

# **GCSE MARKING SCHEME**

## **MATHEMATICS - UNITISED**

**JANUARY 2012** 

#### INTRODUCTION

The marking schemes which follow were those used by WJEC for the January 2012 examination in GCSE MATHEMATICS – UNITISED. They were finalised after detailed discussion at examiners' conferences by all the examiners involved in the assessment. The conferences were held shortly after the papers were taken so that reference could be made to the full range of candidates' responses, with photocopied scripts forming the basis of discussion. The aim of the conferences was to ensure that the marking schemes were interpreted and applied in the same way by all examiners.

It is hoped that this information will be of assistance to centres but it is recognised at the same time that, without the benefit of participation in the examiners' conferences, teachers may have different views on certain matters of detail or interpretation.

WJEC regrets that it cannot enter into any discussion or correspondence about these marking schemes.

	Page
Unit 1 – Foundation Tier	1
Unit 1 – Higher Tier	4
Unit 2 – Foundation Tier	7
Unit 2 – Higher Tier	12

#### **Unit 1 – Foundation Tier**

UNIT 1 Foundation Tier	✓	Mark	Comments
1. (a) $(\pounds76.99)$ $(\pounds)31.75$ $(\pounds)36(.00)$ (Total) $(\pounds)144.74$ (b) 14 (points)		B1 B1 B1 B1	Accept 3175p. Accept 3600p F.T. their amounts. F.T. their total bill.
$2(a)$ $35^{(\circ)}$		B1	Allow $\pm 2^{\circ}$ .
2(b) Sight of $8 \cdot 3(\text{cm})$ $8 \cdot 3 \times 20$ = 166m		B1 M1 A1	Allow $\pm 2$ mm. F.T. their '8·3'. For stated intent to multiply a length by 20. <u>Must show correct units.</u> Unsupported answer in the region 162 to 170 implies B1, M1. Also A1 if units given.
2(c) <b>Use overlay.</b> A line from end of path B to mid point of path AC.		B1	Allow ±2mm for mid point. <b>Use overlay.</b> Do not penalise poorly drawn lines.
3. (70 to 89) (90 to 109) <b>110 to 129</b> (130 to 149)         Using a tally convention.         (4)       9       7       2		B1 B1 B2	Accept any unambiguous indication e.g. 110 – 129. Need not be accurate. Must show a total of at least 13 additional tallies. B2 for all three correct. B1 for 1 or 2 correct.
4(a) (i) Jan(uary).		B1	
4(a) (ii) May.		B1	
4(b) (Hire Cost =) $50 \times 5 + 85$ = 335 ISW		M1 A1	For correct substitution BUT M0 if e.g. 50×90 used or implied.
4(c) Correct strategy (£)30		M1 A1	E.g. Using '10 × 6TND' or '6 × 10TND' etc.

UNIT 1 Foundation Tier	~	Mark	Comments
5. (Perimeter or fence =) $20(m)$ (Cost of fence =) (£)140	✓ ✓	B1 B1	F.T. $7 \times$ their 'perimeter'.
(Area or concrete =) $6 \times 4$ = 24(m <sup>2</sup> ) (Cost of concrete = ) (£)216	✓ ✓ ✓	M1 A1 A1	F.T. $9 \times$ their 'area'.
(Total cost =) $(\pounds)356$	$\checkmark$	B1	F.T their stated costs for the fence and the concrete.
<ul> <li>Look for <ul> <li>spelling</li> <li>clarity of text explanations,</li> <li>the use of notation (watch for the use of '=', '£', m and m<sup>2</sup> being appropriate)</li> </ul> </li> <li>QWC2: Candidates will be expected to <ul> <li>present work clearly, with words explaining process or steps</li> </ul> </li> <li>AND <ul> <li>make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer</li> </ul> </li> <li>QWC1: Candidates will be expected to <ul> <li>present work clearly, with words explaining process or steps</li> </ul> </li> <li>OR <ul> <li>make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer</li> </ul> </li> </ul>	* *	QWC 2	<ul> <li>QWC2. Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.</li> <li>QWC1. Presents relevant material in a coherent and logical manner, but with some errors in use of mathematical form, spelling, punctuation or grammar.</li> <li>OR</li> <li>Evident weakness in organisation of material but using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.</li> <li>QWC0. Evident weakness in organisation of material and errors in use of mathematical form, spelling, punctuation and grammar.</li> </ul>
6.(a) (i) A correct equation formed. (ii) A correct equation formed. (iii) A correct equation formed.		B1 B1 B1	Must use given numbers once only in each case.
6(b) – ÷		B1	
7(a) (i) 'More girls than boys' or equivalent.		B1	Accept 'Twice as many girls as boys'. Do not accept 'more females passed'.
7(a) (ii) 25(%)		B1	<sup>1</sup> / <sub>4</sub> is B0.
7(b) Indication that the range of the marks in History is 6 and in Geography is 9		B2	Allow 'range in Geography is greater' or equivalent. B1 for ranges of 6 and 9 only, with no indication of which is which. OR B1 for 'History 2 to 8 and Geography 1 to 10' OR B1 for one correct range clearly attributed.
7(c) It might appear that the % increase is much greater for one period than the other because of the different scale used.		B2	B1 for comment on misleading visual appearance. B1 for comment on different scale used. Credit similar statements once only. (Mark comments wherever they appear. Ignore other irrelevant comments.)
8. $0.15 \times (\pounds)1240 + 36 \times (\pounds)42$ = $(\pounds)186$ (+) $(\pounds)1512$ = $(\pounds)1698$ ISW	$\checkmark$	M1 B1 B1 A1	For complete method. For sight of 186 or implied in further calculation. For sight of 1512 or implied in further calculation. F.T. addition of their amounts. Correct answer gains all 4 marks.

