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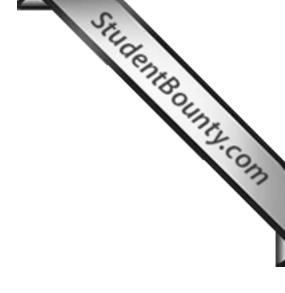
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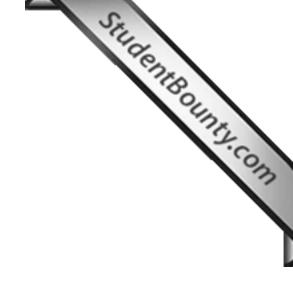




EQUATIONS, INEQUALITIES, & VICs

Math Strategy Guide

This essential guide covers algebra in all its various forms (and disguises) on the GMAT. Master fundamental techniques and nuanced strategies to help you solve for unknown variables of every type.



Equations, Inequalities, and VICs GMAT Strategy Guide, Third Edition

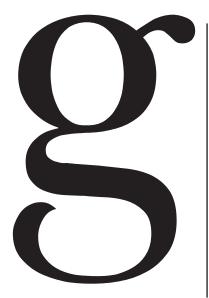
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September 30th, 2008

Dear Student,

Thank you for picking up one of the Manhattan GMAT Strategy Guides—we hope that it refreshes your memory of the junior-high math that you haven't used in years. Maybe it will even teach you a new thing or two.

As with most accomplishments, there were many people involved in the various iterations of the book that you're holding. First and foremost is Zeke Vanderhoek, the founder of Manhattan GMAT. Zeke was a lone tutor in New York when he started the Company in 2000. Now, eight years later, MGMAT has Instructors and offices nationwide, and the Company contributes to the studies and successes of thousands of students each year.

These 3rd Edition Strategy Guides have been refashioned and honed based upon the continuing experiences of our Instructors and our students. We owe much of these latest editions to the insight provided by our students. On the Company side, we are indebted to many of our Instructors, including but not limited to Josh Braslow, Dan Gonzalez, Mike Kim, Stacey Koprince, Jadran Lee, Ron Purewal, Tate Shafer, Emily Sledge, and of course Chris Ryan, the Company's Lead Instructor and Director of Curriculum Development.

At Manhattan GMAT, we continually aspire to provide the best Instructors and resources possible. We hope that you'll find our dedication manifest in this book. If you have any comments or questions, please e-mail me at andrew.yang@manhattangmat.com. I'll be sure that your comments reach Chris and the rest of the team—and I'll read them too.

Best of luck in preparing for the GMAT!

Sincerely,

Andrew Yang Chief Executive Officer Manhattan GMAT

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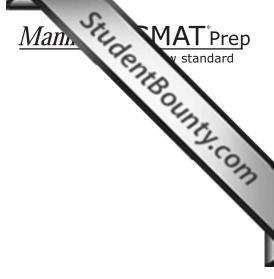
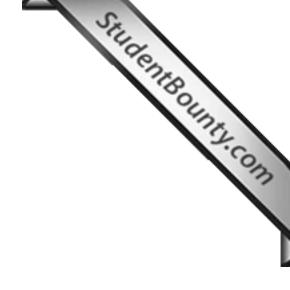


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Chapter 1 EQUATIONS, INEQUALITIES, & VICs

BASIC EQUATIONS





- Solving One-Variable Equations
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- Simultaneous Equations: Three Equations
- Mismatch Problems
- Combo Problems: Manipulations
- Testing Combos in Data Sufficiency
- Absolute Value Equations
- Complex Absolute Value Equations (Advanced)
- Integer Constraints (Advanced)
- Advanced Algebraic Techniques (Advanced)

BASIC EQUATIONS

Algebra is one of the major math topics tested on the GMAT. Your ability to solve equations is an essential component of your success on the exam.

