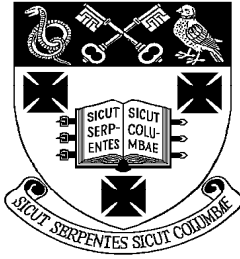


**RADLEY COLLEGE**  
**Entrance Scholarships**



**MATHEMATICS I**

Thursday 13th February 2003  
Time allowed 90 minutes

*You may try the questions in any order and  
are not expected to complete them all.*

***Show all working.***

1. (No calculating aids are to be used in this question)
  - a) Work out exactly
    - i)  $60.8 \times 2.71$
    - ii)  $172.02 \div 47$
  - b) Give the answers to the following as fractions in their simplest form
    - i)  $\frac{13}{15} - \frac{7}{10}$
    - ii)  $7\frac{1}{2} \div 5\frac{1}{4}$
    - iii)  $\left(7\frac{2}{3} + 1\frac{4}{5}\right) \times 1\frac{5}{22}$
  - c) Give the answers to the following in standard form.
    - i)  $(7 \times 10^6) + (5 \times 10^6)$
    - ii)  $(6 \times 10^3) \times (4 \times 10^{-4})$
    - iii)  $(4.8 \times 10^2) \div (6 \times 10^5)$

2. (No calculating aids are to be used in this question)

Work out as simply as possible

a)  $923^2 - 77^2$

b)  $38^2 + (93 \times 38) - (38 \times 31)$

c)  $(83 \times 47) + (17 \times 24) + (36 \times 83) - (41 \times 17)$

d)  $\frac{456^2 + (456 \times 44)}{45.6 \times 25}$

3. a) Multiply out and simplify

i)  $(2x + y)^2$

ii)  $(3x + y)(9x^2 - 3xy + y^2)$

b) Factorise fully

i)  $12x^2y + 16xy^2$

ii)  $27 - 12x^2$

iii)  $x^2 - 11x + 18$

c) Simplify

i)  $\frac{xy + xz}{y^2 - z^2}$

ii)  $\frac{x^2}{y^3} \div x^2y^2$

4. Solve each of these equations for  $x$

a)  $\frac{3x+1}{2} + \frac{2x+1}{7} = 6$

b)  $2x^2 - 6x = 0$

c)  $\frac{42}{x+2} + 6 = \frac{78}{x+2}$

d)  $(3x+1)(x+2) - 3x^2 = 37$

5. Rearrange each of the following formulae to make  $x$  the subject

a)  $a = bx - c$

b)  $\frac{a}{x+b} = \frac{c}{x+d}$

c)  $\sqrt{x-a} = b$

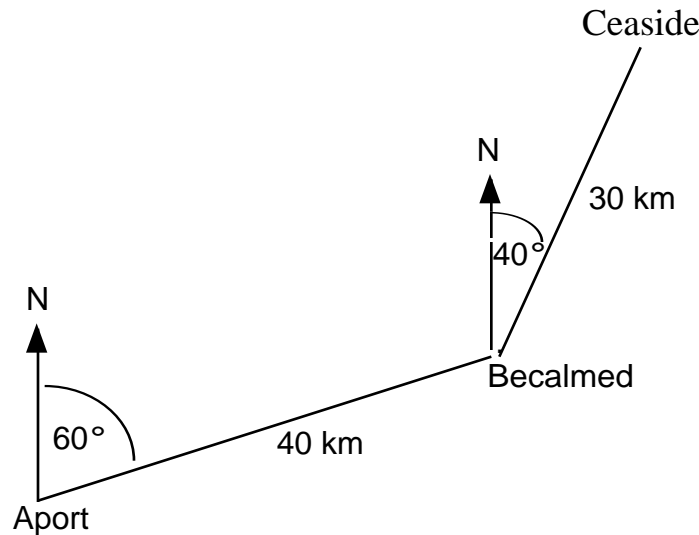
6. In cricket a batsman's average is calculated by dividing the total number of runs he has scored by the number of times he is out. So a batsman who has played 11 innings scoring a total of 400 runs and has been not out three times has an average of 50. ( $400 \div (11 - 3) = 50$ ).

Matthew Matics has become a keen cricketer. In the last match of the season, he scored 63 runs before he was out. He works out that this improved his season's average by 5. Letting  $x$  be the total he had scored before the final match and letting  $y$  be the number of times he had been out previously, write down an equation in  $x$  and  $y$  and show that it simplifies to  $x + 5y^2 - 58y = 0$ .

Then he realises that had he not been out (but still have scored 63 runs), his season's average would have been improved by 9 in the last match. Write down and simplify an equation using this piece of information.

Find the values of  $x$  and  $y$ , and thus find Matthew's batting average for the season.

7. A yachtsman sails 40 km on a bearing  $060^\circ$  from Aport to Becalmed, and then changes direction to sail 30 km on  $040^\circ$  to get to Ceaside.



- How far East of Aport is Becalmed?
  - How far North of Aport is Becalmed?
  - How far East of Aport is Ceaside?
  - How far North of Aport is Ceaside?
  - Had the yachtsman wanted to sail directly from Aport to Ceaside, how far would it have been and on what bearing?
8. For any positive integer,  $n$ , we define  $n!$  to be the product of all the integers between 1 and  $n$  inclusive.

So, for example,  $5! = 1 \times 2 \times 3 \times 4 \times 5 = 120$

- (a) Work out
- $3!$
  - $6!$
  - $1!$

(b) For two positive integers,  $a$  and  $b$ , where  $a > b$ , we define an operation  $*$  such that  $a * b = \frac{a!}{(a-b)!}$

- Show that  $6 * 2 = 30$
- Work out  $7 * 3$ .
- Show that  $n * 1 = n$ , and work out a similar expression for  $n * 2$ .
- Solve the equation  $n * 2 = 8n - 20$ .