UNIT 1 Foundation Tier	~	Mark	Comments
9. 91.36 – ( total cost of three other items)	~	M1	M1 for attempt so do not penalise incorrect total cost OR use of 48 instead of $0.48$
= (£)84.54 or 8454p	~	A1	C.A.O.
(Diesel bought =) $(\pounds)$ 84.54 ÷ 1.409 = 60(litres) ISW	✓ ✓	M1 A1	<ul> <li>F.T. 'their £84.54' (this may be £91.36)</li> <li>Accept answers from a F.T. being rounded or truncated .</li> <li>SC1 for attempting to divide by 140.9.</li> <li>M1A0 for dividing by 1.41 or 1.4(0).</li> <li>M0A0 for dividing by 1.49</li> </ul>
10. Repeated attempt to find 1/3 <u>and subtract</u> or 2/3 of two different amounts. (End of 2 <sup>nd</sup> year) 150(kg)		M1 B1	M1 awarded for intent. Penalise use of decimal approximations to 1/3 or 2/3 once only.
(End of $3^{rd}$ year) 100(kg)		A1	Penalise extra work $-1$ (unsupported 66.6 implies this).
11(a) Q1. A statement regarding e.g. 'not relevant', 'confidentiality', 'too personal'		B1	Only mark answer given in relevant answer space Ignore other statements if B1 awarded. For any equivalent statement.
Q2. 'times not exclusive' 'over what period of time?'		B1	For any <b>one</b> of these, or equivalent statement.
11(b) A criticism regarding location or time.		B1	
12. $55 \times 1.6$ or equivalent. = 88 (km.p.h.) 8 (km.p.h.) (above)		M1 A1 A1	Alternate method. $80 \times 0.625$ M1 $= 50(m.p.h.)$ A1F.T. 'their 88'. $5(m.p.h.)(above)$ A1('above' not required, but 'under' is A0.)A1An unsupported final answer requires units.Unsupported 5(m.p.h.) under is M0A0A0
13. Use overlay Position of ship 065° from Sunderland. Position of ship 6cm from Sunderland. Correct three-figure bearing given		B1 B1 B1	Allow $\pm 2^{\circ}$ . Allow $\pm 2$ mm. ( <i>Ship must be at sea for this B1</i> ) F.T. their ship's position. Allow $\pm 2^{\circ}$ . <b>Use tools.</b>
14. Use of Volume = $\pi \times 12^2 \times \text{height.}$ Height = Volume / $\pi \times 12^2$ (Height of water = ) 19.88 to 19.91 inclusive. 20(cm)		M1 m1 A1 A1	Allow 900, 90 or 9 as intent to use volume. C.A.O. F.T. 'their height' if of equivalent difficulty and gives an answer that is > 0.
15. $4000$ 120 120		B1	For the evaluation of a correct $3\%$ OR Sight of $1.03$ (360 and 4360 imply use of $3\times 120$ and gain B1)
$ \begin{array}{c} 4120 \\ \underline{123.6(0)} \\ 4243.6(0) \\ \underline{127.30(8)} \\ 4370.90(8) \end{array} $		M1	For attempting to find 3 different 3%. OR $4000 \times 1.03^3$ .
(£) 4370.91 ISW		Al	F.T. one error if of equivalent difficulty. Treat 2 years as a misread.