StudentBounty.com Basic GMAT equations are those that DO NOT involve exponents. There are several different types of BASIC equations that the GMAT expects you to solve:

- 1) An equation with 1 variable
- 2) Simultaneous equations with 2 or 3 variables
- 3) Mismatch equations
- 4) Combos
- 5) Equations with absolute value

Several of the preceding basic equation types probably look familiar to you. Others-particularly Mismatch Equations and Combos—are unique GMAT favorites that run counter to some of the rules you may have learned in high-school algebra. Becoming attuned to the particular subtleties of GMAT equations can be the difference between an average score and an excellent one.

Solving One-Variable Equations

Equations with one variable should be familiar to you from previous encounters with algebra. In order to solve one-variable equations, simply isolate the variable on one side of the equation. In doing so, make sure you perform identical operations to both sides of the equation. Here are three examples:

3x + 5 = 26 $3x = 21$ $x = 7$	Subtract 5 from both sides. Divide both sides by 3.
w = 17w - 1 0 = 16w - 1 1 = 16w $\frac{1}{16} = w$	Subtract <i>w</i> from both sides. Add 1 to both sides. Divide both sides by 16.
$\frac{p}{9} + 3 = 5$	Subtract 3 from both sides.
$\frac{p}{9} = 2$ $p = 18$	Multiply both sides by 9.

To solve basic equations, remember that whatever you do to one side, you must also do to the other side.

BASIC EQUATIONS STRATEGY **Chapter 1**

Simultaneous Equations: Solving by Substitution

StudentBounts.com Sometimes the GMAT asks you to solve a system of equations with more than on You might be given two equations with two variables, or perhaps three equations with variables. In either case, there are two primary ways of solving simultaneous equations: by substitution or by combination.

Solve the following for *x* and *y*.

$$x + y = 9$$
$$2x = 5y + 4$$

Use substitution whenever one variable can be easily expressed in terms of the other.

1. Solve the first equation for *x*.

x + y = 9 $x = 9 - \gamma$

2. Substitute this solution into the second equation wherever *x* appears.

$$2x = 5y + 4$$
$$2(9 - \gamma) = 5\gamma + 4$$

3. Solve the second equation for γ .

$$2(9 - y) = 5y + 4$$

$$18 - 2y = 5y + 4$$

$$14 = 7y$$

$$2 = y$$

4. Substitute your solution for y into the first equation in order to solve for x.

$$x + y = 9$$
$$x + 2 = 9$$
$$x = 7$$

BASIC EQUATIONS STRAT

Simultaneous Equations: Solving by Combination

StudentBounty.com Alternatively, you can solve simultaneous equations by combination. In this method, add or subtract the two equations to eliminate one of the variables.

Solve the following for x and y.

$$x + y = 9$$
$$2x = 5y + 4$$

1. Line up the terms of the equations.

$$x + y = 9$$
$$2x - 5y = 4$$

2. If you plan to add the equations, multiply one or both of the equations so that the coefficient of a variable in one equation is the OPPOSITE of that variable's coefficient in the other equation. If you plan to subtract them, multiply one or both of the equations so that the coefficient of a variable in one equation is the SAME as that variable's coefficient in the other equation.

-2(x+y=9)	\rightarrow	-2x - 2y = -18
2x - 5y = 4	\rightarrow	2x - 5y = 4

Note that the *x* coefficients are now opposites.

3. Add the equations to eliminate one of the variables.

$$-2x - 2y = -18 + 2x - 5y = 4 -7y = -14$$

4. Solve the resulting equation for the unknown variable.

$$-7y = -14$$
$$y = 2$$

5. Substitute into one of the original equations to solve for the second variable.

$$x + y = 9$$
$$x + 2 = 9$$
$$x = 7$$

Use combination whenever it is easy to manipulate the equations so that the coefficients for one variable are the SAME or OPPOSITE.

Chapter 1

BASIC EQUATIONS STRATEGY

Simultaneous Equations: Three Equations

StudentBounts.com The procedure for solving a system of three equations with three variables is exact same as for a system with two equations and two variables. You can use substitution combination. This example uses both:

Solve the following for w, x, and y.

