



# **GCSE MARKING SCHEME**

**MATHEMATICS - UNITISED**

**JANUARY 2013**

## INTRODUCTION

The marking schemes which follow were those used by WJEC for the January 2013 examination in GCSE MATHEMATICS - UNITISED. They were finalised after detailed discussion at examiners' conferences by all the examiners involved in the assessment. The conferences were held shortly after the papers were taken so that reference could be made to the full range of candidates' responses, with photocopied scripts forming the basis of discussion. The aim of the conferences was to ensure that the marking schemes were interpreted and applied in the same way by all examiners.

It is hoped that this information will be of assistance to centres but it is recognised at the same time that, without the benefit of participation in the examiners' conferences, teachers may have different views on certain matters of detail or interpretation.

WJEC regrets that it cannot enter into any discussion or correspondence about these marking schemes.

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## UNIT 1 - FOUNDATION TIER

UNIT 1 Foundation Tier	✓	Mark	Final Mark Scheme Comments																		
1(a) (i) 72034		B1																			
1(a)(ii). Five hundred and forty thousand, two hundred and seven.		B1																			
1(b). (Ten percent =) 6657 $6657 \times (\pounds)3$ $= (\pounds)19971$ (To nearest thousand) $(\pounds)20000$ .	✓ ✓ ✓ ✓	B1 M1 A1 A1	F.T. 'their 6657'. F.T. 'their 19971'.																		
2(a). 38		B1																			
2(b). Indicates '2 <sup>nd</sup> notch to the right of 80'.		B1	Allow unambiguous intent.																		
3. An <u>attempt</u> to find values that may be directly compared.  Finding (25%) 30% and 20% OR 25/100 30/100 and 20/100 or equivalent. OR 0.25 0.3 and (0.2) OR three correct calculations for a common amount. (Best bonus scheme from) Company B		M1  A1  A1	All %, OR all fractions with common denominator, OR all decimals, OR using a common amount for sales made, OR a valid combination.  Accept 2.5/10 if comparing 'tenths'.  F.T. if only one error made. Accept any unambiguous indication that Company B has been chosen (e.g. '3/10 is best'). SC1 if Company B chosen but with no supporting work.																		
4. (75 – 99) (100 – 124) <b>125 – 149</b> (150 – 174) Using a tally convention. (6) 8 12 4	✓ ✓ ✓ ✓	B1 B1 B2 B2	Need not be accurate. B2 for all three correct. B1 for 1 or 2 correct.																		
<b>Ribbon marking for 5(a) and 5(b).</b> 5(a). Cost = $24 \times (\pounds)35 + (\pounds)70$ $= (\pounds)910$  5(b). Monthly payment = $\frac{(\pounds)530 - (\pounds)50}{24}$ $= (\pounds)20$		M1 A1  M1  A1	Correctly substituted. M0 if $24 \times (\pounds)105$ attempted.  Correct substitution showing subtraction and division.  Allow embedded reference to the correct answer.																		
6. <table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th>Position</th> <th>Name of Dog</th> <th>Weight</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>Nell</td> <td>(10.6kg)</td> </tr> <tr> <td>2</td> <td>Smot</td> <td>(9kg 624gm)</td> </tr> <tr> <td>3</td> <td>Buster</td> <td>(8.72kg)</td> </tr> <tr> <td>4</td> <td>Rover</td> <td>(8.572kg)</td> </tr> <tr> <td>5</td> <td>Peg</td> <td>(7964gm)</td> </tr> </tbody> </table>	Position	Name of Dog	Weight	1	Nell	(10.6kg)	2	Smot	(9kg 624gm)	3	Buster	(8.72kg)	4	Rover	(8.572kg)	5	Peg	(7964gm)		B3	Mark the order of names only. Disregard any weights that are not given in the question. Allow unambiguous use of friends' names or weights instead of dogs' names.  B1 for Nell AND Peg in correct positions B1 if 'Smot > Buster'. B1 if 'Buster > Rover'.  <i>SC1 for complete reversal of names.</i>
Position	Name of Dog	Weight																			
1	Nell	(10.6kg)																			
2	Smot	(9kg 624gm)																			
3	Buster	(8.72kg)																			
4	Rover	(8.572kg)																			
5	Peg	(7964gm)																			
7(a). 6		B1																			
<b>Ribbon marking for 7(b), 7(c) and 7(d).</b>  7(b). 4 (min) 8 (sec)  7(c). 3 (min) 47 (sec)  7(d). 21 s(econds)		B1 B1 B2	SC1 if both <u>correct</u> answers to (b) and (c) are reversed. (Award this SC1 in part (c).)  F.T. the time difference between their (b) and their (c). B1 for 21 OR B1 for -21 s(econds) B0 for -21																		
8. Showing an understanding of range. (Maximum range for Adam = ) 59 (Minimum range for Ben = ) 41		S1 B1 B1	Must be for runs scored. OR B2 for finding a possible range for Adam that is greater than a possible range for Ben.																		





## UNIT 1 - HIGHER TIER

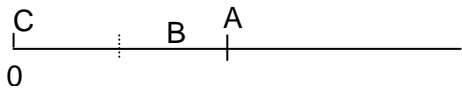
UNIT 1 Higher Tier	✓	Mark	Final Mark Scheme Comments																		
1. (F ⇒) $100 \times 100 - 100^2$ = 0		M1 A1																			
2(a). Attempt at $\sum f \times x$ (162) Division by $\sum f$ (20)  (Mean ⇒) 8.1 (goals)		M1 m1  A1	C.A.O. Accept 8 (goals) only if 162/20 seen.																		
<b>Ribbon marking for 2(b)(i) and 2(b)(ii).</b> 2(b)(i). <table border="1" style="margin: 5px 0;"><tr><td>1-5</td><td>6-10</td><td>11-15</td><td>16-20</td><td>21-25</td><td>26-30</td></tr><tr><td>3</td><td>10</td><td>6</td><td>0</td><td>1</td><td>0</td></tr></table> <table border="1" style="margin: 5px 0;"><tr><td>1-10</td><td>11-20</td><td>21-30</td></tr><tr><td>13</td><td>6</td><td>1</td></tr></table> 2(b)(ii) E.g. 'Kick because it is more detailed'. 'Penalty! because its less cluttered'.	1-5	6-10	11-15	16-20	21-25	26-30	3	10	6	0	1	0	1-10	11-20	21-30	13	6	1		B2  E1	'Blank spaces' to be taken as 0.  For all 9 correct entries. B1 for 7 or 8 correct entries. Allow F.T. from 'Kick' table to 'Penalty!' table.  Reason must be valid for their choice.
1-5	6-10	11-15	16-20	21-25	26-30																
3	10	6	0	1	0																
1-10	11-20	21-30																			
13	6	1																			
3. Three different valid comments.  e.g. 'Not representative.' 'Should only be distributed to car owners', 'Does not ask about the age of the car', 'Does not specify over what period of time', 'How are the questionnaires returned?', 'People might confuse quantity with cost', 'Engine size' 'Type of fuel (diesel/petrol)'	✓  ✓  ✓	B3	B1 for each different valid comment.  Accept equivalent statements e.g. 'biased' (by location).  Do not give more than one mark for the same criticism(s).																		
<b>Ribbon marking for 4(a) and 4(b).</b> 4(a). Bearing of $058^\circ$ from Cherbourg.  Bearing of $135^\circ$ from Portsmouth.  Position marked OR two lines intersecting.  4(b). (Distance ⇒) $3.9 \times 20$ (= 78) (Speed ⇒) $\frac{3.9 \times 20}{4}$ = 19.5 (km/h)		M1  M1  A1  M1 M1  A1	<b>Use overlay.</b> $\pm 2^\circ$ (use overlay). Allow the M marks for dots, crosses or any unambiguous indication that the correct bearings have been offered.  F.T. if at least M1 and two intersecting lines.  <b>Use measuring tool.</b> F.T. their ship's position. Accept $\pm 0.2\text{cm}$ .  Dependent on both M marks.																		
5. (Jack receives) $450 \div 1.2$ = (£)375  (Gillian receives) $400 \times 1.08$ = 432(euros)	✓ ✓ ✓ ✓	M1 A1 M1 A1	<i>Alternative method</i> $450 \div 400$ M1 = 1.125 A1 $1.08 < 1.125 < 1.2$ E1 $1.125 < 1.2$ better for Jack E1 $1.125 > 1.08$ better for Gillian E1																		
A clearly stated explanation that <u>each</u> would have received more of their required currency by swapping.	✓	E1	Explanation should refer to amounts. Allow one arithmetical slip when awarding E mark.																		

