

GCSE MARKING SCHEME

MATHEMATICS - UNITISED

NOVEMBER 2011

INTRODUCTION

The marking schemes which follow were those used by WJEC for the November 2011 examination in GCSE MATHEMATICS - UNITISED. They were finalised after detailed discussion at examiners' conferences by all the examiners involved in the assessment. The conferences were held shortly after the papers were taken so that reference could be made to the full range of candidates' responses, with photocopied scripts forming the basis of discussion. The aim of the conferences was to ensure that the marking schemes were interpreted and applied in the same way by all examiners.

It is hoped that this information will be of assistance to centres but it is recognised at the same time that, without the benefit of participation in the examiners' conferences, teachers may have different views on certain matters of detail or interpretation.

WJEC regrets that it cannot enter into any discussion or correspondence about these marking schemes.

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UNIT 1 - FOUNDATION TIER

NOVEMBER 2011	Mark	FINAL MARK SCHEME (19/11/11)
UNIT 1 Foundation		Comments (Page 1)
1. Sight of $2 \cdot 5(\text{kg})$ OR $2\frac{1}{2}(\text{kg})$	B1	
$2 \cdot 5 \times (\pounds) 1.3(0)$	M1	F.T. 'their scale reading' \times (£)1.3(0)
= (£)3.25	A1	
	3	
2. (a) Blue 12	B2	For all three correct. B1 for one (or two) correct.
Cream 18 Vellow 10		Allow unambiguous indication in either 'Tally' or
renow 10		precedence)
		precedence).
(b) Blue, Cream and Yellow along one axis.	B1	Or indicated on the bars themselves. Accept B.C and Y.
(c) Drae, eream and renow along one and	21	Ignore widths of bars.
Uniform scale starting at 0.	B1	B0 for ambiguous placing of numbers between grid
		lines.
Three bars at correct heights	B2	B1 for two correct heights. F.T. their frequencies.
		If no scale assume one square to represent a frequency
		of 1. Mark heights on uniform scale that does not start at
	6	0 (e.g. starts at 1) accordingly.
3 (a) Moscow Berlin Cardiff Athens Dublin	0 R1	Accept unambiguous correct order e.g. 7, 3, 0, 2, 2
(b) $7(^{\circ}C)$	B1	Accept unamorguous correct order e.g. $-7, -5, 0, 2, 5$.
(c) $8(^{\circ}C)$	B1	B0 for -8
	3	
4. 22:05 OR 10.05(p.m.)	B1	Accept any unambiguous indication that the correct time
		has been chosen.
$15(\min) \text{ or } \frac{1}{4} \text{ (hour)}$	B1	Accept 45(min) or $\frac{3}{4}$ (hour) if 2235 or 10.35p.m. given
	2	in first part.
$5 \qquad 5 \cdot 0.34 \text{or} 500 \cdot 34 (-14.7)$	<u></u> M1	Accept any attempt to find how many 34s in 500
5. $5 \div 0.54$ or $500 \div 54$ (= 14.7) = 14 (neaches)	A1	Accept any attempt to find now many 545 in 500.
$(change =) (\pounds)5 - 14 \times 0.34$	M1	F.T. their number of peaches only if greater than 1 and
		less than 14.
= (£) 0.24	A1	Accept 24(p). Allow $\pounds 0.24p$ but <u>not</u> 0.24p.
$(\mathbf{T}' \cup \mathbf{v} \to \mathbf{v} $	4	
b. $(11me =) (2 +) 9 \times 30(min)$	MI M1	Signt of 9×30 gains M1 BUT make sure that it is 'Time' that is being found. So, for example,
	1111	9 x f 30 or 25 + 270 will be M0 as 'Money' is implied
		2 A 200 of 20 + 270 will be full as fulling is implied.
$= (2 +) 9 \times \frac{1}{2} (hr)$	A1	Sight of 4 ¹ / ₂ (hrs) or 4hr 30min. gains both M marks.
		May be implied in work that shows understanding of
		correct relationship between hours and minutes.
$= 6\frac{1}{2}$ (hrs) OR 6hrs 30min		Accept rounding up to nearest whole hour above.
$(Charge)$ (f)25 + 61/ \times (f)20	M1	ET (their time given in hours' OD (their time gover ded
$(\text{Charge}=) (t)23 + 0/2 \times (t)30$	IVII	to the nearest whole hour above'
=(f)220	A1	SC1 for (\pounds) 195 (call-out charge not included)
(~)		a contraction of the second seco
	5	