### Unit 1 – Higher Tier

UNIT 1 Higher Tier	✓	Mark	Comments
1. Repeated attempt to find 1/3 <u>and subtract</u> , or 2/3 of two different amounts. OR Repeated attempt to find 20% <u>and subtract</u> , or 80% of two different amounts.		M1	Treat going on for an extra year as a misread. Treat consistent increase as a misread. M1 awarded for intent.
(Tree A =) 100(kg) (Tree B =) 128(kg) Tree B by 28(kg)		A1 A1 A1	C.A.O. C.A.O. F.T. their amounts. SC1 for Tree B by 45(kg) [(200–40–40) –(225–75–75)]
2(a) (i) Intent to multiply values by frequencies and add up $(0 \times 11 + 1 \times 25 + 2 \times 4 + 3 \times 2 + 30 \times 2)$ their $\sum fx \div 44$ $= 2 \cdot 25$		M1 m1 A1	CAO (but ignore if $2 \cdot 25$ seen and then rounded to 2)
<ul><li>2(a)</li><li>(ii) Some indication that this is not typical for the majority of the workforce.</li></ul>		B1	E.g. 'Most are absent fewer than 2 days', '30 days skew things'.
<ul> <li>2(b) Some reference to most being in the first group or that most of the group intervals would be empty. OR</li> <li>Some reference to loss of raw data or that the answer will be an estimate</li> </ul>		B1	Do not accept that '4 is not a factor of 30' for a B1.
3. <b>Use overlay</b> Position of ship 065° from Sunderland. Position of ship 6cm from Sunderland. Correct three-figure bearing given		B1 B1 B1	Allow $\pm 2^{\circ}$ . Allow $\pm 2$ mm. ( <i>Ship must be at sea for this B1</i> ) F.T. their ship's position. Allow $\pm 2^{\circ}$ . <b>Use tools.</b>
4. $55 \times 1.6$ or equivalent. = 88 (km.p.h.) 8 (km.p.h.) (above)		M1 A1 A1	Alternate method. $80 \times 0.625$ M1 $= 50(m.p.h.)$ A1F.T. 'their 88'. $5(m.p.h.)$ (above)A1('above' not required, but 'under' is A0.)A1An unsupported final answer requires units.Unsupported 5(m.p.h.) under is M0A0A0
5(a) (i) 5(%)		B1	
5(a) (ii) No because the graph show (%) growth not actual numbers.		B1	Accept equivalent valid statements.
5(b) E.g. 'No scale (so might not be 'huge'). 'Only two plots (so might not be 'steady'). 'Not clear how 'burglaries' are defined'.		B2	B1 for each valid reason. Credit similar reasons once only.
6 Sight of 8 hours difference in time. Sight of take off time as 18:10 (London) Correct addition of 11hrs 20 min. (Time in Los Angeles) 21:30 Tuesday		B1 B1 B1 B1	May be given as 10:10 (Los Angeles) F.T. their 'initial' time. (Accept e.g. 05:30 but not 29:30) Must give both time and day. These marks may be implied in their answer(s). E.g. (2h30min + 11h20min) '+' 07:40 =) 21:30 gains B3. 'Tuesday 21:30' on its own gains B4