Solve three simultaneous equations step-by-step. Keep careful track of your work to avoid careless errors, and look for ways to reduce the number of steps needed to solve.

x + w = y2y + w = 3x - 213 - 2w = x + y

1. The first equation is already solved for *y*.

y = x + w

2. Substitute for γ in the second and third equations.

Substitute for <i>y</i> in the second equation:	Substitute for <i>y</i> in the third equation:
2(x+w)+w=3x-2	13 - 2w = x + (x + w)
2x + 2w + w = 3x - 2	13 - 2w = 2x + w
-x + 3w = -2	3w + 2x = 13

3. Multiply the first of the resulting two-variable equations by (-1) and combine them with addition.

$$x - 3w = 2$$

+ $2x + 3w = 13$
 $3x = 15$ Therefore, $x = 5$

4. Use your solution for *x* to determine solutions for the other two variables.

3w + 2x = 13	y = x + w
3w + 10 = 13	y = 5 + 1
3w = 3	y = 6
w = 1	

The preceding example requires a lot of steps to solve. Therefore it is unlikely that the GMAT will ask you to solve such a complex system—it would be difficult to complete in two minutes. Here is the key to handling systems of three or more equations on the GMAT: look for ways to simplify the work that you have to do. Look especially for shortcuts or symmetries in the form of the equations to reduce the number of steps needed to solve the system.

BASIC EQUATIONS STRAT. File Chapter 1

Take this system as an example:

What is the sum of *x*, y and *z*?

x + y = 8x + z = 11y + z = 7

In this case, DO NOT try to solve for *x*, *y*, and *z* individually. Instead, notice the symmetry of the equations—each one adds exactly two of the variables—and add them all together:

x + y = 8x + z = 11+ y + z = 72x + 2y + 2z = 26

Therefore, x + y + z is half of 26, or 13.

Mismatch Problems

Consider the following rule, which you might have learned in a basic algebra course: if you are trying to solve for 2 different variables, you need 2 equations. If you are trying to solve for 3 different variables, you need 3 equations, etc. The GMAT loves to trick you by taking advantage of your faith in this easily misapplied rule.

MISMATCH problems, which are particularly common on the Data Sufficiency portion of the test, are those in which the number of unknown variables does NOT correspond to the number of given equations. Do not try to apply that old rule you learned in high-school algebra, because it is not applicable for many GMAT equation problems. All MISMATCH problems must be solved on a case-by-case basis.

Solve for *x* given the following two equations:

(1)
$$\frac{3x}{3y+5z} = 8$$
 (2) $6y + 10z = 18$

It is tempting to say that these two equations are not sufficient to solve for *x*, since there are 3 variables and only 2 equations. However, note that the question does NOT ask you to solve for all three variables. It only asks you to solve for *x*, which IS possible:

First, get the *x* term on one side of the equation:

Then, notice that the second equation gives us a value for 3y + 5z, which we can substitute into the first equation in order to solve for *x*:

$\frac{3x}{3} = 8$	6y + 10z = 18	3x = 8(3y + 5z)
3y + 5z	2(3y+5z)=18	3x = 8(9)
3x = 8(3y + 5z)	3y + 5z = 9	x = 8(3) = 24

Do not assume that the number of equations must be equal to the number of variables. **Chapter 1**

BASIC EQUATIONS STRATEGY

Now consider an example in which 2 equations with 2 unknowns are actual sufficient to solve a problem:

Solve for *x* given the following two equations:

(1) $y = x^3 - 1$ (2) y = x - 1

StudentBounts.com It is tempting to say that these 2 equations are surely sufficient to solve for x, since there are 2 different equations and only 2 variables. However, notice that if we take the expression for *y* in the first equation and substitute into the second, we actually get multiple answers:

$x^3 - 1 = x - 1$	$x(x^2-1)=0$
$x^3 = x$	x(x+1)(x-1) = 0
$x^3 - x = 0$	$x = \{-1, 0, 1\}$

Because of the exponent on x, we have THREE values for x (-1, 0, or 1). Therefore we do NOT have sufficient information to solve for *x*. This example is typical.