NOVEMBER 2011	Mark	FINAL MARK SCHEME (19/11/11)
UNIT 1 Foundation		Comments (Page 2)
7. (a) $18 + 1.2$ OR $18000 + 1200$	M1	Must use the same units.
(Total weight =) $19 \cdot 2(kg)$ OR $19200(g)$	A1	
0.8(kg) (under) OR 800(g) (under) Look for clarity of text explanations and correct units shown the use of notation (watch for the use of '=', '+' being appropriate)	A1 QWC2	FT their total weight. 'under' not needed for A1, but will be assessed within QWC. QWC2. Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.
		QWC1. Presents relevant material in a coherent and
 QWC2: Candidates will be expected to present work clearly, with words explaining process or steps AND make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer QWC1: Candidates will be expected to present work clearly, with words explaining process or steps OR make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer (b) 50 ÷ 2·2 OR 20(kg) = 20 × 2·2 (lbs) = 22(·727) or 23 = 44(lbs) 	M1 A1	logical manner, but with some errors in use of mathematical form, spelling, punctuation or grammar. OR Evident weakness in organisation of material but using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar. QWC0. Evident weakness in organisation of material and errors in use of mathematical form, spelling, punctuation and grammar. <u>An unsupported answer is QWC0.</u> In (b) they must show their method before any marks can be awarded Also allow $21 \times 2 \cdot 2$ or $22 \times 2 \cdot 2$ $= 46 \cdot 2$ $= 48 \cdot 4$
Luggage is over weight limit.	8 AI	r.1. tielf allswer.
8. 36.8	B2 2	B1 for 36.83(722)
9. (a) 40(% are girls) (b) 0.44×25 or equivalent method = 11(girls)	B2 M1 A1	B1 for $2/5$ (are girls) SC1 for unambiguous correct conversion of $3/5$ or $4/5$ to a percentage (e.g. $3/5 = 60\%$ but not 60% alone).
(c) (No) We do not know how many pupils in Class A.	B1 5	The 'No' may be implied. A correct reason must be given.
10 (a) (Volume =) $8 \cdot 5 \times 6 \cdot 6 \times 3 \cdot 7$	M1	M1 implied by an answer between 207 and 208 inclusive
= 207.57	A1	Accept 207.6 and 207.5.
cm ³	U1	Independent of previous marks.
(b) $(85 \times 66 \times 37) \div (8 \cdot 5 \times 6 \cdot 6 \times 3 \cdot 7)$ OR $10 \times 10 \times 10$	M1	Also allow $(85 \times 66 \times 37) \div$ 'their 207.57'.
= 1000	A1 5	C.A.O.

NOVEMBER 2011	Mark	FINAL MARK SCHEME (19/11/11)
UNIT 1 Foundation		Comments (Page 3)
11. Labelling litres and uniform scale on vertical axis	B1	
Uniform scale on horizontal axis	B1	
		P0,L0 if no attempt at uniform scaling.
Plotting at least two correct points.	P1	\pm ' ¹ / ₂ small square'. The origin may be one of the points.
Correct line drawn	L1	Correct line implies P1L1.
Any correct strategy, e.g 10 times value at 35 litres.	M1	M0 if inappropriate scale used. E.g. 350 litres on scale.
A correct answer for their line.	A1	F.T. their line. Allow M1,A1 for unsupported answers
		between 76 and 78 inclusive or if graph not used.
	6	
12. B	BI	
C .	BI	
A	BI	
	3	
13. Showing a strategy to find total 'running time'	81	E.g. 'Running time' + 'walking time' = 60 minutes .
and total 'walking time' OR use of km/min.	D 1	
Runs for 50min AND walks for 10min.	BI	OR Ten repeats of 5min running and 1min walking is
		enough for STB1
Use of Distance – Time × Speed	M1	Allow this M1 even if time in minutes and sneed per hr
$Runs 18 \times 50/60 (-15 km)$	m1	E T their 'running time' if less than 60 minutes
Walks $6 \times 10/60$ (- 1km)	m1	F T their 'walking time' if less than 60minutes and not
		equal to 'running time'
(Distance =) 16 (km)	A1	equal to running time .
	6	
14. 23970 - 23500	M1	Look out for those who incorrectly use 23970 as a
23500		denominator (giving an answer of 1.96%) which is
× 100	m1	then approximated to 2%. M0m0A0.
=2(%)	A1	
	3	
15. Least Value Greatest Value		
		B1 for each correct entry.
19.5 20.5		Accept 20.49 recurring but not 20.49.
	B4	
745 755		Accept 754.9 recurring but not 754.9.
	4	