UNIT 1 Higher Tier	✓	Mark	Comments
7. (Taxable Income = ) $(\pounds)44,850$	$\checkmark$	B1	For sight of 44850.
(Tax on first £35000 =) (£)7000	~	B1	For sight of 7000.
(Additional Tax =) $0.4 \times (\pounds)9850$ = $(\pounds)3940$	√ √	M1 A1	F.T. $0.4 \times$ ('their 44850' - 35000).
(Total Tax =) (£)10,940	~	A1	F.T. 'their 7000' + 'their 3940'.
<ul> <li>Look for</li> <li>spelling</li> <li>clarity of text explanations,</li> <li>the use of notation (watch for the use of '=', £, % being appropriate)</li> </ul>	√ √	QWC 2	QWC2. Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.
<ul> <li>QWC2: Candidates will be expected to <ul> <li>present work clearly, with words explaining process or steps</li> </ul> </li> <li>AND <ul> <li>make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer</li> </ul> </li> <li>QWC1: Candidates will be expected to <ul> <li>present work clearly, with words explaining process or steps</li> </ul> </li> <li>OR <ul> <li>make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer</li> </ul> </li> </ul>			<ul> <li>QWC1. Presents relevant material in a coherent and logical manner, but with some errors in use of mathematical form, spelling, punctuation or grammar. OR</li> <li>Evident weakness in organisation of material but using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.</li> <li>QWC0. Evident weakness in organisation of material and errors in use of mathematical form, spelling, punctuation and grammar.</li> </ul>
		7	
AND of 1yd (being represented by) 9cm		BI	Allow $^{1}\text{Im} = 10\text{cm}^{2}$ or $^{1}\text{Iyd} = 9\text{cm}^{2}$ etc. Allow $\pm 0.1\text{cm}$ in measurement of 10cm and 9cm.
1/10  metre = 1/9  yard   or equivalent e.g. '1yd = 0.9m' (1 metre = ) $1.1(\text{yards})$		M1 A1	F.T. their line measurements.
9. $60\% \equiv (\pounds)192$		B1 M1	Accept any indication.
$\frac{192}{60} \times 100$		IVIII	$\mathbf{O}_{\mathbf{r}} = \mathbf{Q}_{\mathbf{r}} \mathbf{V}_{\mathbf{r}} \mathbf{U}_{\mathbf{r}} $
=(f)320		A1	
<ul> <li>10. Correct substitution into formula. Making 'Annual Bonus' subject of formula. Using consistent units of '£' or 'pence'. (Annual Bonus = ) (£)30.26 or 3026 (p)</li> </ul>		M1 m1 M1 A1	Do not penalise 'mixing' units at this stage. Allow missing brackets but not incorrect use of $+$ and $-$ . Allow also (£)30.24 or 3024(p) and (£)30.25 or 3025(p) Allow also (£)30.27 or 3027(p) and (£)30.28 or 3028(p)
11. Strategy to find (Fractional or % or actual) return for either currency.		M1	E.g. $\frac{11.6}{12.2}$ (×100) or $\frac{127.2}{135.9}$ (×100) OR using £x £x × $\frac{11.6}{12.2}$ or £x × $\frac{127.2}{135.9}$
(HK\$) $0.95(08)$ or $95(.08\%)$ (Return) (Yen) $0.93(60)$ or $93(.60\%)$ (Return)		A1 A1	If $x = \pounds 100$ return = £95(.08) If $x = \pounds 100$ return = £93(.60)
More is lost on the Yen		A1	F.T. their calculated amounts.

UNIT 1 Higher Tier	~	Mark	Comments
12. $4 \times \frac{2}{6}$	$\checkmark$	M1	Or equivalent e.g. $\times 1/3$ or $\div 3$ .
$\times \frac{15}{3}$	✓	M1	Or equivalent e.g. $\times$ 5 or $\div$ 0.2.
= 20/3 (hrs) = 6hrs 40min	✓ ✓	A1 A1	C.A.O. or equivalent e.g. $6.66$ (hrs). Alternate presentation. <u>Tanks</u> <u>Pumps</u> <u>Hours</u> <u>6</u> 15 4 M1 for 'two' steps. M1 for next 'two' steps. <u>2</u> 3 <b>20/3</b> A1 C.A.O. (Watch out for compensating errors) F.T. conversion from 'their 20/3' only if an M1 gained and is of equivalent difficulty.
13. Sight of 67.5(m) AND 68.5(m)	✓	B1	Allow B1 for sight of 6750 AND 6850.
Sight of 35.5(cm) AND 36.5(cm)	~	B1	Allow B1 for sight of $0.355$ AND $0.365$ .
(Least number required) $\frac{6750}{36\cdot 5}$ or equivalent 185 (Greatest number required) $\frac{6850}{35\cdot 5}$ or equivalent 193	✓ ✓ ✓	M1 A1 M1 A1	<ul> <li>F.T. 'their least corridor' / 'their biggest tile'. (with consistent units used)</li> <li>Must be a whole number of tiles. Unsupported 184 gains M1A0</li> <li>F.T. 'their biggest corridor' / 'their smallest tile'. (with consistent units used)</li> <li>Must be a whole number of tiles BUT do not penalise again if already penalised once before. Unsupported 192 gains M1A0</li> <li>If no M marks gained, allow SC1 <u>once</u> for a 'correct' method but using 'mixed' units, e.g. 67.5/36.5.</li> </ul>
Both parts, (a) and (b) marked together 14 (a) <u>Angle AOB</u> $\times 2 \times \pi \times 18 = 66$		M1	For correct substitution.
$A\hat{O}B = \underline{66 \times 360}$ or equivalent		A1	
$2 \times \pi \times 18$ $210^{(\circ)}$		A1	For an answer that rounds or truncates to 210.
(b) (Area =) $\frac{150}{360} \times \pi \times 18^2$		M1	F.T. 'their 210'.
$= 424(\cdot 11)(cm^2)$		A1	Accept values that are correct to 3 sig.fig. SC1 for 593(.76) or 594.
15. Sight of $\pi \times r^2 \times 5$ AND $\frac{1}{3} \times \pi \times r^2 \times 18$ $\pi \times r^2 \times 5 + \frac{1}{3} \times \pi \times r^2 \times 18$ $(11\pi r^2) = 1244$	$\checkmark$	B1 M1 m1	Allow only if equivalent to kr <sup>2</sup> .
$r = \sqrt{(1244 / 11\pi)}$	~	A1	Incorrect manipulation of equation is A0,A0,A0.
r = 6(cm) (Diameter =) 12(cm)	✓ ✓	A1 A1	F.T. their radius.