Now consider another example in which 2 equations with 2 unknowns are actually NOT sufficient to solve a problem. This time we will avoid exponents altogether:

Solve for *x* given the following two equations:

(1)
$$x - y = 1$$
 (2) $xy = 12$

Again, it is tempting to say that these 2 equations are sufficient to solve for x, since there are 2 equations and only 2 variables. However, notice that when you actually combine the two equations algebraically, you wind up with a quadratic equation that has multiple solutions:

$$x - y = 1$$

$$x - 1 = y$$

$$x(x - 1) = 12$$

$$x^{2} - x = 12$$

$$x^{2} - x - 12 = 0$$

$$(x - 4)(x + 3) = 0$$

$$x = 4 \text{ or } x = -3$$

Although we have narrowed down the possibilities for x to just two choices, this is not enough. We do NOT have sufficient information to solve for *x*.

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Follow through with the algebra on potential mismatch problems to determine whether a single solution is possible. BASIC EQUATIONS STRAT

A MASTER RULE for determining whether 2 equations involving 2 variables (say, x and ywill be sufficient to solve for the variables is this:

- StudentBounty.com (1) If both of the equations are linear—that is, if there are no squared terms (such as x^2 or y^2) and no xy terms—the equations will be sufficient UNLESS the two equations are mathematically identical.
- (2) If there are ANY non-linear terms in either of the equations (such as x^2 , y^2 , xy, or

 $\frac{x}{y}$, there will USUALLY be two (or more) different solutions for each of the variables and the equations will not be sufficient.

Examples:

Solve for *x* in the given equations:

Solve for x in the given equations:

(1) $2x + 3y = 8$	(1) $x^2 + y = 17$
(2) $2x - y = 0$	(2) $y = 2x + 2$

Because both of the equations are linear, and because they are not mathematically identical, there is only one solution (x = 1 and y = 2) so the equations are SUFFICIENT. Because there is an x^2 term in equation 1, as usual there are two solutions for x and y (x = 3 and y = 8, or x = -5 and y = -8), so the equations are NOT SUFFICIENT.

Combo Problems: Manipulations

The GMAT often asks you to solve for a combination of variables, called COMBO problems. For example, a question might ask, what is the value of x + y?

In these cases, since you are not asked to solve for one specific variable, you should generally NOT try to solve for the individual variables right away. Instead, you should try to manipulate the given equation(s) so that the COMBO is isolated on one side of the equation. Only try to solve for the individual variables after you have exhausted all other avenues.

There are four easy manipulations that are the key to solving most COMBO problems. You can use the acronym MADS to remember them.

M: Multiply or divide the whole equation by a certain number.

A: Add or subtract a number on both sides of the equation.

D: Distribute or factor an expression on ONE side of the equation.

S: Square or unsquare both sides of the equation.

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With 2 equations and 2 unknowns, linear equations usually lead to one solution and nonlinear equations usually lead to 2 (or more) solutions.

Chapter 1

BASIC EQUATIONS STRATEGY

Here are three examples, each of which uses one or more of these manipula.

If
$$x = \frac{7 - y}{2}$$
, what is $2x + y$?

$$x = \frac{7 - y}{2}$$

$$2x = 7 - y$$

$$2x + y = 7$$

StudentBounts.com Here, getting rid of the denominator by multiplying both sides of the equation by 2 is the key to isolating the combo on one side of the equation.

If $\sqrt{2t+r} = 5$, what is 3r + 6t?

To solve for a variable combo, isolate the combo on one side of the equation.

 $\left(\sqrt{2t+r}\right)^2 = 5^2$ 2t + r = 256t + 3r = 75

Here, getting rid of the square root by squaring both sides of the equation is the first step. Then, multiplying the whole equation by 3 forms the combo in question.