UNIT 2 - FOUNDATION TIER

2011 Autumn UNIT 2 (Non calculator)		FINAL POST CONFERENCE
Foundation Tier	Marks	MARK SCHEME
		Comments (21/11/2011) (Page 1)
1. (a) (i) Eleven thousand three hundred and sixty five	B1	
(pounds) (ii) (f) 110680(00p)	B 1	
(1) (2) 110080(.00p)	DI	
(h) (i) 30	B1	
(i) 25	B1	Accept 5×5 OR 5 ²
(iii) 29 OR 31	B1	For either or both, but B0 if any incorrect number given
	5	
2. (a) 700 OR 7 hundred	B1	Do not accept hundred(s)
(b) 1, 3, 9, 27	B2	B1 for any 2 or 3 factors and no incorrect numbers OR for all 4 factors and 1 incorrect number.
(c) $(0).25$	B1	
2/10 OR 1/5	B1	
60(%)	B1	<u>60/100 gets B0</u>
(d) $\pounds 5 - 5 \times 90(p)$	M1	Intention to subtract as many 90p as possible allowing for
		arithmetical errors.
$= 50(\mathbf{p})$	A1	Allow £.50p for the A1, but .50p or £50 get A0.
(e) 3×70	M1	The 3 must not be changed. The 69.8 must be changed to a
= 210	A1	whole number. Only $3 \times 70 = 210$ gets M1, A1.
		All others, for example, 3×69 (= 207) get M1, A0.
	10	
^{3. (a)} C A B	B1	A should be at the half way mark
	B1	<u>B should be to the right of the 'd' and up to 1 exclusive</u>
	B1	C should be at 0.
(b) unlikely	D1	
(b) unikely		
4. (a) 2 rectangles of 6 by 4.5	B1	Use overlay (+2mm)
2 rectangles of 3 by 4.5	B1	
1 rectangle of 6 by 3	B1	
Makes a correct net	B1	
(b) 4	BI	
(c) []		
	B2	B1 for all 4 correct squares and one extra
		OR 2/3 correct squares and no incorrect squares
	7	
5. A (-4,4)	/ B1	Allow the marks even if only the letters as long as it is clear
B (0, 2)	B1	that the correct point is being indicated.
$D^{-}(0, -2)$		Actorise coor unhates gets by on every occasion.
C (-1, -3)	B1	
	3	

