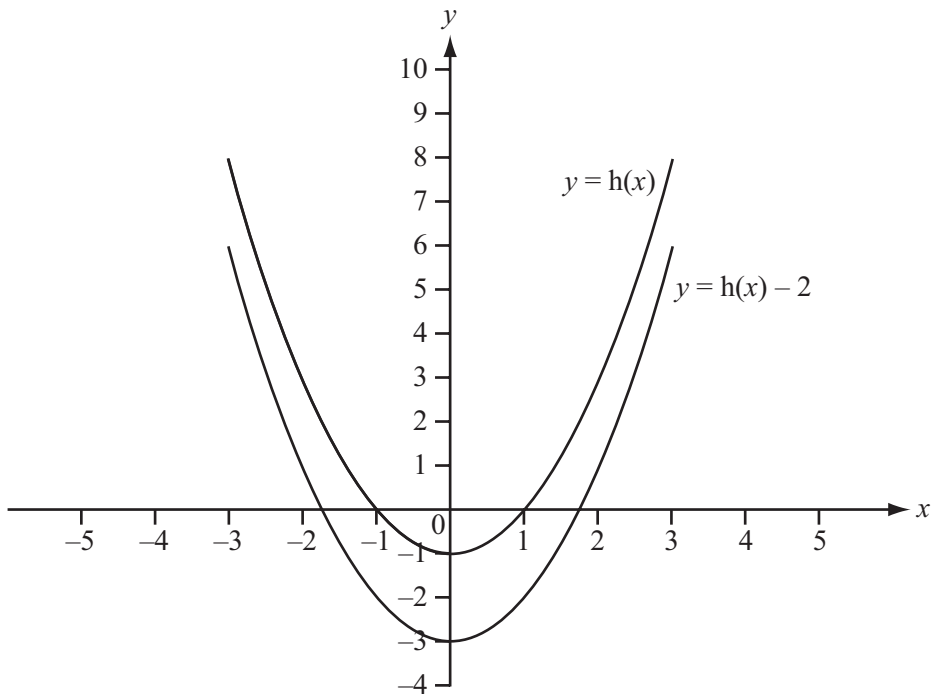
Describe fully the **single** transformation that maps the graph of $y = \mathrm{h}(x)$ onto the graph of $y = \mathrm{h}(x) - 2$.

Answer (b)(ii) .... [2]

10 The time, in minutes, required to cook a piece of meat weighing between 1 and 3 kilograms is 30 minutes per kilogram plus 20 minutes extra.

This information is shown by the function t(w) = aw + b, where w is the weight of the meat in kilograms.

(a) Write down the values of a and b.

Answer(a) a = ...

b = ... [2]

(b) Complete the statement about the domain of t(w).

Answer(b) .... $< w <$ .... [1]

(c) Find the range of t(w).

Answer(c) .... [2]

(d) Find t(2.5).

Answer(d) .... [1]

(e) Draw the graph of $y = t(w)$ on the grid below.

[2]

(f) Use your graph to find w when $t(w) = 65$.

Answer(f) w = ... [1]

20

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