UNIT 1 Higher Tier	✓	Mark	Final Mark Scheme Comments
<p>6. (Total income =) (£)44600 (Taxable income =) (£)37125 A correct method of finding 20% or 40% of a relevant value. (Tax due =) (£) 850 (+ 7000) = (£)7850.</p> <p>(Tax paid =) (£)8920</p> <p>AND a correct statement for their amount</p> <p>Look for</p> <ul style="list-style-type: none"> <li>• spelling</li> <li>• clarity of text explanations,</li> <li>• the use of notation (watch for the use of '=', £, % being appropriate)</li> </ul> <p>QWC2: Candidates will be expected to</p> <ul style="list-style-type: none"> <li>• present work clearly, with words explaining process or steps</li> </ul> <p>AND</p> <ul style="list-style-type: none"> <li>• make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer</li> </ul> <p>QWC1: Candidates will be expected to</p> <ul style="list-style-type: none"> <li>• present work clearly, with words explaining process or steps</li> </ul> <p>OR</p> <ul style="list-style-type: none"> <li>• make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer</li> </ul>	<p>✓</p> <p>✓</p> <p>✓</p> <p>✓</p> <p>✓</p> <p>✓</p> <p>✓</p> <p>✓</p> <p>✓</p> <p>✓</p>	<p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>A2</p> <p>A2</p> <p>QWC 2</p> <p>QWC</p> <p>QWC</p>	<p>F.T. 'their total income' – 7475.</p> <p>F.T. 40% of ['their 37125' – 35000]. F.T. 'their 850' + 'their 7000'.</p> <p>F.T. 20% of 'their 44600'. OR showing £7850 to be 17.6% of £44600. A1 if no statement or an incorrect statement.</p> <p>QWC2. Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.</p> <p>QWC1. Presents relevant material in a coherent and logical manner, but with some errors in use of mathematical form, spelling, punctuation or grammar. OR Evident weakness in organisation of material but using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.</p> <p>QWC0. Evident weakness in organisation of material and errors in use of mathematical form, spelling, punctuation and grammar.</p>
<p>7. (The following are for using the two times linked to Carol as a starting point). Looking at time differences.</p> <p>(Differences) 2days, 7hours, 10min</p> <p>(Bryn phoned on 'Wed 6.24am + 2days 7hrs 10min') <u>Friday</u> at <u>1</u> : <u>34</u> p.m.</p> <p>OR</p> <p>(The following are for using the two times linked to the answering machine as a starting point). Looking at time differences.</p> <p>(Differences) 1days, 4hours, 6min</p> <p>(Bryn phoned on 'Sat 5.40pm – 1day 4hrs 6min') <u>Friday</u> at <u>1</u> : <u>34</u> p.m.</p>	<p>✓</p> <p>✓</p> <p>✓</p> <p>✓</p> <p>✓</p> <p>✓</p> <p>✓</p> <p>✓</p> <p>✓</p>	<p>M1</p> <p>A2</p> <p>A2</p> <p>A2</p> <p>OR</p> <p>M1</p> <p>A2</p> <p>A2</p>	<p>Award M1 if any one of the following is being considered, Sat/Thurs OR 5pm/10am OR 40/30. A1 for one correct difference. Units not required as long as each value is unambiguously identifiable.</p> <p>F.T. their differences. A1 for one correct. Must have p.m. (or a.m. on a FT) or correct 24-hour time for the A2.</p> <p>OR</p> <p>Award M1 if any one of the following is being considered, Wed/Thurs OR 6am/10am OR 24/30. A1 for one correct difference. Units not required as long as each value is unambiguously identifiable.</p> <p>F.T. their differences. A1 for one correct. Must have p.m. (or a.m. on a FT) or correct 24-hour time for the A2.</p>
<p>8. 87% = (£)4760000 (Last year's profit) <math>\frac{4760000}{87} \times 100</math> = (£)5471264(.368) = (£)5470000</p>	<p>✓</p> <p>✓</p> <p>✓</p> <p>✓</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>B1</p>	<p>Accept any indication.</p> <p>F.T. from above if of equivalent difficulty.</p>

UNIT 1 Higher Tier	✓	Mark	Final Mark Scheme Comments
9. Sight of (diameter =) 49.5 (cm) Sight of (length =) 45.5 (cm) AND (width =) 32.5(cm)  (Circumference =) $\pi \times 49.5$ OR (Perimeter =) $2 \times (45.5 + 32.5)$ (Crcmf. =) 155.5(cm) AND (Perim. =) 156(cm) A clear statement that the length of tape around the rectangular base can be longer than the length around the circular base.	✓ ✓ ✓ ✓ ✓	B1 B1  M1 A1 A1	Or (radius =) 24.75 (cm) <i>Ignore other values.</i>  F.T. their values as long as ‘diameter’ < 50, ‘length’ > 45 and ‘width’ > 32. Accept 155.4 to 155.6 for circumference. Accept equivalent wording as long as it is consistent with ‘Perimeter’ > ‘Circumference’.
10. $12 \times \frac{72000}{54000}$  $\times \frac{1}{2}$  = 8 (hrs)		M1  M1  A1	Or equivalent work.  Or equivalent work.  C.A.O.
<b>Ribbon marking for 11(a) and 11(b).</b>			
11(a). $\frac{80}{360} \times 2 \times \pi \times 15$  = 20.9(4....) (cm) OR $20\pi/3$  11(b). $\frac{360 - 80}{360} \times \pi \times 15^2$  = 549(.77...) (cm <sup>2</sup> ) OR $175\pi$		M1  A1  M2  A1 5	Accept 20.9 to 21 inclusive.  M1 for $\frac{80}{360} \times \pi \times 15^2$ and A1 for 157(.07..) Accept 549 to 550 inclusive.
12  Use made of ‘Distance / Time’. Use made of ‘1000 metres in 1 km’. Use made of ‘1 mile ≈ 1.6km’. Use made of ‘3600 seconds in 1 hour’.  $\left[ \frac{60}{1000} \times \frac{3600}{1.6 \times 3} \right]$  = 45 (mph)	✓ ✓ ✓ ✓         ✓	M1 M1 M1 M1         A1	Candidates may earn these M marks (or some of them) in the order that they undertake each step. <i>(Watch out for embedded ‘multiple method’ steps.)</i> <i>(Ignore units at this stage.)</i> E.g. (i) $60/3 = 20(\text{ms}^{-1})$ $20 \times 3600 = 72000(\text{mh}^{-1})$ $72000/1000 = 72(\text{kmh}^{-1})$ $72/1.6$  E.g. (ii) 1mile = 1600m (2 <sup>nd</sup> M1 and 3 <sup>rd</sup> M1) $1600/20 = 80$ (1 <sup>st</sup> M1 implied by 20) $3600/80$ (4 <sup>th</sup> M1)  (To gain <u>all four</u> M marks then candidates must make <u>correct use</u> of each one.) <i>Note when part methods are earned</i> E.g. $20/1600 (= 0.0125)$ M1, M1, M1, M0 A0 if any pre-approximations used.
13. (Volume of cone =) $\frac{1}{3} \times \pi \times 12^2 \times h$ (Volume of cylinder =) $\pi \times 12^2 \times 5h$  20 litres = 20000 (cm <sup>3</sup> )  $20000 = \frac{1}{3} \times \pi \times 12^2 \times h + \pi \times 12^2 \times 5h$  $h = \frac{3 \times 20000}{144 \times \pi \times 16}$ or equivalent  = 8.28(93..)  (Total height =) 49.7(.....) (cm)	✓ ✓ ✓ ✓  ✓ ✓ ✓ ✓	B1 B1  B1  M1  A1  A1  A1	Accept any notation or word(s) for ‘height’. B1 given only when its height is noted as 5× height of cone.  B1  F.T their ‘20000’. F.T. their two volumes only if of equivalent form (i.e. contains ‘ $\pi$ ’ AND the <u>height of the cylinder expressed as a multiple of the height of the cone.</u> )  Accept correct to 1dp.  F.T. 6 × ‘their 8.28(93..)’



