



---

# **GCSE MARKING SCHEME**

---

**SUMMER 2016**

**GCSE MATHEMATICS LINKED PAIR METHODS  
UNIT 1 HIGHER  
4363-02**

## **INTRODUCTION**

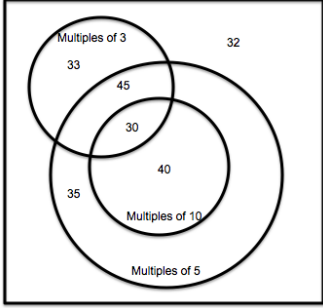
This marking scheme was used by WJEC for the 2016 examination. It was finalised after detailed discussion at examiners' conferences by all the examiners involved in the assessment. The conference was held shortly after the paper was taken so that reference could be made to the full range of candidates' responses, with photocopied scripts forming the basis of discussion. The aim of the conference was to ensure that the marking scheme was interpreted and applied in the same way by all examiners.

It is hoped that this information will be of assistance to centres but it is recognised at the same time that, without the benefit of participation in the examiners' conference, teachers may have different views on certain matters of detail or interpretation.

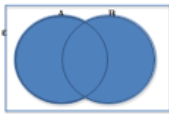
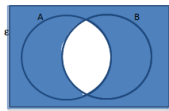
WJEC regrets that it cannot enter into any discussion or correspondence about this marking scheme.

**METHODS IN MATHEMATICS**  
**UNIT 2 (HIGHER TIER) SUMMER 2016**

Methods in Mathematics Unit 1 Higher Tier	Mark	Comments
1. $x = 40(^{\circ})$ $y = 75(^{\circ})$ Sight of $180 - 75 - 40$ or $105 - 40$ or equivalent $z = 65(^{\circ})$	B1 B1 M1 A1 4	FT 180 – ‘their x’ – ‘their y’ FT 180 – ‘their x’ – ‘their y’ correctly evaluated
2(a) 0.625  0.2727... or 0.27 Recurring, Terminating, Recurring  (b) $\frac{0.27}{5.4}$ or $\frac{0.9}{18}$ or $\frac{0.3}{6}$ or equivalent correct 1 <sup>st</sup> step $\frac{27}{540}$ or $\frac{9}{180}$ or $\frac{3}{60}$ or 0.05  $\frac{1}{20}$  (c) Method that ‘... $\times 12 + 56 = 200$ , or $\frac{\dots \times 12 + 56}{100} = 2$ Number is 12	B1  B1 B1  M1  M1  A1  M1  A1 8	FT provided at least 1 of the decimals is correct, i.e. at least B1 previously awarded  Allow for sight of 0.27  FT expressing as a fraction (with whole number numerator and denominator) provided equivalent level of difficulty, $2.7/5.4 = 27/54$ or $\frac{1}{2}$ is equivalent level of difficulty (M0, M1, A0) CAO  OR $2 \times 100$ , then ‘their 200’ – 56, then ‘their 144’ $\div 12$ , or trial & improvement with correct operations in the correct order CAO
3(a)(i) -8 (ii) -1 (iii) 1  (b)(i) $-8g - 29h$ as an expression  (ii) $x + 8$	B1 B1 B1  B2  B1 6	B1 for either $-8g$ or $-29h$ Mark final answer Accept $(x + 8)^1$
4.(a) rhombus (b) kite	B1 B1 2	Do not accept diamond
5.(a)(i) Method that produces prime factors with 2 correct primes before the 2 <sup>nd</sup> error Prime factors: 2, 2, 2, 3, 5, 5 $2^3 \times 3 \times 5^2$ (ii) $2 \times 3$ or 6  (b) $440 \times 6 \div 11$  (£)240	M1  A1 B1 B1  M1 A1 6	Ignore 1s included FT for equivalent level of difficulty FT for equivalent level of difficulty from (i)  Allow with sight of the smaller share

