## MATHEMATICAL STUDIES <br> STANDARD LEVEL <br> PAPER 1



Number
Friday 9 November 2001 (afternoon)
1 hour

## INSTRUCTIONS TO CANDIDATES

- Write your name and candidate number in the boxes above.
- Do not open this examination paper until instructed to do so.
- Answer all the questions in the spaces provided.
- Unless otherwise stated in the question, all numerical answers must be given exactly or to three significant figures, as appropriate.
- Write the make and model of your calculator in the box below e.g. Casio $f x-9750 G$, Sharp EL-9600, Texas Instruments TI-85.

Calculator

| Make | Model |
| :--- | :--- |
|  |  |


| EXAMINER | TEAM LEADER |  | IBCA |  |
| :---: | :--- | :--- | :--- | :---: |
| TOTAL |  | TOTAL | TOTAL |  |
|  |  |  |  |  |
|  | 160 |  |  |  |

Maximum marks will be given for correct answers. Where an answer is wrong, some marks may be given for a correct method provided this is shown by written working. Working may be continued below the box, if necessary. (If graphs from a graphic display calculator are being used to find solutions, you should sketch these graphs as part of your answer.)

1. The speed of sound in air is given as $300 \mathrm{~m} \mathrm{~s}^{-1}$.
(a) How many metres does sound travel in air in one hour?
(b) Express your answer to part (a)
(i) correct to two significant figures;
(ii) in the form $a \times 10^{k}$, where $1 \leq a<10$ and $k \in \mathbb{Z}$.

Working:

Answers:
(a)
(b) (i)
(ii) $\qquad$
2. The bar chart below shows the number of people in a selection of families.

(a) How many families are represented?
(b) Write down the mode of the distribution.
(c) Find, correct to the nearest whole number, the mean number of people in a family.

## Working:

Answers:
(a)
(b)
(c) $\qquad$
3. Two propositions $p$ and $q$ are defined as follows.
$p:$ Jones passed this course
$q:$ Smith passed this course
(a) Write in symbolic form
(i) neither Jones nor Smith passed the course;
(ii) it is not the case that Jones and Smith both passed the course.
(b) Complete the following truth table for the logic statement $\neg p \vee q$.

| $p$ | $q$ | $\neg p$ | $\neg p \vee q$ |
| :---: | :---: | :---: | :---: |
| T | T |  |  |
| T | F |  |  |
| F | T |  |  |
| F | F |  |  |

Working:

Answers:
(a) (i)
(ii)
4. The following is part of a display on the notice board of a bank in the United Kingdom. It shows the exchange rate between one British pound (GBP) and other currencies.

| EXCHANGE RATES |  |  |
| :--- | :---: | :---: |
|  | Bank buys <br> foreign currency | Bank sells <br> foreign currency |
| Denmark (KR) | 11.38 | 10.78 |
| Finland (MKK) | 7.00 | 6.60 |
| France (FFR) | 10.05 | 9.45 |
| Germany (DM) | 2.854 | 2.798 |
| Greece (DR) | 292 | 266 |
| NO COMMISSION CHARGED |  |  |

Geraldine eats a meal in a restaurant while on holiday in Greece. The meal costs 4256 drachma (DR).
(a) Use the bank-selling price to calculate the cost of the meal in British pounds.

The Williams family go to Germany. Before leaving, they change GBP 600 into German marks.
(b) Calculate the number of German marks they receive for GBP 600, giving your answer correct to two decimal places.

They spend DM 824 in Germany, and on returning to the United Kingdom, they change their remaining German marks into British pounds.
(c) Calculate the number of British pounds they receive, correct to two decimal places.

## Working:

## Answers:

(a)
(b) $\qquad$
(c) $\qquad$
5. The equation of a line $l_{1}$ is $y=\frac{1}{2} x$.
(a) On the grid, draw and label the line $l_{1}$.