If a(4-c) = 2ac + 4a + 9, what is ac?

4a - ac = 2ac + 4a + 9-ac = 2ac + 9-3ac = 9ac = -3

Here, distributing the term on the left-hand side of the equation is the first key to isolating the combo on one side of the equation; then we have to subtract 2ac from both sides of the equation.

Testing Combos in Data Sufficiency

StudentBounty.com Combo problems occur most frequently in Data Sufficiency. Whenever you detect that a Data Sufficiency question may involve a combo, you should try to manipulate the given equation(s) so that the combo is isolated on one side of the equation. Then, if the other side of the equation contains a VALUE, that equation is SUFFICIENT. If the other side of the equation contains a VARIABLE EXPRESSION, that equation is NOT SUFFICIENT.

What is
$$\frac{x}{y}$$
?
(1) $\frac{x+y}{y} = 3$
(2) $x+y = 12$

Manipulate statement (1) to solve for $\frac{x}{-}$ on one side of the equation. Since the other side of the equation contains a VALUE, statement (1) is SUFFICIENT:

$$\frac{x+y}{y} = 3$$
$$x+y = 3y$$
$$x = 2y$$
$$\frac{x}{y} = 2$$

Manipulate statement (2) to solve for $\frac{x}{2}$ on one side of the equation. Since the other side of the equation contains a VARIABLE EXPRESSION, Statement (2) is INSUFFICIENT:

$$y = 12$$
$$x = 12 - y$$
$$\frac{x}{y} = \frac{12 - y}{y}$$
$$\frac{x}{y} = \frac{12 - y}{y}$$
$$\frac{x}{y} = \frac{12}{y} - 1$$

х

The key to solving this problem easily is to AVOID trying to solve for the individual variables.

Avoid attempting to solve for the individual variables in a combo problem, unless there is no obvious alternative.

Chapter 1

BASIC EQUATIONS STRATEGY

Absolute Value Equations

StudentBounty.com Absolute value refers to the POSITIVE value of the expression within the absolu brackets. Equations that involve absolute value generally have TWO SOLUTIONS the actual value of the expression inside the brackets could be POSITIVE OR NEGA It is important to consider this rule when thinking about GMAT questions that involve absolute value. The following three-step method should be used when solving for a variable expression inside absolute value brackets.

Solve for w, given that 12 + |w - 4| = 30.

1. Isolate the expression within the absolute value brackets.

12 + |w - 4| = 30|w-4| = 18

2. The rule, once we have an equation of the form |x| = a with a > 0, is that $x = \pm a$. Remove the absolute value brackets and solve the equation for 2 cases:

<u>CASE 1: $x = a$ (x is positive)</u>	<u>CASE 2: $x = -a$ (x is negative)</u>
w - 4 = 18	w - 4 = -18
w = 22	w = -14

3. Check to see whether each solution is valid by putting each one back into the original equation and verifying that the two sides of the equation are in fact equal.

In case 1, the solution, w = 22, is valid because 12 + |22 - 4| = 12 + 18 = 30. In case 2, the solution, w = -14, is valid because 12 + |-14 - 4| = 12 + 18 = 30.

Solve for *n*, given that |n+9| - 3n = 3.

Again, isolate the expression within the absolute value brackets and consider both cases.

|n+9| = 3 + 3n1.

2.

CASE 2: n + 9 is negative: CASE 1: n + 9 is positive: n + 9 = 3 + 3nn + 9 = -(3 + 3n)n = -3n = 3

3. The first solution, n = 3, is valid because |(3) + 9| - 3(3) = 12 - 9 = 3.

However the second solution, n = -3, is NOT valid because |(-3) + 9| - 3(-3) = 6 + 9 =15. This solution fails because when n = -3, the absolute value expression (n + 9 = 6) is not negative, even though we assumed it was negative when we calculated that solution.