Methods in Mathematics Unit 1 Higher Tier	Mark	Comments
<p>6(a) Reason, e.g. ‘all multiples of 10 are multiples of 5’, ‘multiples of 10 are also multiples of 5’, ‘not all multiples of 5 are multiples of 10’, ‘multiples of 10 is a subset of multiples of 5’</p> <p>(b)(i) 6 numbers placed correctly</p>  <p>(ii) 0 1/6 2/6 (= 1/3)</p>	<p>E1</p> <p>B3</p> <p>B1 B1 B1 7</p>	<p>Do not accept ‘some multiples of 10 are also multiples of 5’</p> <p>B2 for 4 or 5 numbers uniquely placed correctly, the other 2 or 1 number(s) respectively omitted or incorrectly placed or repeated, OR B1 for 2 or 3 numbers uniquely placed correctly, the other 4 or 3 numbers respectively omitted or incorrectly placed or repeated</p> <p><i>Penalise extra numbers included -1 throughout</i></p> <p><i>In (b)(ii) ignore incorrect cancelling.</i> FT their Venn diagram CAO</p>
<p>7(a) <math>360 \div 18</math> 20 (sides)</p> <p>(b) (Total of interior angles) <math>3 \times 180(^{\circ})</math> 540(<math>^{\circ}</math>)</p> <p><math>125(^{\circ}) + 130(^{\circ}) + 135(^{\circ}) + \dots + \dots =</math> sum of interior angles of a polygon <math>(540(^{\circ}) - 390(^{\circ})) \div 2</math> or <math>150(^{\circ})/2</math> (Each interior angle is ) 75(<math>^{\circ}</math>)</p> <p>QWC2: Candidates will be expected to</p> <ul style="list-style-type: none"> <li>present work clearly, with words explaining process or steps</li> </ul> <p><b>AND</b></p> <ul style="list-style-type: none"> <li>make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer</li> </ul> <p>QWC1: Candidates will be expected to</p> <ul style="list-style-type: none"> <li>present work clearly, with words explaining process or steps</li> </ul> <p><b>OR</b></p> <ul style="list-style-type: none"> <li>make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer</li> </ul>	<p>M1 A1</p> <p>M1 A1</p> <p>M1</p> <p>m1 A1</p> <p>QWC 2</p> <p>9</p>	<p>Or equivalent <b>complete</b> method</p> <p>or <math>5 \times (180(^{\circ}) - 360(^{\circ}) \div 5)</math> alternative full method</p> <p>FT ‘their 540’ provided &gt; 390</p> <p>Rearranged form or manipulated correctly to this stage of working</p> <p><i>Alternative:</i> (Exterior angles are) <math>180(^{\circ}) - 125(^{\circ}), 180(^{\circ}) - 130(^{\circ})</math> &amp; <math>180(^{\circ}) - 135(^{\circ})</math> <i>M1</i></p> <p>(Each remaining exterior angle) FT from M1 <math>360(^{\circ}) - 55(^{\circ}) - 50(^{\circ}) - 45(^{\circ})</math> <math>\div 2</math> <i>M1</i> <i>m1</i></p> <p>(depends on at least M1 previously awarded) (Each exterior angle is) 105(<math>^{\circ}</math>) CAO <i>A1</i> (Each interior angle is) 75(<math>^{\circ}</math>) <i>A1</i> FT 180 – ‘their 105’ provided M1, M1 and m1 awarded</p> <p>QWC2 Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.</p> <p>QWC1 Presents relevant material in a coherent and logical manner but with some errors in use of mathematical form, spelling, punctuation or grammar OR evident weaknesses in organisation of material but using acceptable mathematical form, with few if any errors in spelling, punctuation and grammar.</p> <p>QWC0 Evident weaknesses in organisation of material, and errors in use of mathematical form, spelling, punctuation or grammar.</p>