## UNIT 2 - FOUNDATION TIER

UNIT 2 (Non calculator) Foundation Tier	Marks	Final Mark Scheme Comments
1. (a) (i) 19526	B1	
1. (a) (ii) Thirty thousand and fifty four	B1	Ignore extra words such as 'pounds. Ignore slight misspellings.
1. (b) (i) 32, 38	B1	
1. (b) (ii) 57	B1	
1. (b) (iii) 35	B1	
1. (c) (i) 36800	B1	
1. (c) (ii) 36830	B1	
1. (d) (i) 42, 48	B1, B1	-1 for each extra incorrect number.
1. (d) (ii) 49	B1	B1 for $7 \times 7$ OR $7^2$ , but B0 for $7 \times 7 = \text{wrong number}$ . B0 for 7.
2. mm OR cm OR m g km l(itres)	B1 B1 B1 B1	
3. (a) 9	B1	
3. (b) 	B1 B1 B1	A should be at the half way mark. B should be between $\frac{1}{4}$ and $\frac{1}{2}$ <u>exclusive</u> (Between the c and h of 'Rachel') C should be at 0.
4. (a) (i) Subtract 9 from the previous term (ii) Multiply the previous term by 4	B1 B1	Accept - 9 Accept $\times 4$
4. (b) (0).15	B1	
4. (c) $\frac{40}{100} \times 70$ = 28	M1 A1	Any correct method for finding 40% M1, A0 for incorrect units, e.g. 28% or £28
4. (d) For the '8' sequence (+ 3) For the '12' sequence (+ 3) 27	B1 B1 B1	8, 16, 24, (32), ... OR 11, 19, 27, (35), ... 12, 24, ..... OR 15, 27, .... Award B3 for an answer of 27. SC1 for 24.

UNIT 2 (Non calculator) Foundation Tier	Marks	Final Mark Scheme Comments
<p><b>Indirect marking - Tick marked</b></p> <p>5. Cost of entrance fee for children = (£) <math>8 \times 5 \times 9</math> OR <math>8 \times 45</math> = (£) 360</p> <p>Total cost of adult tickets = (£) <math>523 - 360 - 115</math> = (£) 48</p> <p>Number of adults = <math>48/12</math> = 4</p> <p>Look for</p> <ul style="list-style-type: none"> <li>• spelling</li> <li>• clarity of text explanations,</li> <li>• the use of notation (watch for the units (£, p))</li> </ul> <p>QWC2: Candidates will be expected to</p> <ul style="list-style-type: none"> <li>• present work clearly, with words explaining process or steps</li> </ul> <p>AND</p> <ul style="list-style-type: none"> <li>• make few if any mistakes in mathematical form, spelling, punctuation and grammar in their final answer</li> </ul> <p>QWC1: Candidates will be expected to</p> <ul style="list-style-type: none"> <li>• present work clearly, with words explaining process or steps</li> </ul> <p>OR</p> <p>make few if any mistakes in mathematical form, spelling, punctuation and grammar in their final answer.</p>	<p>✓</p> <p>M1 A1 M1 A1 M1 A1</p> <p>QWC 2</p>	<p>F.T. 'their 360'</p> <p>F.T. 'their 48'</p> <p>QWC2 Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.</p> <p>QWC1 Presents relevant material in a coherent and logical manner but with some errors in use of mathematical form, spelling, punctuation or grammar.</p> <p>OR</p> <p>Evident weaknesses in organisation of material but using acceptable mathematical form, with few if any errors in spelling, punctuation and grammar.</p> <p>QWC0 Evident weaknesses in organisation of material, and errors in use of mathematical form, spelling, punctuation and grammar.</p>
<p><b>Indirect marking - Tick marked</b></p> <p>6. Either <math>\frac{1}{4}</math> of £600 = (£)150 <math>\frac{1}{5}</math> of £600 = (£)120 Remainder = (£) 330</p> <p>Fraction = <math>330/600</math> = <math>11/20</math>. If 'their <math>330/600</math> cannot be reduced then A0</p> <p>OR <math>\frac{1}{4} + \frac{1}{5}</math> = <math>9/20</math> Remainder = <math>1 - 9/20</math> = <math>11/20</math></p>	<p>✓</p> <p>B1 B1</p> <p>M1 A1</p>	<p>Any incorrect method for adding fractions, e.g. <math>2/9</math> gets M0 C.A.O.</p> <p>F.T. their first part. .55 OR 55% get M1, A0</p>
<p>7.</p>	<p>B2</p>	<p>B1 for each quadrant</p>
<p>8. (a) <math>4x - 2y</math></p>	<p>B2</p>	<p>B1 for either in an expression of the form <math>af(x) \pm bg(y)</math> Allow B1 for <math>4-2y</math> OR <math>4x-2</math> etc <math>4x</math> and <math>-2y</math> separated gets B1 <math>4x+-2y</math> gets B1</p>
<p>8. (b) (i) <math>(y=) 72</math></p>	<p>B1</p>	<p>Accept embedded answers such as <math>72/6 = 12</math></p>
<p>8. (b) (ii) <math>7x = 28</math> <math>x = 4</math></p>	<p>B1 B1</p>	<p>Isolate the x term F.T. <math>ax = b</math> (<math>a \neq 1</math>) B0 for <math>28/7</math> Accept embedded answers such as <math>7 \times 4 - 8 = 20</math></p>
<p>8. (c) <math>5(n + 4)</math> OR <math>(n + 4)5</math> OR <math>5n + 20</math></p>	<p>B2</p>	<p>B1 for <math>5 \times n+4</math> OR <math>n+4 \times 5</math>. B0 for <math>5n + 4</math></p>