2011 Autumn UNIT 2 (Non calculator)		FINAL POST	CONFERENCE
Foundation Tier	Marks	MARK	SCHEME
		Comments (21/1	1/2011) (Page 2)
6. (a) [11 12 13]	B2	B1 for at least 9 correct	IF their sample space has
21 22 23		<u>entries</u>	more than 18 entries
31 32 33			(including the given 3), then
41 42 43			BU for (a) and F.I. in parts (h) and (a) where n aggins
51 52 53			(b) and (c) where possible
01 02 03			
(b) $3/18$ ISW (= 1/6)	B2	FT their table	
		B1 for a numerator of 3 in a	
		fraction less than 1.	
		B1 for a denominator of 18 in	
		a fraction less than 1.	
		Do not penalise incorrect	NOTES
	D.	reduction of fractions.	Penalise –1 for use of words
(c) (1) $6/18$ I.S.W (= $1/3$)	BI	F.T. their sample space in (a)	such as "3 out of 18", "3 in
(ii) $12/19$ LSW (-2/2)	D1	If at least B1 awarded $ET = 1 - (their (a)(i))^2$ if a	18" UR "3:18".
(II) $12/18$ I.S.W $(-2/3)$	DI	$F.I.I^{-}$ then (C)(I) If a fraction < 1	when fraction and wrong
	6		penalise wrong notation
Alternative Mark Scheme for O6 when the tens and unit	s are revei	sed OR their sample space has	less than 9 entries:
internative main peneme for Qo when the tenb and and	<u>, are rever</u>	Sea Ort men sumpre space nas	
6. (a) [11 12 13]	<u>B1</u>	For all entries correct	IF their sample space has
12 22 32			less than 9 entries, then 0
13 23 33			<u>(a) B0 (b) 0 (c) 0</u>
14 24 34			
15 25 35			
10 20 30			
(b) 0/18	B2	B1 for 0 or impossible.	
		·	
(c) (i) 9/18 I.S.W			
(ii) 9/18 I.S.W	<u>B1</u>	<u>IF their (c)(ii) is 1 – their (c) i</u>	2
7 (a) (b) (b -) A(a)	<u>4</u> D1		:
(i) $(B -) + (g)$ (ii) e.g. 5 5 on left pan and 3 3 on right pan	B1	Any answer that makes $\mathbf{B} = A$	ET 'their B'
(ii) e.g. 3, 3 on left with 5 on right pan	B1	Any answer that balances with f	the 1
(ii) e.g. 7, 7 on left with 4 on right with the 10	B1	Any answer that balances with	the 10
(ii) e.g. 4, 4 on left and 7 with the 1	B1	Any answer that balances with	the 1
	5	-	
8. (a) 9	B1		
(b) (i) 84n (p)	B1	Ignore units	
(ii) $x - 100$ (m)	B1	Ignore units	
(c) $3x + 3y$ (d) $6 - 2(4 - 1)2$	B2	B1 for $3x + f(y)$ OR $g(x) + 3$	y
(d) $6x - 3 (= 4x + 2)$	BI D1	Correct clearing bracket	F.1. until 2 nd error
2x = 3 x = 2.5 OR 21/2 OR 5/2	B1	E T av = $b(a \neq 1)$	
x = 2.5 OK 2/2 OK 3/2	8	$1.1. ax = 0 (a \neq 1)$	
9. Table: Probabilities total 1 from the 4 boxes	B1	Evidence for the 1 st 3 marks ma	y be elsewhere on the page
White is 0.2	B1		
P(Y) = 0.3 and $P(P) = 0.3$	B1		
Spinner: R opposite W and Y opposite P	B1		
Given that $P(Y) = P(P)$ and $P(R) = P(W)$ and $P(W) < P(W)$ in the table $V(R)$ is table $V(R)$	B1	Must be from entries in the tab	le. No entries in the table, B0
r(1) in the table, Y & P in <u>larger sectors</u> and K & W in smaller sectors			
H2	5		
	5		

2011 Autumn UNIT 2 (Non calculator)		FINAL POST CONFERENCE
Foundation Tier	Marks	MARK SCHEME
		Comments (21/11/2011) (Page 3)
10.(a) Strategy for the idea of time difference, e.g. 16 hours different, 2 days + 8 1/2 (from NY time on clock)	S1	For the idea of time difference, but there may be an error in the actual time difference Sight of 16
Use of timeline or calculation, e.g. $15\ 00 + 16$ hours, or $3pm + 9$ hours to midnight +, or $0630 + 48$ hrs + $8\frac{1}{2}$ hrs	M1	Sight of 31 or 56 ¹ / ₂ . Or M1 for an alternative complete method that could lead to a correct answer
Thursday AND 07(:)00 or 7 am	A1	Needs day and time, time (0700 or 7am) alone gets S1 M1 A0. Do not accept 700 or 7 as a time, but do not penalise again in QWC <i>An answer of '7(pm) Thurs' when S1 awarded gets M1 A0, but when S1 not awarded gets M0 A0.</i>
OWC: Candidates would be expected to		Penalise-1 for going from London to Sydney (leading to 2am Thursday)
 clearly show how they arrived at their solution have few errors in spelling, punctuation and grammar use capital letters appropriately 	QWC 2	QWC2 Presents relevant material in a coherent and logical manner, using acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.
QWC2: Candidates will be expected to		QWC1 Presents relevant material in a coherent and logical manner but with some errors in use of mathematical form, spelling, punctuation or grammar
 present work clearly, with words explaining process or steps 		OR
 Make few if any mistakes in mathematical form, spelling, punctuation and grammar 		mathematical form, with few if any errors in spelling, punctuation and grammar.
 QWC1: Candidates will be expected to present work clearly, with words explaining process or steps 		QWC0 Evident weaknesses in organisation of material, and errors in use of mathematical form, spelling, punctuation or grammar.
 OR make few if any mistakes in mathematical form, 		A final statement only, e.g. 'Thursday 0700' gets QWC0
their final answer	M2	M1 for intention to multiply by 60, or M1 for intention to divide by 1000 (may be shown by 0.6 km)
(b) 600×60	A1	CAO
1000 36 (km/h)	8	
11. (a) Method that produces at least 2 correct prime	M1	Before 2 nd error
factors	A1	Ignore 1s seen
Sight of correct factors (2, 2, 2, 2, 7) $2^4 \times 7$	B1	FT their factors (with at least 1 index >1 used). Do not ignore 1s.
(b) E.g. ${}^{2^5}$ not even power' or 'no whole number times itself gives 32', '32 is in between 5 ² and 6 ² '	E1	Accept no number times itself gives 32 with 5×5 and 6×6 given. Accept $5 \times 5 = 25$ and $6 \times 6 = 36$ ' Do not accept '25' 36'
H6cd	4	