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Do not forget to check each of your solutions to absolute value equations by putting each solution back into the original equation.

Complex Absolute Value Equations (Advanced)

StudentBounty.com So far we have only looked at absolute value equations that have one unknown inside one absolute value expression. However, these equations can get more complicated by including more than one absolute value expression. There are two primary types of these <u>complex</u> absolute value equations:

(1) The equation contains TWO or more variables in more than one absolute value expression. These equations, which usually lack constants, are generally NOT easy to solve with algebra. Instead, a conceptual approach is preferable. Problems of this type are discussed in the "Positives & Negatives Strategy" chapter of the Manhattan GMAT Number Properties Strategy Guide.

(2) The equation contains ONE variable and at least one CONSTANT in more than one absolute value expression. These equations are usually easier to solve with an algebraic approach than with a conceptual approach. For example:

If |x-2| = |2x-3|, what are the possible values for x?

We have one variable (x) and three constants (-2, 2 and -3). Thus we know that we should take an algebraic approach to the problem.

Because there are two absolute value expressions, each of which yields two algebraic cases, it seems that we need to test *four* cases overall: positive/positive, positive/negative, negative/positive, and negative/negative.

(1) The positive/positive case:	(x-2) = (2x-3)
(2) The positive/negative case:	(x-2) = -(2x-3)
(3) The negative/positive case:	-(x-2) = (2x-3)
(4) The negative/negative case:	-(x-2) = -(2x-3)

However, note that case (1) and case (4) yield the same equation. Likewise, case (2) and case (3) yield the same equation. Thus, you only need to consider two real cases: one in which neither expression changes sign, and another in which one expression changes sign. GMAT problems will often

CASE A: Same signCASE B: Different signs
$$(x-2) = (2x-3)$$
 $(x-2) = -(2x-3)$ $1 = x$ $3x = 5$ $x = \frac{5}{3}$

We also have to check the validity of the solutions once we have solved the equations.

Both solutions are valid, because |1-2| = |2(1)-3| = 1, and $\left|\frac{5}{3}-2\right| = \left|2\left(\frac{5}{3}\right)-2\right| = \frac{1}{3}$.

When you have an equation with one variable in more than one absolute value expression, you should probably take an algebraic approach.

BASIC EQUATIONS STRATEGY **Chapter 1**

Integer Constraints (Advanced)

StudentBounty.com Occasionally on the GMAT, an algebra problem will contain integer constraints. case, there might be many possible solutions among *all* numbers but only one INTA solution.

2y - x = 2xy and $x \neq 0$. If x and y are integers, which of the following could equal y?

(A)	2
(B)	1
(C)	0
(D)	-1
(E)	-2

When you have integer constraints on solutions, solve for one variable and then test numbers.

First, we solve for x in terms of y, so that we can test values of y in the answer choices.

 $x = \frac{2y}{2y+1}$ 2y = 2xy + x 2y = x(2y + 1)2y - x = 2xy

Ordinarily, this result would not be enough for us to reach an answer. However, we know that both x and y must be integers. Therefore, we should find which integer value of y generates an integer value for *x*.

Now, we test the possibilities for *y*, using the answer choices. The case y = 0 produces x = 0, but this outcome is disallowed by the condition that $x \neq 0$. The only other case that produces an integer value for x is y = -1, yielding x = 2. Thus, the answer is (**D**). (Incidentally, if we relax the integer constraints, x and y can take on many non-integer values.)

If x and y are nonnegative integers and x + y = 25, what is x?

(1) 20x + 10y < 300(2) 20x + 10y > 280

First, we should note that since x and y must be positive integers, the smallest possible value for 20x + 10y is 250, when x = 0 and y = 25. Statement (1) does not tell us what x is, nor does statement (2). However, if we combine the statements, we get:

280 < 20x + 10y < 300280 < 20x + 10(25 - x) < 300Substituting (25 - x) for *y*: 280 < 20x + 250 - 10x < 30030 < 10x < 503 < x < 5

Since x must be an integer, x must equal 4. Therefore the answer is (C): Statements 1 and 2 TOGETHER are sufficient. (Incidentally, if we relax the integer constraint, x can be any real number that is more than 3 and less than 5.) Remember to pay attention to integer constraints on more difficult algebra problems.