#### Unit 2 – Foundation Tier

UNIT 2 (Non-calculator) Foundation Tier	Marks	Comments
1 (a) (i) 6043	1	
1 (a) (ii) thirty two thousand (and) five	1	
1. (b) (i) 36 and 54	1	
1. (b) (ii) 45	1	Allow 45 + 36 (=81)
1. (b) (iii) 42	1	
1. (c) (i) 45700	1	
1. (c) (ii) 46000	1	
1. (d) (i) 24	1	
1. (d) (ii) 27	1	
1. (d) (iii) 23 OR 29	1	For either or both with no incorrect answers
2. g(rams) m(etres) km l(itres) OR cm <sup>3</sup> OR ml OR cc 3. (a) Trapezium Rectangle Rhombus Square	1 1 1 1 B4	Allow incorrect spelling as long as comprehensible Note: the contents of a bracket are not required If more than one answer given, they all have to be correct. e.g. miles, kilometres gets 0 e.g. allow g OR gram OR grams allow m OR metres allow kilometre but not kilo B1 for each B0 for any shape that is in at least 2 places
3. (b) (i) Correct line with no incorrect lines	1	
3. (b) (ii) 2 correct lines with no incorrect lines	1	

UNIT 2 (Non-calculator) Foundation Tier	Marks	Comments
4. (a) 40	1	
4. (b) (i) Add eleven (to the previous term)	B1	Accept +11 Accept any equivalent statement.
4. (b) (ii) Divide (the previous term) by two	B1	Accept ÷2 Accept any equivalent statement.
4. (c) (i) 7 OR -7	1	Allow 7.0 etc. Do not accept $7 \times 7$ OR 72.
4. (c) (ii) 0.09	1	Allow .09
$\begin{array}{r} 4. \ (d) \ 80/100 \ \times \ 60 \\ = \ 48 \end{array}$	M1 A1	Any correct method for finding 80% SC1 for 48%
5. (a) (i) (£) $\frac{1}{2}b$ OR equivalent	1	Ignore units, no £ sign required. Do not accept words, e.g. half of b, 50% of b B0 for $1/2b$ OR $b - b/2$
5. (a) (ii) $x + 4$ (cm) OR $4 + x$	1	Ignore units, no cm required. Ignore x=, for example, B1 for $x = x+4$ , $x+4=x$ B1 for $x+4=4x$ , but B0 for $4x=x +4$
5. (b) 8	B2	B1 for 52/4 or 13 OR B1 for 'their 13' – 5 Accept embedded answers like 8+5=13×4=52
5. (c) $5(n+6)$	B2	Ignore x= etc B1 for 5. n+6 (No bracket). B0 for 5n + 6 B1 for $n + 6 \times 5$ but B0 for $n + 30$ But n+6 = 6n $\times 5$ gets B0. Also n+6(5) gets B0 Penalise -1 for inappropriate algebra if B2
Overlay (viewed with diagram) 6. All 3 quadrants correct	B3	B1 for each correct quadrant.