UNIT 2 (Non calculator) Foundation Tier	Marks	Final Mark Scheme Comments
<p><b><u>Indirect marking - Tick marked</u></b></p> <p>9.(Monthly saving =) <math>0.15 \times 1260</math> (£)189 (Needs to save £1340 - £584 = £)756 (more) (Number of months =) <math>756/189</math> or equivalent</p> <p style="text-align: center;">4 (months)</p>	<p>✓ M1 A1 B1 m1</p> <p>A1</p>	<p>An answer of 18.9(0) implies M0</p> <p>FT 'their 189' provided M1 awarded or if place value error in digits 1890 And FT 'their 756' Or repeat addition, with 189, 378, 567 shown, or any 3 correct terms in an appropriate summation series with no more than 1 incorrect, or <math>2 \times 378</math> seen</p> <p>As a final answer. If units are given they must be correct Depends on M1 and m1 and must FT for their values including rounding up if necessary</p> <p>Alternative: <span style="float: right;">Memo</span>  <math>0.15 \times 1260</math> <span style="float: right;">M1</span> <span style="float: right;">584</span>  <math>=</math> (£)189 <span style="float: right;">A1</span> <span style="float: right;">773</span>  <math>584 + 189 + 189</math> <span style="float: right;">m1 (no extra)</span> <span style="float: right;">962</span>  <math>+ 189 + 189 = 1340</math> <span style="float: right;">A1</span> <span style="float: right;">1151</span>  OR reverse calculation working back from 1340 <span style="float: right;">1340</span>  4 (months) <span style="float: right;">A1</span></p> <p>Unsupported 4 gets 0</p>
<p>10. (a) Realising only 1 way to score 14, i.e. <math>8+6</math> OR '8 and 6' Number of possible outcomes <math>6 \times 8 (=48)</math></p> <p style="text-align: center;"><math>1/48</math></p> <p>(b) 1</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p>	<p>Do not accept <math>\frac{1}{6} + \frac{1}{6}</math> as evidence Accept sight of <math>6 + 8 = 14</math> Accept sight of <math>./48</math> or <math>./8 \times ./6</math> Sight of <math>\frac{1}{8} \times \frac{1}{6}</math> is awarded B1, B1 with no other ways CAO <i>An answer of 1:48 gets B2</i> Accept fractions equivalent to 1 and 100% B0 for 'certain' B0 for incorrect notation such as 14 out of 14, 14:14 etc</p>
<p><b><u>Indirect marking - Tick marked</u></b></p> <p>11. <math>\hat{ADC} = 90^\circ</math> <math>\hat{FDE} = 60^\circ</math> <math>\hat{FDA} = 30^\circ</math> <math>\hat{AFD} = 30^\circ</math> <math>\hat{DFE} = 60^\circ</math> Therefore <math>\hat{AFE} = 90^\circ</math> OR <math>270^\circ</math></p>	<p>✓</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p>	<p>Watch out for work on the DIAGRAM, but work given on the dotted lines takes precedence in any conflict.</p> <p>Any angle in the square Any angle in the equilateral triangle C.A.O. F.T. their <math>\hat{FDA}</math></p> <p>F.T. 60 + their <math>\hat{DFA}</math></p> <p>Unsupported answer of <math>90^\circ</math> gets 0.</p>
<p><b><u>All parts (a) – (c) marked at the same time</u></b></p> <p>12. (a) 11</p> <p><b><u>Use overlay</u></b></p> <p>12. (b) Plots All correct plots joined with a curve</p> <p>12. (c) From their graph (approximately -2.2 and 1.6)</p>	<p>B1</p> <p>P1 C1</p> <p>B1</p>	<p>Allow one error. FT 'their (a)' or 11 FT 'their (a)' or 11. If (a) blank then FT points given, otherwise must include plot at <math>x=-3</math></p> <p>FT their graph. x-values, coordinates are not required</p>

## UNIT 2 - HIGHER TIER

UNIT 2 Higher Tier	Mark	Final Mark Scheme Comments												
<p>1.(Monthly saving <math>\Rightarrow</math>) <math>0.15 \times 1260</math> (£)189 (Needs to save <math>\pounds 1340 - \pounds 584 = \pounds 756</math> (more) (Number of months <math>\Rightarrow</math>) <math>756/189</math> or equivalent</p> <p style="text-align: center;">4 (months)</p> <p>Look for</p> <ul style="list-style-type: none"> <li>spelling</li> <li>clarity of text explanations,</li> <li>the use of notation (watch for the units 'months' and £)</li> </ul> <p>Needs to have sufficient stages of working processed for QWC2</p> <p>QWC2: Candidates will be expected to</p> <ul style="list-style-type: none"> <li>present work clearly, with words explaining process or steps AND</li> <li>make few if any mistakes in mathematical form, spelling, punctuation and grammar in their final answer</li> </ul> <p>QWC1: Candidates will be expected to</p> <ul style="list-style-type: none"> <li>present work clearly, with words explaining process or steps OR</li> <li>make few if any mistakes in mathematical form, spelling, punctuation and grammar in their final answer</li> </ul>	<p>M1 A1 B1 m1</p> <p>A1</p> <p>QWC 2</p>	<p>An unsupported answer of 18.9(0) implies M0</p> <p>FT 'their 189' provided M1 awarded OR if place value error in digits 1890 and FT 'their 756' Or repeat addition, with 189, 378, 567 shown , or any 3 correct terms in an appropriate summation series with no more than 1 incorrect, or <math>2 \times 378</math> seen</p> <p>As a final answer. If units are given they must be correct Depends on M1 and m1 and must FT for their values including rounding up if necessary</p> <p>Award no marks for an unsupported answer of 4(months)</p> <p>Alternative:</p> <table style="width: 100%; border: none;"> <tr> <td style="text-align: right;"><math>0.15 \times 1260</math></td> <td style="text-align: right;">= (£)189</td> <td style="text-align: right;">M1</td> </tr> <tr> <td style="text-align: right;"><math>584 + 189 + 189</math></td> <td style="text-align: right;"><math>+ 189 + 189 = 1340</math></td> <td style="text-align: right;">A1</td> </tr> <tr> <td></td> <td></td> <td style="text-align: right;">m1 (no extra)</td> </tr> <tr> <td></td> <td></td> <td style="text-align: right;">A1</td> </tr> </table> <p><i>OR reverse calculation working back from 1340</i> 4 (months) A1</p> <p>(For information: 584, 773, 962,1151,1340</p> <p>QWC2 Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.</p> <p>QWC1 Presents relevant material in a coherent and logical manner but with some errors in use of mathematical form, spelling, punctuation or grammar. OR Evident weaknesses in organisation of material but using acceptable mathematical form, with few if any errors in spelling, punctuation and grammar.</p> <p>QWC0 Evident weaknesses in organisation of material, and errors in use of mathematical form, spelling, punctuation and grammar.</p>	$0.15 \times 1260$	= (£)189	M1	$584 + 189 + 189$	$+ 189 + 189 = 1340$	A1			m1 (no extra)			A1
$0.15 \times 1260$	= (£)189	M1												
$584 + 189 + 189$	$+ 189 + 189 = 1340$	A1												
		m1 (no extra)												
		A1												
<p>2. Realising only 1 way to score 14, i.e. '8+6' OR '8 and 6'</p> <p>Number of possible outcomes <math>6 \times 8 (=48)</math></p> <p style="text-align: center;">1/48</p>	<p>B1 B1 B1</p>	<p><u>Do not accept <math>\frac{1}{6} + \frac{1}{8}</math> or <math>1/14</math></u> Accept sight of <math>6 + 8 = 14</math> Accept sight of <math>.. /48</math> or <math>.. /8 \times .. /6</math> Sight of <math>\frac{1}{8} \times \frac{1}{6}</math> is awarded B1, B1 with no other ways CAO <i>An answer of 1:48 gets B2</i></p>												
<p>3(a) <math>3q = m - h^2</math> <math>q = (m - h^2)/3</math> or equivalent</p>	<p>B1 B1</p>	<p>FT from <math>3q = m + h^2</math> or <math>3q = h^2 - m</math> <i>Allow SC1 provided no other marks awarded for missing brackets:</i> <math>q = m - h^2 \div 3</math> OR <math>q = m - h^2/3</math> provided no previous incorrect working</p>												
<p>3(b) <math>3x = 15 \times 2</math> or <math>x/2 = 15/3</math> <math>x = 10</math></p>	<p>M1 A1</p>	<p><math>x = 30/3</math> gets M1 A0</p>												