Advanced Algebraic Techniques (Advanced)

MULTIPLYING OR DIVIDING TWO EQUATIONS

StudentBounty.com A general rule of thumb in algebra is that you can do just about anything you want to one side of an equation, as long as you do the same thing to the other side (except divide or multiply by 0). Thus, you can multiply or divide two complete equations together, because when you do so, you are doing the same thing to both sides of the equation by definition, both sides of an equation are equal.

What does it mean to multiply two equations together? It means that you multiply the left sides of the two equations together, and also multiply the right sides of the equations together. You then set those products equal to each other. To divide two equations, you take the same kinds of steps.

If
$$xy^2 = -96$$
 and $\frac{1}{xy} = \frac{1}{24}$, what is y?

While we could calculate the individual variables by solving for x or y first and substituting, if we simply multiply the equations together, we will quickly see that y = -4:

$$xy^{2}\left(\frac{1}{xy}\right) = -96\left(\frac{1}{24}\right) \qquad \frac{xy^{2}}{xy} = \frac{-96}{24} \qquad y = -4$$

If $\frac{a}{b} = 16$ and $\frac{a}{b^{2}} = 8$, what is ab ?

Again, we could calculate the individual variables by solving for *a* first and substituting. But if we simply divide the first equation by the second, we will quickly see that b = 2:

$$\frac{\frac{a}{b}}{\frac{a}{b^2}} = \frac{16}{8} \qquad \qquad \frac{b^2 a}{ba} = 2 \qquad \qquad b = 2$$

We can then solve for *a*, and find that ab = 64:

$$\frac{a}{2} = 16$$
 $a = 16(2) = 32$ $ab = 32(2) = 64$

Multiply or divide two equations when it seems that you can cancel a lot of variables in one move.

Chapter 1

BASIC EQUATIONS STRATEGY

ADVANCED FACTORING & DISTRIBUTING

StudentBounty.com GMAT problems often contain expressions that can be presented in factored for tributed form. Distributing a factored expression or factoring a distributed expression often help the solution process. A general rule of thumb is that when you encounter expression or equation in which two or more terms include the same variable, you should consider factoring as an approach. Similarly, when an expression is given in factored form, consider distributing it.

Factoring or distributing may be beneficial in various situations. It is especially important to note that you should feel comfortable going both ways: from distributed form to factored form, and vice versa. Here are some examples:

DISTRIBUTED FORM		FACTORED FORM
$x^2 + x$	$ \longrightarrow $	x(x+1)
$x^{5} - x^{3}$		$x^{3}(x^{2}-1) = x^{3}(x+1)(x-1)$
$6^5 - 6^3$	\checkmark	$6^3(6^2-1) = 35 \cdot 6^3$
$4^8 + 4^9 + 4^{10}$		$4^8(1+4+4^2) = 17 \cdot 4^8$
$p^3 - p$	\checkmark	$p(p^2-1) = p(p+1)(p-1)$
$a^{b} + a^{b+1}$ $3^{5} + 3^{6}$	\checkmark	$a^{b}(1+a)$ $3^{5}(1+3)$
$m^n - m^{n-1}$ $5^5 - 5^4$	\leftrightarrow	$m^{n}(1-m^{-1}) = m^{n-1}(m-1)$ $5^{5}(1-\frac{1}{5}) = 5^{4}(5-1)$
xw + yw + zx + zy	\leftrightarrow	w(x + y) + z(x + y) = $(w + z)(x + y)$

If you have trouble seeing how one form translates into the other, you should practice both recognizing and manipulating in both directions.

Be ready to switch between the distributed and the factored form of any expression.