Methods in Mathematics Unit 1 Higher Tier	Mark	Comments																																													
<p>8(a) Showing 6 can be scored in 3 ways,  <math>6 \times 1</math> <math>2 \times 3</math> (and <math>3 \times 2</math>) with no others            Idea that there are 32 possible outcomes</p> <p style="text-align: right;">9</p> <p>(b) Considering all possibilities, e.g.  <math>\text{odd} \times \text{even} = \text{even}</math>, <math>\text{even} \times \text{odd} = \text{even}</math>, <math>\text{odd} \times \text{odd} = \text{odd}</math> and  <math>\text{even} \times \text{even} = \text{even}</math>, OR</p> <table border="1" data-bbox="240 745 735 875"> <thead> <tr> <th></th> <th>1</th> <th>2</th> <th>3</th> <th>4</th> <th>5</th> <th>6</th> <th>7</th> <th>8</th> </tr> </thead> <tbody> <tr> <th>1</th> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> <td>7</td> <td>8</td> </tr> <tr> <th>2</th> <td>2</td> <td>4</td> <td>6</td> <td>8</td> <td>10</td> <td>12</td> <td>14</td> <td>16</td> </tr> <tr> <th>3</th> <td>3</td> <td>6</td> <td>9</td> <td>12</td> <td>15</td> <td>18</td> <td>21</td> <td>24</td> </tr> <tr> <th>4</th> <td>4</td> <td>8</td> <td>12</td> <td>16</td> <td>20</td> <td>24</td> <td>28</td> <td>32</td> </tr> </tbody> </table> <p>Appropriate conclusion, e.g. stating that possible products more often give even, OR            stating possibility of odd 8 times with even 24 times,            or equivalent, OR <math>P(\text{even}) = 24/32</math> or <math>P(\text{odd}) = 8/32</math></p>		1	2	3	4	5	6	7	8	1	1	2	3	4	5	6	7	8	2	2	4	6	8	10	12	14	16	3	3	6	9	12	15	18	21	24	4	4	8	12	16	20	24	28	32	<p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>E1</p> <p>5</p>	<p>Do not accept if <math>1 \times 6</math> also given</p> <p>Accept from sight of <math>4 \times 8</math> or <math>1/8 \times 1/4</math> or similar            Allow from incorrect evaluation of a suitable calculation</p> <p>FT 'their 3 ways' provided <math>6 \times 1</math> is considered or            'their 32' outcomes provided their number of            outcomes is <math>&gt;24</math>, that is  <math>(96 \div \text{'their number of outcomes'}) \times \text{'their 3 ways'}</math>,            accept approximation or rounding of division to a            whole number            An answer only given as a probability, <math>9/96</math>, is            awarded B1, B1, B0</p> <p>Accept for sight of <math>24/32</math> or <math>8/32</math></p> <p>FT from 2 errors in the evaluation of the products  <i>Award B1 and E1 for a statement such as            'You <b>only</b> get odd numbers from odd times odd'</i>            If no marks, award SC1 for '<math>\text{even} \times \text{odd} = \text{even}</math>'            with an appropriate conclusion stated</p>
	1	2	3	4	5	6	7	8																																							
1	1	2	3	4	5	6	7	8																																							
2	2	4	6	8	10	12	14	16																																							
3	3	6	9	12	15	18	21	24																																							
4	4	8	12	16	20	24	28	32																																							
<p>9(a) Correctly completing the tree diagram 0.4, 0.8,            0.8, 0.2            (b) <math>0.6 \times 0.2</math>                  = 0.12            (c) <math>0.4 \times 0.2</math>                  = 0.08</p>	<p>B2</p> <p>M1 A1</p> <p>M1 A1 6</p>	<p>B1 for any one pair of branches correct (total 1)</p> <p>Or equivalent</p> <p>FT for their tree diagram            Or equivalent</p>																																													

Methods in Mathematics Unit 1 Higher Tier	Mark	Comments
10(a) 12  (b) 10 (with no working or from correct working)  (c) $6 \times 10^{-5}$  (d) $3 \times 10^{12}$  (e) $\frac{17\pi}{4}$ or $4\frac{1}{4}\pi$ or $4.25\pi$	B2  B3  B1  B2  B2  10	B1 for one <b>appropriate</b> step, e.g. cancelling $\sqrt{5}/\sqrt{5}$ , or sight of $\sqrt{9}$ or 3, not $(\sqrt{3})^2$ Do not accept $4\sqrt{45}/\sqrt{5}$ until simplified  B2 for 5 <b>AND</b> .../9 respectively B1 for 5 <b>OR</b> .../9 respectively For B2 or B1 the 5, .../9 may be in working, rather than expressed as a quotient  B1 for 3 000 000 000 000 or sight of $\dots \times 10^{12}$  Mark final answer B1 for $\frac{10\pi}{4} + \frac{7\pi}{4}$ or $2.5\pi + 1.75\pi$ or equivalent
11. Strategy, e.g. 'square + 1 + square' OR attempt to look at second difference           $(n+1)^2 + 1 + \dots$ or $\dots + 1 + n^2$ or second difference 4  $(n+1)^2 + 1 + n^2$ or $2n^2 + 2n + 2$ or equivalent	S1      M1  A1  3	OR break down, for a couple of patterns into: " 'larger square' + 1 + 'smaller square' " Maybe implied by $\dots + n^2$ or $(n+1)^2 + \dots$ or for example $'6^2 + 5^2 + 1'$ , OR for giving the correct number of squares in any pattern number $>4$ (strictly $>4$ , not for pattern 4), not for Pattern number 5 written in the table for Pattern n, but allow if shown in a sequence  Implies S1 also. Allow for $'n^2 + 1 + n^2'$ or $'n^2 + 1 + (n-1)^2'$ or similar ISW $n+1 \times n+1 + 1 + n^2$ is awarded S1, M1, A0
12. $y = -x^2$ $y = 1/x$ $y = x^3 + 1$	B1 B1 B1 3	
13. $12 \times 2 = 4 \times k$ $k = 6$ (cm)	M1 A1  2	Do not accept from incorrect working, e.g. $4 + 2$ , is awarded M0, A0
14(a) Correct region shaded 	B1	
(b) Correct region shaded 	B1  2	