UNIT 2 Higher Tier	Mark	Final Mark Scheme Comments
4(a) 11	B1	
4(b) Plots All correct plots joined with a curve	P1 C1	Allow one error. FT 'their (a)' or 11 FT 'their (a)' if reasonable or 11. If (a) blank then FT points given, otherwise must include plot at $x=-3$
4(c) From their graph (approximately -2.2 and 1.6)	B1	FT their graph. x-values, coordinates are not required
5(a) $-3n + 15$ or equivalent	B2	B1 for sight of '-3n'
5(b) $2n + 1$ or equivalent	B2	B1 for ' $2n + \dots$ ', OR for sight of 3, 5, 7 showing difference of 2, NOT for ' $n+2$ '
6(a) Any 2 lines drawn correctly  Correct region identified	B2  B1	B1 for any 1 line drawn correctly Allow where ambiguous x or y as 1 or -2 unless incorrect line uniquely selected. Allow any line as correct if selected as a side of the region CAO
6(b) $5x < 40$ or $x < 40/5$ $x < 8$	M1 A1	No marks for use of =, unless replaced to give $x < 8$ , then allow both marks SC1 for $x < 40/11$
7 (a) $4c + 5p = 38.8$ and $2c + 7p = 35.6$ or equivalent  Equating one variable One correct solution Method to find the other variable, e.g. substitution Other correct variable	B1  M1 A1 m1 A1	<u>FT from 1 slip in setting up equations</u> Allow 1 slip but not in the equated variable <i>Any change of unit must be consistent</i> FT their solution provided M1 awarded Solutions $p = 3.6$ (cm) and $c = 5.2$ (cm) <i>No marks for trial and improvement, apart from maybe the first B1.</i> <i>Answer only gets no marks</i>
7 (b) $(80 - 38.8)/c$ (= 41.2/ 'their c') OR attempt ' $c \times \text{value} = 80 - 38.8$ ' OR alternative full method working with 80, 38.8 and c  7 (beads)	M1  A1	<u>Must strictly FT from <math>c=5.2</math> or 'their c'</u> FT number of (whole) $(80-38.8)/$ 'their c' Do not accept use of 'p' (as problem to solve requires thinking to use 'c') FT response must be rounded down to nearest whole Answer must be from correct working (if seen), e.g $7 \times 5.2 = 36.4$ compared with 41.2, or attempt $41.2/c$ Do not accept an answer of 8, however do accept answers (whole numbers) $< 7$ if working is shown and a reason given based on fitting on the necklace
8(a) $2.4 \times 10^{-3}$ $10^3$ 2100 $2.4 \times 10^3$ or equivalent	B2	Mark answer space, unless blank B1 for a run of 3 in the correct order ignoring the incorrect one (i.e. blank out 1 value to find 3 in the appropriate order ignoring the gap made by the incorrect value, placing on the answer spaces thus incorrect) For incorrect value written in answer space for 2400, 1000 or 0.0024 in the answer space penalise -1 only
8(b) $1.5 \times 10^{14}$	B2	B1 for $15 \times 10^{13}$

UNIT 2 Higher Tier	Mark	Final Mark Scheme Comments
9. $(3+3)/2$ or $(20+16)/2$  First point found to be (0,18) Reflection to give (1,10)  Method to find gradient, e.g. sketch with points plotted with horizontal and vertical lines drawn to give an appropriate triangle Gradient = -8 Conclusion $y = -8x + 18$	M1  A1 B1  M1  A1 A1	Or suitable sketch with indication of points and idea to locate mid-way (e.g. showing step triangles), or look at number pattern  Notation not required, e.g. accept without brackets Notation not required, e.g. accept without brackets <u>FT provided at least one of (0, 18), (1, 10) correct</u> Or $(18 - 10)/(0 - 1)$  Gradient given as '8' gets M1 A0  If first M1, A1 award but final M0, A0, A0 then award SC1 for their answer with $y=mx + 18, m \neq 0$ If no marks, then SC2 for their answer with $y=mx + 18, m \neq 0$
10(a) Correct rotation	B2	B1 for anticlockwise rotation about (2,1), OR For clockwise rotation about (1,2)
10(b) Enlarge scale factor $(\pm)1/2$ Correct position	B1 B1	Any placement For their 'enlargement', i.e working with '- ' and using (0,0) as the centre
11. ( $\hat{B}AC = 75^\circ$ )  Reason: Tangent meet radius $90^\circ$ Reason: Angle at the centre is twice angle at circumference	B2  E1 E1	B1 for sight of $\hat{B}OC = 150^\circ$ E marks <b>depend on appropriate B mark awarded and must be stated</b> ( $90^\circ$ indicated on diagram is insufficient) Angle sum of quadrilateral is <b>insufficient</b>  <i>Alternative:</i> <i>Equal tangents (leading to isosceles triangle),</i> <i><math>CBT = BCT = 75^\circ</math> followed by</i> <i>alternate segment theorem and</i> <i><math>\hat{B}AC = 75^\circ</math></i> <i>respectively E1, B1, E1 and B1 with E marks depending on B marks.</i>
12(a) 1	B1	
12(b) $\sqrt{80} = \sqrt{(16 \times 5)}$ or $\sqrt{(4 \times 4 \times 5)}$ or $4\sqrt{5}$ $\{ (\sqrt{80} - \sqrt{5})^2 \} = (4\sqrt{5} - \sqrt{5})^2 = (3\sqrt{5})^2$ $= 45$	M1 M1 A1	CAO <i>Alternative method:</i> <i>M2 for <math>80 - 2\sqrt{80}\sqrt{5} + 5 (=80 - \sqrt{80}\sqrt{5} - \sqrt{80}\sqrt{5} + 5)</math></i> <i>or M1 for <math>80 \dots + 5</math> or <math>80 - \sqrt{80}\sqrt{5} - \sqrt{80}\sqrt{5} \dots</math></i> <i>or <math>\dots - \sqrt{80}\sqrt{5} - \sqrt{80}\sqrt{5} + 5</math></i> <i>A1 45 CAO</i> <i>Method may be shown in stages</i> <i><math>-\sqrt{80}\sqrt{5}</math> may be written <math>-\sqrt{400}</math> or <math>-20</math></i>
12(c) $x = 0.42828\dots$ <b>and</b> $100x = 42.828\dots$ with an attempt to subtract  $424/990 (=212/495)$	M1  A1	Or $10x$ <b>and</b> $1000x$ , or equivalent. Or alternative method An answer of $42.4/99$ gains M1 only. Mark final answer, do not ignore incorrect cancelling
12(d) $3\pi + \pi^2 - 9 - 3\pi$ $= \pi^2 - 9$	M1 A1	Must have 3 of the 4 terms correct CAO. Mark final answer
13(a) $10/25 \times 9/24$ $90/600 (= 9/60 = 0.15)$ ISW	M1 A1	<i>ISW means ignore incorrect final cancelling throughout</i>

UNIT 2 Higher Tier	Mark	Final Mark Scheme Comments
13(b) $1 - P(\text{no pinto beans})$  $1 - 16/25 \times 15/24$  $= 360/600 (=36/60 = 0.6)$ ISW	M1  M1  A1	Or other <b>full</b> method showing intended operations In terms of beans, so may be replacement Overall <b>full</b> method showing intention of operations with correct values substituted <i>ISW means ignore incorrect final cancelling            throughout</i> <i>Alternatives:</i> $2 \times P(pk) = 2 \times 9/25 \times 6/24,$ $2 \times P(pb) = 2 \times 9/25 \times 10/24,$ $P(pp) = 9/25 \times 8/24$ <i>OR</i> $P(\text{pinto, not pinto}) = 2 \times 9/25 \times 16/24,$ with $P(pp) = 9/25 \times 8/24$