The line $l_{2}$ has the same gradient as $l_{1}$ but crosses the $y$-axis at 3 .
(b) What is the geometric relationship between $l_{1}$ and $l_{2}$ ?
(c) Write down the equation of $l_{2}$.
(d) On the same grid as in part (a), draw the line $l_{2}$.

## Working:

Answers:
(b) $\qquad$
(c) $\qquad$
6. In the triangle $\mathrm{OAB}, \mathrm{P}$ is the mid-point of $\mathrm{AB}, \mathrm{X}$ is the mid-point of $\mathrm{OB}, \overrightarrow{\mathrm{OA}}=\boldsymbol{a}$ and $\overrightarrow{\mathrm{OB}}=\boldsymbol{b}$.


## Diagram not to scale

Express the following vectors in terms of $\boldsymbol{a}$ and $\boldsymbol{b}$
(a) $\overrightarrow{\mathrm{AB}}$;
(b) $\overrightarrow{\mathrm{OP}}$;
(c) $\overrightarrow{\mathrm{AX}}$.

Working:

Answers:
(a)
(b)
(c)
7. The first four terms of an arithmetic sequence are shown below.

$$
1,5,9,13, \ldots \ldots .
$$

(a) Write down the $n^{\text {th }}$ term of the sequence.
(b) Calculate the $100^{\text {th }}$ term of the sequence.
(c) Find the sum of the first 100 terms of the sequence.

Working:

Answers:
(a)
(b)
(c)
8. The diagram shows a cuboid 22.5 cm by 40 cm by 30 cm .

(a) Calculate the length of $[\mathrm{AC}]$.
(b) Calculate the size of G $\widehat{A} C$.

Working:

Answers:
(a)
(b)
9. A committee $U$ has three sub-committees: research $R$, finance $F$ and purchasing $P$. No member belongs to both finance and purchasing sub-committees. Some members belong to both research and purchasing committees. All members of the finance sub-committee also belong to the research sub-committee.

Draw a Venn diagram, showing the relationship between the sets $U, R, F$ and $P$.

Answer:
10. Write down the three inequalities that define the shaded region $(R)$, shown in the diagram below.


Working:

## Answers:

11. (a) Factorise the expression $2 x^{2}-3 x-5$.
(b) Hence, or otherwise, solve the equation $2 x^{2}-3 x=5$.

## Working:

## Answers:

(a)
(b)
12. A teacher has a box containing six type A calculators and four type B calculators.

The probability that a type A calculator is faulty is 0.1 and the probability that a type B calculator is faulty is 0.12 .
(a) Complete the tree diagram given below, showing all the probabilities.

(b) A calculator is selected at random from the box. Find the probability that the calculator is
(i) a faulty type A;
(ii) not faulty.

Working:

Answers:
(b) (i) $\qquad$
(ii) $\qquad$
13. In the diagram the shaded region represents a circular track with centre $O$, within a square field PQRS. The outer edge of the track touches the sides of the field. The radii of the inner and outer edges of the track are $x \mathrm{~m}$ and $y \mathrm{~m}$ respectively.

## Diagram not to scale


(a) Write down an expression for the area of the track.
(b) The area of the field PQRS is $4900 \mathrm{~m}^{2}$.
(i) Find $y$.
(ii) Given that $x=21$, find the area of the track.

Working:

Answers:
(a)
(b) (i)
(ii)
14. The graph below shows the curve $y=k\left(2^{x}\right)+c$, where $k$ and $c$ are constants.


Find the values of $c$ and $k$.

Working:

## Answers:

15. A ski lift travels in a straight line between two points, A and B . The coordinates of A and B are $(100,0,300)$ and $(200,250,0)$ respectively, where 1 unit represents 1 metre.

Heidi is travelling to the top of the ski lift at $B$. She is now at point $M$, halfway between A and B .
(a) Write down the coordinates of M .
(b) How far does Heidi still have to travel to reach B ?

Working:

Answers:
(a)
(b)