StudentBounty.com BASIC EQUATIONS PROBLEM

Problem Set

For problems #1-6, solve for all unknowns.

- $\frac{3x-6}{5} = x-6$ 1. $\frac{x+2}{4+x} = \frac{5}{9}$ 2.
- 22 |y + 14| = 203.
- |6+x| = 2x + 14.
- 5. y = 2x + 9 and 7x + 3y = -51
- a + b = 10, b + c = 12, and a + c = 166.

For problems #7-10, determine whether it is *possible* to solve for x using the given equations. (Do not solve.)

7.
$$\frac{\sqrt{x}}{6a} = T$$
 and $\frac{Ta}{4} = 14$

8. 3x + 2a = 8 and 6a = 24 - 9x

9.
$$3a + 2b + x = 8$$
 and $12a + 8b + 2x = 4$

4a + 7b + 9x = 17 and 3a + 3b + 3x = 3 and $9a + \frac{b}{4} + \frac{x}{9} = 9$ 10.

For problems #11–17, solve for the specified expression.

11. Given that
$$\frac{x+y}{3} = 17$$
, what is $x + y$?

- Given that $\frac{a+b}{b} = 21$, what is $\frac{a}{b}$? 12.
- Given that 10x + 10y = x + y + 81, what is x + y? 13.
- Given that 5x + 9y + 4 = 2x + 3y + 31, what is x + 2y? 14.

15. Given that
$$\frac{zx + zy}{9} = 4$$
 and $x + y = 3$, what is z?

16. Given that
$$\frac{b+a}{2a} = 2$$
 and $a+b=8$, what is a?

17. Given that
$$ab = 12$$
 and $\frac{c}{a} + 10 = 15$, what is *bc*?

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IN ACTION ANSWER KEY

BASIC EQUATIONS SOLUT

1 12.		
	$\frac{3x-6}{5} = x-6$ 3x-6 = 5(x-6) 3x-6 = 5x-30 24 = 2x 12 = x	Solve the de variab
2. $x = \frac{1}{2}$:	$\frac{x+2}{4+x} = \frac{5}{9}$ $9(x+2) = 5(4+x)$	
	$9x + 18 = 20 + 5x$ $4x = 2$ $x = \frac{1}{2}$	Cross- distrib

HudentBounty.com by multiplying both sides by 5 to eliminate enominator. Then, distribute and isolate the ole on the left side.

s-multiply to eliminate the denominators. Then, bute and solve.

3.
$$y = \{-16, -12\}$$
:

 $22 - \begin{vmatrix} y + 14 \\ y + 14 \end{vmatrix} = 20$ $\begin{vmatrix} y + 14 \\ z \end{vmatrix} = 2$

First, isolate the expression within the absolute value brackets. Then, solve for two cases, one in which the expression is positive and one in which it is negative. Finally, test the validity of your solutions.

Case 1:
$$y + 14 = 2$$

 $y = -12$
Case 2: $y + 14 = -2$
 $y = -16$

Case 1 is valid because 22 - |-12 + 14| = 22 - 2 = 20. Case 2 is valid because 22 - |-16 + 14| = 22 - 2 = 20.

4.
$$x = 5$$
:

|6+x| = 2x+1

First, isolate the expression within the absolute value brackets. Then, solve for two cases, one in which the expression is positive and one in which it is negative. Finally, test the validity of your solutions. Note that Case 2 is not valid here.

Case 1:
$$6 + x = 2x + 1$$

 $5 = x$
Case 2: $6 + x = -(2x + 1)$
 $6 + x = -2x - 1$
 $3x = -7$
 $x = -\frac{7}{3}$

Case 1 is valid because |6+5| = 11 and 2(5) + 1 = 11. Case 2 is NOT valid because $\left| 6 - \frac{7}{3} \right| = \frac{11}{3}$, but $2\left(-\frac{7}{3} \right) + 1 = -\frac{11}{3}$.

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