UNIT 2 (Non-calculator) Foundation Tier	Marks	Comments
<ul> <li>7. Indirect (✓) marking</li> <li>For trying to find the costs of a common number of bricks</li> <li>For example: Davies 40 bricks cost (£) 6 × 4</li> <li>= (£) 24</li> <li>Jones 40 bricks cost (£) (£) 20</li> <li>Profit on a common number of bricks</li> <li>How many bricks for a profit of (£)20</li> </ul>	S1 M1 A1 A1 B1 B1	Method of finding the cost of common number of bricks from either Davies or Jones for first correct cost, for the other. Finding the profit F.T. their common number of bricks costs.
<ul> <li>OR</li> <li>Davies' bricks cost 600/10</li> <li>= 60p each</li> <li>Jones' bricks cost 50p each</li> <li>Davies gains 10p per brick</li> <li>They sold 200 bricks</li> <li>Look for <ul> <li>Spelling</li> <li>Clarity of text explanations</li> <li>The use of notation – watch for '=','£', 'p' being used appropriately.</li> </ul> </li> <li>QWC2: Candidates will be expected to <ul> <li>present work clearly, with words explaining their processes or steps</li> </ul> </li> <li>AND <ul> <li>make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer</li> <li>OWC1: Candidates will be expected to</li> </ul> </li> </ul>	SI MI A1 A1 B1 B1 QWC 2	<ul> <li>For trying to find the cost of 1 brick</li> <li>Method of doing it for Davies or Jones for first correct cost, for the other.</li> <li>Finding the profit</li> <li>F.T. their common number of bricks costs.</li> </ul> QWC2 Presents material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar. QWC1 Presents material in a coherent and logical manner but with some errors in use of mathematical form, spelling, punctuation or grammar OR evident weaknesses in organisation of material but using acceptable mathematical
<ul> <li>present work clearly, with words explaining their processes or steps</li> <li>OR</li> <li>make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer</li> </ul>		form, with few if any errors in spelling, punctuation and grammar. QWC0 Evident weaknesses in organisation of material, and errors in use of mathematical form, spelling, punctuation and grammar.

UNIT 2 (Non-calculator) Foundation Tier	Marks	Comments	
Both parts (a) – (b) marked at the same time         8. (a) Completed card numbers 2(3) 4, 5 and 2, 4, 56         6       12       18       24       30         (5)       10       (5)       20       25         (4)       8       12       16       20         2       4       6       8       10         2       (3)       4       5	B1 B2	C.A.O. F.T. their table, particularly if they writ row values in a different order to the ma B1 for 2 or 3 correct columns OR 2 or 3	e the column and/or ark Scheme 3 correct rows.
View with table from (a)         8. (b) (i) 9/16	B2	F.T. their table B1 for a numerator of 9 in a fraction less than 1. B1 for a denominator of 16 in a fraction less than 1. Do not penalise incorrect reduction of fractions.	NOTES Penalise –1 for use of words such as "9 out of 16", "9 in 16" OR "9:16". When fraction and wrong notation seen, DO NOT penalise wrong notation.
8. (b) (ii) 7/16	B1	F.T. 1– 'their (b)(i)' if a fraction $< 1$	
Overlay (viewed with diagram) 9. Correct rotation	B2	B1 for anticlockwise about (1,4) OR Clockwise about (4,1) OR a near miss B0 if all 4 rotations shown	
10.(a) Sight of 35° or 65° in appropriate working (or on diagram) 115°	M1 A1	May be on the diagram	
10.(b) $x+3x+5x = 180$ , $9x = 180$ or other suitable method (x =) 20(°)	M1 A1		
$(3x =) 60(^{\circ})$ and $(5x =) 100(^{\circ})$	B1	FT their x for their 3x and 5x. May be	on the diagram

UNIT 2 (Non-calculator) Foundation Tier	Marks	Comments
11. Split into 2 triangles, or 4 when using a centre point Making use of 180° as angle sum of a triangle 2 ×180° = 360° or 4 ×180° - 360° = 360°	B1 B1 B1	If diagram with angles torn to then meet at a point gets B1 B1 B0. If only square or rectangle considered, i.e. $4 \times 90^{\circ}$ is $360^{\circ}$ award B1 B1 B0, Or if only square or rectangle considered with angles discussed but no sizes given, then B1, B0, B0, Or angles of 90° with implication of '4' sides or angles, B0, B1, B0 If a candidate quotes '180 $(n - 2)$ ' with $n = 4$ substituted to get 360 then B2, OR for quoting '180 $(n - 2)$ then B1, However, if '180 $(n - 2)$ is explained, based on number triangles, then probably B1, B1, B1. Remember: if a special case quadrilateral is considered then maximum B2. If MR and working to show exterior angles $360^{\circ}$ then for equivalent work treat as MR-1
12.(a) 4x + 20 - 6x + 12 = -2x + 32	B1 B1	FT until 2 <sup>nd</sup> error
12. (b) y <sup>14</sup>	B1	
12.(c) $3b > 27$	M1	
b > 9	A1	27/3 must be evaluated
		If '=' used but replaced to give b>9 then M1,A1, otherwise no
		marks
		SC1 for b>31/3 but do not ignore incorrect cancelling