<b>Methods in Mathematics Unit 1 Higher Tier</b>	<b>Mark</b>	<b>Comments</b>
15. (a) 1 or equivalent  (b) $P(\text{odd, even}) + P(\text{even, odd})$  $\frac{4}{5} \times \frac{1}{4} + \frac{1}{5} \left( \times \frac{4}{4} \right)$ $= \frac{8}{20} (= \frac{4}{10} = \frac{2}{5})$	B1  S1  M1  A1  4	<i>Penalise incorrect cancelling of fractions-1 once</i>  OR listing 10 correct no reverse combinations, or 20 correct combinations, or sight of 20 outcomes (e.g. for $5 \times 4$ ) Listing all 20 combinations and selecting the correct 8 odd results, or 10 combinations and selection of 4 odd results Accept a correct answer from 10 possible combinations. Allow M1 A0 if FT from 1 slip in counting the combinations
16(a) $2x^2 + 4x - 5x - 10 + 3 - 3x + 2x - 2x^2 (+1)$ or $\frac{2x^2}{2x^2} - \frac{x}{x} - 10 + 3 - x - 2x^2 (+1)$  $-2x - 6 =$ $-2(x + 3)$  (b) $(x + 3)(x + 4)$ $(x + 3)(x - 3)$ $\frac{x + 4}{x - 3}$	M2  A1 A1  B1 B1 B1  7	M1 for any 4 terms correct  Must be convincing from sight of $-2x - 6$ Allow expanding RHS provided M2, A1 previously awarded  Mark final answer. FT for equivalent level of difficulty provided B1 previously awarded and cancelling required
17(a)(i) $3x(^{\circ})$ or equivalent  (ii) $90(^{\circ}) - x(^{\circ})$  (iii) $2x(^{\circ})$  (b) $180(^{\circ}) - 2x(^{\circ})$ or equivalent Reason, '(Opposite angles of a) cyclic quadrilateral (are supplementary)'	B1  B1  B1  B1 E1 5	Mark final answer  Mark final answer  Mark final answer  Mark final answer Depends on the sight of $S\hat{J}F = 180(^{\circ}) - 2x(^{\circ})$ or equivalent
18(a) $\frac{4(2x - 3) - 3(x + 5)}{12}$ as a numerator as a denominator  $\frac{5x - 27}{12}$  (b) $(x + 9)^2 + 19$	B1 B1  B1  B2  5	Not depending on a correct denominator Attempt common denominator 12 or multiple of 12  Mark final answer  B1 for $a = (+)9$ , B1 for $b = (+)19$ , only award B2 for $(x + 9)^2 + 19$
19(a) $y = \frac{1}{3}x - 5$ or equivalent  (b) Perpendicular gradient -3 Mid point $\frac{6 + -2}{2}$ or $\frac{5 + -5}{2}$  $(2, 0)$ $y = -3x + 6$	B2  M1 M1  A1 A1 6	Accept $y = \frac{2x}{6} + -5$ or equivalent Mark final answer B1 for $m = \frac{1}{3}$ or equivalent, B1 for $c = -5$ Only award B2 if given as an equation  FT -1/their m Sight of $(\dots, 0)$ is insufficient evidence for M1 Accept attempt to plot the 2 points with attempt to find the mid-point  ISW. FT provided M1 and M1 both awarded