UNIT 3 (Calculator allowed) Foundation Tier	Marks	Final Mark Scheme Comments
5.(a) $38 - 16$ $= 22$	M1 A1	
5. (b) 26	B1	
5. (c) Total = 138 $\div 5$ 27.6	M1 m1 A1	Allow up to 2 errors in their readings for the M1 C.A.O.
<b>Use Overlay</b> 6. (a) $\hat{A}BC = 73^\circ$ $\hat{A}CB = 55^\circ$ Completed triangle	B1 B1 B1	Allow $\pm 2^\circ$ Allow $\pm 2^\circ$ Only if at least one B1 awarded. Complete reflection of the triangle gets B2
<b>Use Overlay</b> 6. (b) Arcs for first step Line drawn	B1 B1	
<b>Use Overlay</b> 6. (c) Arcs for $60^\circ$ Bisecting $60^\circ$ arcs step 1 Bisecting $60^\circ$ arcs step 2 and line drawn.	B1 B1 B1	
7. (a) $5/8 - 2/8$ $= 3/8$	M1 A1	Accept decimals, e.g. $(0).625 - (0).25 = (0).375$
(b) $3x = 15$ $x = 5$	B1 B1	F.T. $ax = b, a \neq 1$
(c) $32 = 3 \times 6 + 2W$ $2W = 14$ $W = 7$	B1 B1 B1	Correct substitution Isolating the W F.T. if $ax = b (a \neq 1)$
8. (a) 1.829	B2	B1 for 1.82(8836..) OR 1.83 All places given must be correct rounded or truncated.
8. (b) 30.74	B2	B1 for 30.74(1781...) All places given must be correct rounded or truncated
9. Adults (£) $668 + 668$ Cost per child = $668/2 + 150$ Children $484 \times 3$ Sea view $10 \times 5 \times 14$ Balcony $6 \times 5 \times 14$ Total (£)3908	(1336) B1 B1 (1452) B1 (700) B1 (420) B1 (£)3908 B1	Using the adult and child prices consistently from another row of the table gets MR-1. OR B1 for 50 AND 30 OR B1 for 140 AND 84 F.T. for one error ( i.e. if B4 awarded from first five B1s).
Look for <ul style="list-style-type: none"> <li>spelling</li> <li>clarity of text explanations,</li> <li>the use of notation (watch for the units £)</li> </ul> QWC2: Candidates will be expected to <ul style="list-style-type: none"> <li>present work clearly, with words explaining process or steps</li> </ul> AND <ul style="list-style-type: none"> <li>make few if any mistakes in mathematical form, spelling, punctuation and grammar in their final answer</li> </ul> QWC1: Candidates will be expected to <ul style="list-style-type: none"> <li>present work clearly, with words explaining process or steps</li> </ul> OR <ul style="list-style-type: none"> <li>make few if any mistakes in mathematical form, spelling, punctuation and grammar in their final answer</li> </ul>	QWC 2	QWC2 Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.  QWC1 Presents relevant material in a coherent and logical manner but with some errors in use of mathematical form, spelling, punctuation or grammar. OR Evident weaknesses in organisation of material but using acceptable mathematical form, with few if any errors in spelling, punctuation and grammar.  QWC0 Evident weaknesses in organisation of material, and errors in use of mathematical form, spelling, punctuation and grammar.