#### Unit 2 – Higher Tier

UNIT 2 (Non-calculator) Higher Tier	Marks	Comments
1.(a) Sight of 35° or 65° in appropriate working (or on diagram) 115°	M1 A1	May be on the diagram
1.(b) $x+3x+5x = 180$ , $9x = 180$ or other suitable method	M1	
(x =) 20(°)	A1	
$(3x =) 60(^{\circ})$ and $(5x =) 100(^{\circ})$	B1	FT their x for their 3x and 5x. May be on the diagram
2. Correct rotation	B2	B1 for anticlockwise about (1,4) OR Clockwise about (4,1) OR a near miss B0 if all 4 rotations shown
3.(a) Sight of 49 or 16 from correct working	M1	<i>Or:</i> 49.2804 – 15.21, both must be correct M1
Sight of 49 – 16 with 33 shown	A1	(34.0704) rounded to 33 A1 Or: $(7+4)(7-4)$ or unrounded difference of 2 sq M1 Followed by $11 \times 3 = 33$ A1
3. (b) Correct interpretation of $6 \frac{1}{4}$ %, e.g. sight of $(25/4)/100$ or sight	B1	Or splitting percentages correctly with correct place
of 6.25/100, or 0.0625 or 6 <sup>1</sup> / <sub>4</sub> /100	2.01	values, but not showing the sum
$\begin{array}{c} 6 \frac{1}{4} / 100 \times 40 \text{ or } 0.0625 \times 40 \text{ or sum of appropriate percentages} \\ (\pounds) 2.5(0) \end{array}$	MI A1	A method that could lead to a correct response
3. (c) 1 / 2.5 or similar evidence of understanding of term reciprocal	M1	
2/5 or 0.4 or 10/25 or equivalent	A1	Do not accept answer as a decimal within a fraction
3. (d) -11xy -14y +4x	B1	Do not ignore further working. Mark final answer.
4. Deciding of possible outcomes HH TT HT TH	M1	Or calculation P(TT) = $\frac{1}{2} \times \frac{1}{2}$ shown
$P(TT) = \frac{1}{4}$	A1	
Conclusion that the statement is true $(\frac{1}{4} < \frac{1}{2})$	A1	
5.(a) 4x + 20 - 6x + 12	B1	FT until 2 <sup>nd</sup> error
= -2x + 32	B1	Mark final answer
5.(b) $y^{14}$	B1	
5.(c) $3b > 27$	M1	
b > 9	A1	27/3 must be evaluated
		If '=' used but replaced to give b>9 then M1,A1,
		otherwise no marks
		SC1 for $b>31/3$ but do not ignore incorrect
		cancelling

UNIT 2 (Non-calculator) Higher Tier	Marks	Comments
6. Split into 2 triangles, or 4 when using a centre point Making use of $180^{\circ}$ as angle sum of a triangle $2 \times 180^{\circ} = 360^{\circ}$ or $4 \times 180^{\circ} - 360^{\circ} = 360^{\circ}$	B1 B1 B1	If diagram with angles torn to then meet at a point gets B1 B1 B0, with maximum QWC2
		If only square or rectangle considered, i.e. 4 × 90° is 360° award B1 B1 B0, Or if only square or rectangle considered with angles discussed but no sizes given, then B1, B0, B0, Or angles of 90° with implication of '4' sides or angles, B0, B1, B0 AND maximum QWC1 because the communication is only for a special case
		If a candidate quotes '180 $(n - 2)$ ' with $n = 4$ substituted to get 360 then B2, OR for quoting '180 $(n - 2)$ then B1, AND maximum QWC1 However, if '180 $(n-2)$ is explained, based on number triangles, then probably B1, B1, B1 with QWC2 available
		Remember: if a special case quadrilateral is considered then maximum B2 and QWC1
		If MR and working to show exterior angles $360^{\circ}$ then for equivalent work treat as MR-1
<ul> <li>QWC2: Candidates will be expected to</li> <li>present work clearly, with words explaining process or steps with a statement that the angle sum of a triangle is 180° within their response</li> </ul>	QWC 2	QWC2 Presents <u>relevant</u> material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.
<ul> <li>make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer</li> </ul>		QWC1 Presents material in a coherent and logical manner but with some errors in use of mathematical form, spelling, punctuation or grammar OR
<ul> <li>QWC1: Candidates will be expected to</li> <li>present work clearly, with words explaining process or steps with a statement that the angle sum of a triangle is 180° within their response</li> </ul>		evident weaknesses in organisation of material but using acceptable mathematical form, with few if any errors in spelling, punctuation and grammar.
<ul> <li>or within their response</li> <li>or make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer</li> </ul>		QWC0 Evident weaknesses in organisation of material, and errors in use of mathematical form, spelling, punctuation or grammar.
7.(a)(i) Any two points calculated or plotted correctly, with no incorrect points, OR a correct straight line but may have an extra incorrect point plotted	M2	Otherwise M1 for any single correct point, not simply an intersection with an incorrect line, or from an incorrect calculation (0, 6) (1, 4, 5) (2, 3) (3, 1, 5) (4, 0)
Points joined by one straight line	A1	Single straight line, do not ignore incorrect points joined If 1 error in manipulating the equation then penalise -1, then FT. More than 1 manipulative error gets no marks.
7.(a)(ii) -1.5 or equivalent	B1	
7.(b) B D E in this order (y=5x y-3x = 4 $x+y-5=0$ )	B3	B1 for each correct answer

UNIT 2 (Non-calculator) Higher Tier	Marks	Comments
8.(a) 7 000 000 ÷ 4	M1	
= 1,750,000	A1	
$1.75 \times 10^{6}$	B1	FT if M1 awarded, and equivalent difficulty SC1 for $2.8 \times 10^7$
8. (b) 2/3 × 24.6 (million)	M1	Ignore place value in initial calculation
16.4 (million) or 16 400 000	A1	ISW from 16.4 (million), but if incorrect place value then B0
16 million or 16 000 000 or $1.6 \times 10^7$	B1	FT their 2/3 of 24.6 provided M1 awarded. Do not ignore place value, i.e. 16 gets B0
9.(a) $6x^2 + 9x - 10x - 15$	B2	B1 for any 3 correct terms
6x <sup>2</sup> - x -15	BI	Mark final answer
9.(b) Method to eliminate a variable	M1	Allow 1 slip (not in matched variable)
First variable correct	Al	$\mathbf{x} = -3$
Method to find 2 <sup>rd</sup> variable	MI	F I their 1 <sup>st</sup> variable $y = 10$
Second variable	AI	
		FT until 2 <sup>nd</sup> error
9.(c) $3t = 5d - dt$	M1	Expansion of bracket within any step
3t + dt = 5d	M1	Collect terms in t
t(3+d) = 5d	M1	Factorise for t
t = 5d / (3 + d)	Al	Only FT for equivalent difficulty, must have factorised
10. Cyclic quadrilateral opposite angles total 180°	M1	'Cyclic quadrilateral' is insufficient, however
<bad -="" 180="" =="" td="" x<=""><td>M1</td><td>If 180-x seen, this implies 'opposite angles total 180', so if 'cyclic quadrilateral' stated previous M1 can be awarded</td></bad>	M1	If 180-x seen, this implies 'opposite angles total 180', so if 'cyclic quadrilateral' stated previous M1 can be awarded
As an appropriate $2^{nd}$ stage: angle at the centre is twice the angle at the circumference	M1	
<BOD = 2(180 - x) OR $<$ BOD = 360 - 2x convincing	A1	(Accept $^{2} \times 180 - x'$ for $2(180 - x)$ ) Final A1 depends on all previous M marks <i>Alternative:</i> If 'reflex angle at the centre is used, then angles at the point'
		M1 reflex angle at the centre is twice the angle at the circumference
		M1 Reflex $\leq$ BOD = 2x, may be implied in words if given finally algebraically
		M1As an appropriate $2^{nd}$ stage: Angles at a point sum is 360
		A1 360 – 2x convincing
		(Final A1 depends on all previous M marks)
11.(a) $x = 0.0343434$ and $100x = 3.434$ with an attempt to subtract OR equivalent (e.g. $1000x - 10x$ )	M1	OR 3.4/99
34/990 or equivalent	A1	Mark final answer
	<b>D</b> 2	
11.(b) $45 - 3\sqrt{5}\sqrt{2} + 3\sqrt{5}\sqrt{2} - 2$ 43 <b>and</b> rational	B2 B1	CAO
12. Deciding on a strategy, either tree diagrams or appropriate terms	S1	
P(BB) + P(B'B) or equivalent 15 x 5 + 5x 15 must show no replacement	m1	Or equivalent
20 19 2019 inust show no replacement		(For information: P(YB)=45/380, P(RB)=30/380)
150/380 or equivalent	A1	ISW

GCSE MATHEMATICS - UNITISED MS - January 2012



WJEC 245 Western Avenue Cardiff CF5 2YX Tel No 029 2026 5000 Fax 029 2057 5994 E-mail: <u>exams@wjec.co.uk</u> website: <u>www.wjec.co.uk</u>