UNIT 3 (Calculator allowed) Foundation Tier	Marks	Final Mark Scheme Comments																																																								
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10. (b) 20 (km)	B1	Ignore sight of incorrect units																																																								
10. (c) $2\frac{1}{2}$ (km) / 30(minutes) OR $2\frac{1}{2}$ / 0.5 OR equivalent 5 km/h	M1 A1 U1	Accept statement '2 ½ (km) in half hour' or similar (OR 5000) Independent of other marks (OR ..... m/h) Accept k(m)ph																																																								
<p><b>Indirect marking - Tick marked</b></p> <p>11. 1 hat made in <math>\frac{2}{3}</math> hour or 40 minutes Pay per hat (<math>\frac{2}{3}</math> of £12.60) (£)8.4(0) (Cost of fabric) <math>0.45 \times 3.4(0)</math> (= £)1.53 (Total costs excluding ribbon £) 8.4(0)+ 1.53 (=£9.93) (Ribbon cost per hat) (£)10.25 – (£)9.93 (= £0.32 or 32p) (Ribbon costs) 64(p) (per metre)</p>	B1 B1 M1 A1 m1 m1 A1	<p><i>If units are given they must be correct, penalise once only</i></p> <p>FT 'their 1.53' provided M1 awarded and 'their £8.40' provided ≠£12.60 FT 10.25 – 'their 9.93', provided it includes pay and fabric costs CAO <i>Alternative:</i> (Cost of fabric for 3 hats) <math>3 \times 0.45 \times 3.4(0)</math> M1 = (£)4.59 AI (or M1, A1 for cost of fabric for 1 hat £1.53) (Pay for 3 hats in 2 hours <math>2 \times £12.60 = £)25.2(0)</math> B1 (Sales of 3 hats <math>3 \times 10.25 = £)30.75</math> B1  (Cost of ribbon for 3 hats) (£)30.75 – (£)4.59 – (£)25.2(0) (=96p) m1 FT provided first M1 and includes pay and sales  (Cost ribbon per hat or per metre) <math>\div 3</math> (<math>\times 2</math>) m1 FT provided first M1 and includes pay and sales  (Cost of ribbon per metre) 64(p) or (£)0.64 AI CAO</p>																																																								
<p>12. (a) <math>6x + 7 = 4x + 24</math> <math>2x = 17</math> <math>x = 8.5</math> OR <math>8\frac{1}{2}</math></p> <p>(b) <math>\frac{x}{5} = 9</math> OR <math>x + 20 = 65</math> <math>x = 45</math></p>	B1 B1 B1  B1 B1	<p>Correctly clearing brackets F.T. until second error Collecting terms F.T. <math>ax = b</math> with <math>a \neq 1</math></p> <p>Accept embedded answers such as <math>45/5 = 9</math> for B2, but if they go on to write <math>x=13</math> for example then B1 only.</p>																																																								
<p>13. One correct evaluation, <math>2 \leq x \leq 3</math></p> <p>2 correct evaluations, <math>2.55 \leq x \leq 2.75</math>, one either side of 0</p> <p>2 correct evaluations, <math>2.65 \leq x \leq 2.75</math>, one either side of 0</p> <p>2.7 No calculations shown: accept "too high", "&gt;", etc.</p>	B1  B1  M1  A1	<table border="0"> <tr> <td>x</td> <td><math>x^3 + 2x - 25</math></td> <td></td> <td></td> </tr> <tr> <td>2</td> <td>-13</td> <td></td> <td></td> </tr> <tr> <td>2.1</td> <td>-11.5..</td> <td></td> <td></td> </tr> <tr> <td>2.2</td> <td>-9.95..</td> <td></td> <td></td> </tr> <tr> <td>2.3</td> <td>-8.2..</td> <td></td> <td></td> </tr> <tr> <td>2.4</td> <td>-6.37..</td> <td></td> <td></td> </tr> <tr> <td>2.5</td> <td>-4.37..</td> <td></td> <td></td> </tr> <tr> <td></td> <td></td> <td>2.55</td> <td>-3.318..</td> </tr> <tr> <td>2.6</td> <td>-2.2..</td> <td><b>2.65</b></td> <td><b>-1.09..</b></td> </tr> <tr> <td><b>2.7</b></td> <td><b>0.083</b></td> <td></td> <td></td> </tr> <tr> <td></td> <td></td> <td>2.75</td> <td>1.29..</td> </tr> <tr> <td>2.8</td> <td>2.55..</td> <td></td> <td></td> </tr> <tr> <td>2.9</td> <td>5.18..</td> <td></td> <td></td> </tr> <tr> <td>3</td> <td>8</td> <td></td> <td></td> </tr> </table>	x	$x^3 + 2x - 25$			2	-13			2.1	-11.5..			2.2	-9.95..			2.3	-8.2..			2.4	-6.37..			2.5	-4.37..					2.55	-3.318..	2.6	-2.2..	<b>2.65</b>	<b>-1.09..</b>	<b>2.7</b>	<b>0.083</b>					2.75	1.29..	2.8	2.55..			2.9	5.18..			3	8		
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1(b) 20 (km)	B1	Ignore sight of incorrect units																																																																														
1(c) $2\frac{1}{2}$ (km) / 30(minutes) OR $2\frac{1}{2}$ / 0.5 OR equivalent 5 km/h	M1 A1 U1	Accept statement ‘ $2\frac{1}{2}$ (km) in half hour’ or similar (OR 5000) Independent of other marks (OR ..... m/h) Accept k(m)ph																																																																														
2. $360/6$ OR $4 \times 180/6$ OR $720/6$ $60^\circ$ (exterior ) OR $120^\circ$ (interior )	M1 A1	Need not be associated with interior or exterior angle Accept in working, or $120^\circ$ <b>implied</b> in the drawing, Do not accept if incorrectly labelled on a drawing, e.g $120^\circ$ drawn but incorrectly labelled $60^\circ$ , allow M1, A0. Allow unless contradicted																																																																														
<b>4</b> (of the 5) sides to be drawn forming a polygon drawn all of length 4cm ( $\pm 2$ mm) <b>4</b> (of the 6) angles drawn correctly (within $2^\circ$ tolerance) A correct hexagon, within tolerances allowed	B1 B1 B1	Irrespective of angles  See overlay <i>Penalise drawing polygons with number of sides 5, 7, 8, ... as -1 then FT,</i>																																																																														
3. Strategy: measure angles $120^\circ$ , $240^\circ$ in both pie charts, or appropriate 1:2 ratio, or sight of appropriate $\frac{1}{3}$ to $\frac{2}{3}$ , or appropriate use of ratio for 1 pie chart 50 boys <b>and</b> 100 girls in year 7 90 boys in Year 8  90/2 or 45 girls in Year 8 (Total number of girls) 145	S1  B1 B1  B1 B1	Accept sight of ‘ $120$ and $240$ ’, or ‘ $120^\circ/360^\circ$ is $\frac{1}{3}$ ’ or ‘ $240^\circ/360^\circ$ is $\frac{2}{3}$ ’  May be in different sections of working and implies S1 FT ‘their 50’ + 40 provided S1 awarded and ‘their 50’ $\neq$ 120 FT ‘their 90’/2 provided S1 awarded CAO <i>If incorrect angles used, they must total <math>360^\circ</math>, then mark as follows: S0, FT to possible B1, B1, then B0, B0</i>																																																																														
4. (£) 42.21/7 (£)6.03 and (£)36.18	M1 A1																																																																															
5. One correct evaluation, $2 \leq x \leq 3$  2 correct evaluations, $2.55 \leq x \leq 2.75$ , one either side of 0  2 correct evaluations, $2.65 \leq x \leq 2.75$ , one either side of 0  2.7 <i>No calculations shown: accept “too high”, “&gt;”, etc.</i>	B1  B1  M1  A1	<table style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 10%;"></td> <td style="width: 10%; text-align: center;"><math>x</math></td> <td style="width: 10%; text-align: center;"><math>x^3 + 2x - 25</math></td> <td style="width: 10%;"></td> <td style="width: 10%;"></td> <td style="width: 10%;"></td> </tr> <tr> <td></td> <td style="text-align: center;">2</td> <td style="text-align: center;">-13</td> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td style="text-align: center;">2.1</td> <td style="text-align: center;">-11.5..</td> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td style="text-align: center;">2.2</td> <td style="text-align: center;">-9.95..</td> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td style="text-align: center;">2.3</td> <td style="text-align: center;">-8.2..</td> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td style="text-align: center;">2.4</td> <td style="text-align: center;">-6.37..</td> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td style="text-align: center;">2.5</td> <td style="text-align: center;">-4.37..</td> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td></td> <td></td> <td style="text-align: center;">2.55</td> <td style="text-align: center;">-3.318..</td> <td></td> </tr> <tr> <td></td> <td style="text-align: center;">2.6</td> <td style="text-align: center;">-2.2..</td> <td style="text-align: center;"><b>2.65</b></td> <td style="text-align: center;"><b>-1.09..</b></td> <td></td> </tr> <tr> <td></td> <td style="text-align: center;"><b>2.7</b></td> <td style="text-align: center;"><b>0.083</b></td> <td style="text-align: center;">2.75</td> <td style="text-align: center;">1.29..</td> <td></td> </tr> <tr> <td></td> <td style="text-align: center;">2.8</td> <td style="text-align: center;">2.55..</td> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td style="text-align: center;">2.9</td> <td style="text-align: center;">5.18..</td> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td style="text-align: center;">3</td> <td style="text-align: center;">8</td> <td></td> <td></td> <td></td> </tr> </table>		$x$	$x^3 + 2x - 25$					2	-13					2.1	-11.5..					2.2	-9.95..					2.3	-8.2..					2.4	-6.37..					2.5	-4.37..							2.55	-3.318..			2.6	-2.2..	<b>2.65</b>	<b>-1.09..</b>			<b>2.7</b>	<b>0.083</b>	2.75	1.29..			2.8	2.55..					2.9	5.18..					3	8			
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Unit 3 Higher Tier	Mark	Final Mark Scheme Comments
<p>6.</p> <p>1 hat made in 2/3 hour or 40 minutes Pay per hat (2/3 of £12.60) (£)8.4(0) (Cost of fabric) <math>0.45 \times 3.4(0)</math> <math>(= \text{£})1.53</math> (Total costs excluding ribbon £) <math>8.4(0) + 1.53 (= \text{£}9.93)</math> (Ribbon cost per hat) (£)10.25 – (£)9.93 (= £0.32 or 32p) (Ribbon costs) 64(p) (per metre)</p> <p>QWC2 requires sight of the majority of the process steps shown, labelled, with units and money expressed correctly, with a clear final answer</p> <p>QWC1 requires at least 2 of the process steps, which are labelled and units correct in a labelled final answer OR QWC1 majority of process steps shown with units correct in a labelled final answer</p> <p>Look for</p> <ul style="list-style-type: none"> <li>• spelling</li> <li>• clarity of text explanations,</li> <li>• the use of notation (watch for the units and ‘0’ for unit pence when using £)</li> </ul> <p>QWC2: Candidates will be expected to</p> <ul style="list-style-type: none"> <li>• present work clearly, with words explaining process or steps AND</li> <li>• make few if any mistakes in mathematical form, spelling, punctuation and grammar in their final answer</li> </ul> <p>QWC1: Candidates will be expected to</p> <ul style="list-style-type: none"> <li>• present work clearly, with words explaining process or steps OR</li> <li>• make few if any mistakes in mathematical form, spelling, punctuation and grammar in their final answer</li> </ul>	<p>B1 B1 M1 A1 m1 m1 A1 QWC 2</p>	<p><i>If units are given they must be correct, penalise once only</i></p> <p>FT ‘their 1.53’ provided M1 awarded and ‘their £8.40’ provided ≠£12.60 FT 10.25 – ‘their 9.93’, provided it includes pay and fabric costs CAO</p> <p><i>Alternative:</i> (Cost of fabric for 3 hats) <math>3 \times 0.45 \times 3.4(0)</math> M1 <math>= (\text{£})4.59</math> A1 (or M1, A1 for cost of fabric for 1 hat £1.53) (Pay for 3 hats in 2 hours <math>2 \times \text{£}12.60 = \text{£})25.2(0)</math> B1 (Sales of 3 hats <math>3 \times 10.25 = \text{£})30.75</math> B1 (Cost of ribbon for 3 hats) <math>(\text{£})30.75 - (\text{£})4.59 - (\text{£})25.2(0) (=96p)</math> m1 FT provided first M1 and includes pay and sales (Cost ribbon per hat or per metre) <math>\div 3 (\times 2)</math> m1 FT provided first M1 and includes pay and sales (Cost of ribbon per metre) <math>64(p)</math> or <math>(\text{£})0.64</math> A1 CAO</p> <p>QWC2 Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.</p> <p>QWC1 Presents relevant material in a coherent and logical manner but with some errors in use of mathematical form, spelling, punctuation or grammar. OR Evident weaknesses in organisation of material but using acceptable mathematical form, with few if any errors in spelling, punctuation and grammar.</p> <p>QWC0 Evident weaknesses in organisation of material, and errors in use of mathematical form, spelling, punctuation and grammar.</p>
7(a) $6x^2(x - 2)$	B2	B1 for correct partial factorisation, OR B1 for correct highest common factor and 1 term in brackets correct
7(b) $(x - 7)(x + 6)$	B2	Mark final answer. B1 for $(x \dots 7)(x \dots 6)$
7(c) $(3x + 2)(5x + 7)$	B2	Mark final answer. B1 for $(3x + 7)(5x + 2)$ or $(3x \dots 2)(5x \dots 7)$ or $5x(3x + 2) + 7(3x + 2)$ or equivalent
8(a) $2x + 5 = 5x + 5$ $x = 0$	M1 A1	Or $3x = 0$ Accept $0 = x$ . Do not accept $x = 0$ from incorrect working, if M0 seen, then A0
8(b) $2x + 3 + 3 \times 4x = 8 \times 3$ or $2x/3 + 1 + 4x = 8$ $14x = 21$ or $14x/3 = 7$ $x = 3/2$ or 1.5 or equivalent	B1 B1 B1	Sight of $\frac{3}{2}$ written as 0.6 is an error. FT until 2 <sup>nd</sup> error Mark final answer
9(a) $w^2 + 12.7^2 = 56.2^2$ or $(w^2 =) 56.2^2 - 12.7^2$ $w^2 = 2997.15$ or $(w =) \sqrt{2997.15}$ $54.7(46\dots \text{cm})$ or 55 (cm)	M1 A1 A1	

Unit 3 Higher Tier	Mark	Final Mark Scheme Comments																						
9(b) $\sin m = 14.2/34.6$ $m = 24(.23\dots^\circ)$	M1 A2	A1 for $m = \sin^{-1}0.4(104\dots)$																						
10. $(x =) (46.2/8.4) \times 10$ (OR $5.5 \times 10$ ) (=) 55(cm) $(y =) 18.7 \div (46.2/8.4)$ (OR $18.7/5.5$ ) (=) 3.4(cm)	M1 A1 M1 A1	Or alternative full method to find x, x not implicit Or alternative full method to find y, y not implicit Alternatively candidates may refer to scale factor 5.5 throughout																						
11. In either order: D with F, in any order Reason: 3 sides or SSS C with E, in any order Reason: 2 sides and <u>included</u> angle or SAS	B1 E1 B1 E1	E marks depend on B marks																						
12(a) Intention to subtract horizontal values on x-axis for vertical axis reading across at 45 and 15 (= 30 – 13 to 14) IQR answers in the range 16 to 17  12(b) Indicates the first task due to smaller IQR	M1 A1  E1	FT for ‘their IQR’ comparison with conclusion																						
13(a)(i) -2.5 <b>and</b> 5	B1																							
13(a)(ii) Sight of $y=5$ , in working or on graph -2.2 to -2.1 AND 4.6 to 4.7	M1 A1																							
13(b) Strategy, set up a table or list to calculate values for $y=x^2 - 2x - 3$ with at least 1 point correct, or equate $-2x^2 + 5x + 25 = x^2 - 2x - 3$ At least 3 values in their table or list correct <b>and</b> plotted, OR $3x^2 - 7x - 28 = 0$ with substitution into quadratic formula (allow 1 slip)  All necessary correct points plotted joined with <b>correct curve drawn</b> to intersections, OR $x = \{7 \pm \sqrt{385}\} / 6$  Intersection approximately at $x = 4.4$ and $x = -2.1$ $x = 4.4, y = 7.8$ and $x = -2.1, y = 5.6$	S1  M1  A1  A1 A1	<table border="1"> <tr> <td>x</td> <td>-3</td> <td>-2</td> <td>-1</td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> </tr> <tr> <td>y</td> <td>12</td> <td>5</td> <td>0</td> <td>-3</td> <td>-4</td> <td>-3</td> <td>0</td> <td>5</td> <td>12</td> <td>21</td> </tr> </table> CAO. Not a FT from incorrect points, then FT for possible A marks  FT from points plotted but not joined FT provided M1 FT their graph, or their x calculation to evaluate y correctly	x	-3	-2	-1	0	1	2	3	4	5	6	y	12	5	0	-3	-4	-3	0	5	12	21
x	-3	-2	-1	0	1	2	3	4	5	6														
y	12	5	0	-3	-4	-3	0	5	12	21														
14(a) Mid points 14.5, 24.5, 34.5, 44.5 $2 \times 14.5 + 18 \times 24.5 + 29 \times 34.5 + 1 \times 44.5 (=1515)$ $\sum fx / 50$  (£) 30.3(0)	B1 M1 m1 A1	FT for their mid points from within group FT for correct sum of their $fx$ terms /50 FT their $\sum fx / 50$ correctly evaluated Accept (£)30 provided correct working seen																						
14(b) Strategy, e.g. noticing 0 to 20 same area as 20 to 30, or noticing first 2 rectangles are of equal area  $20 \times \text{frequency density} = 8$ , or equivalent, or 16 people split 8 people and 8 people for first 2 rectangles  Uniform scale, implied or shown (height of first rectangle is 0.4, 2 <sup>nd</sup> height is 0.8, etc.)  $8 \times 10 + 8 \times 25 + 11 \times 32.5(0) + 12 \times 37.5(0) + 9 \times 42.5(0) + 1 \times 47.5(0)$ OR $20 \times 0.4 \times 10 + 10 \times 0.8 \times 25 + 5 \times 2.2 \times 32.50 + 5 \times 2.4 \times 37.50 + 5 \times 1.8 \times 42.50 + 5 \times 0.2 \times 47.50$  (£)1517.5(0)	S1  B1  B1  M2  A1	Or £20 with 8 people, or 32 squares for £30, or 32 squares for 16 people, or 16 squares for 8 people  Or sight of 0.4 Award of this B1 implies S1 also  Or sight of 0.4 and 0.8 appropriately, or ‘each person 2 squares’, or sight of 8, 8,11,12, 9,1 or sight of any 4 of 10, 25, 32.5(0), 37.5(0), 42.5(0), 47.5(0) Award of this B1 implies S1 and previous B1 also <i>If M1 or M2 are awarded,</i> <i>this implies previous S1, B1 and B1</i> <u>Do not FT from incorrect frequency density scale</u> M1 for <ul style="list-style-type: none"> <li>any 3 correct products within the overall sum</li> <li>the appropriate sum of products but with bounds used instead of mid points, or</li> <li>use of mid points 10, 25, 32.5(0), 37.5(0), 42.5(0) and 47.5(0) within a product sum</li> </ul> CAO. Mark final answer																						

Unit 3 Higher Tier	Mark	Final Mark Scheme Comments								
15(a) $g \propto t^2$ or $g = kt^2$ $450 = k \times 7.5^2$ $g = 8t^2$ 15(b) <table border="1" data-bbox="188 309 687 365"> <tr> <td>g</td> <td>50</td> <td>450</td> <td>800</td> </tr> <tr> <td>t</td> <td>2.5</td> <td>7.5</td> <td>(+) 10</td> </tr> </table>	g	50	450	800	t	2.5	7.5	(+) 10	B1 M1 A1  B2	Ignore incorrect use of '=' or ' $\alpha$ ' throughout FT from non linear only May be implied in (b)  B1 for each value. FT non linear expressions for SC1 only if both FT answers accurately evaluated
g	50	450	800							
t	2.5	7.5	(+) 10							
16. Use of sine rule followed by cosine rule $AC/\sin 49 = 142/\sin 62$ $AC = \sin 49 \times 142/\sin 62$ $AC = 121$ or $121.3(76\dots)$ or $121.4$ (metres) $AD^2 = AC^2 + 224^2 - 2 \times AC \times 224 \times \cos 74$ $AD^2 = 49875.25$ to $49922.816\dots$ $AD = 223(.3\dots)$ metres	S1 M1 A1 A1 M1 A1 A1	FT their AC provided $\neq 142$ or $\neq 224$ or spurious  Depends on previous M1 and A1								
17. $70^\circ$ and $290^\circ$ with no other values	B2	B1 for either value								



WJEC  
245 Western Avenue  
Cardiff CF5 2YX  
Tel No 029 2026 5000  
Fax 029 2057 5994  
E-mail: [exams@wjec.co.uk](mailto:exams@wjec.co.uk)  
website: [www.wjec.co.uk](http://www.wjec.co.uk)