UNIT 1 - HIGHER TIER

NOVEMBER 2011	Mark	FINAL MARK SCHEME (19/11/11)
UNIT I Higher	M1	Comments (Page 1)
1. (£) 24×1.2 OR (£) $24 + 24 \times 0.2$ = (£) $28.8(0)$	A1	
$(\pounds)28.8(0) \times 4$ OR $(\pounds)28.8(0) - 28.8(0) \times 4$ = $(\pounds)21.6(0)$	M1 A1	F.T. their '24 + VAT' (Must be greater than 24). OR (£)24(.00) \times ³ / ₄ OR (£)24.(00) - 24.(00) \times ¹ / ₄ M1 = (£)18.(00) A1 (£)18 \times 1·2 OR (£)18 + 18 \times 0·2 M1 F.T. 'their (£)18'. = (£)21.6(0) A1
	4	
2. Correctly drawn and labelled.	B4 4	'Correct' angles taken as given below (inclusive). Conservative 167° to 172°, Labour 141° to 145°, Liberal Democrats 29° to 34° and Others 14° to 18°. (As total not a multiple or factor of 360 allow greater tolerance than the usual $\pm 2^\circ$.) B3 for 4 correct angles drawn but not labelled correctly. B2 for 2 or 3 correct angles drawn and labelled. B1 for 1 correct angle drawn and labelled. If no B marks gained. M1 for sight of using a correct method to find an angle or percentage.
3. Three different valid comments.	B3	B1 for each different valid comment.
 e.g. 'Not representative of whole school' 'Small sample' 'Might not get a truthful answer' 'Does not specify over what period of time', 'Might get a poor response' 'Use boxes to show times'. 	2	Accept equivalent statements e.g. 'biased' (by age, gender or ability). 'not confidential' (a criticism of question (i)) 'is it per night or per week?' (a criticism of question (ii)) 'pupils will forget (to hand them in)' <i>Do not give more than one mark for similar criticism(s).</i>
4 (f)800 × 2.08		
= 1664 (NZ dollars)	A1	
270 (NZ dollars on return)	B1	F.T. 'their 1664' – 1391 AND truncated.
$270 \div 2.25$ = (£)120 Look for	M1 A1 QWC2	F.T. 'their return dollars' even if not multiple of 10. QWC2. Presents relevant material in a coherent and logical manner, using acceptable mathematical form,
spellingclarity of text explanations,the use of notation (watch for the use of units being		and with few if any errors in spelling, punctuation and grammar.
appropriate) QWC2: Candidates will be expected to • present work clearly, with words explaining process or steps AND		QWC1. Presents relevant material in a coherent and logical manner, but with some errors in use of mathematical form, spelling, punctuation or grammar. OR Evident weakness in organisation of material but using
 make tew if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer QWC1: Candidates will be expected to 		acceptable mathematical form, and with few if any errors in spelling, punctuation and grammar.
 present work clearly, with words explaining process or steps OR make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units in their final answer 	7	QWC0. Evident weakness in organisation of material and errors in use of mathematical form, spelling, punctuation and grammar.

NOVEMBER 2011	Mark	FINAL MARK SCHEME (19/11/11)
UNIT 1 Higher	D1	Comments (Page 2)
S. B	BI B1	
A	B1	
	3	
6. Showing a strategy to find total 'running time' and total 'walking time' OR use of km/min	S1	E.g. 'Running time' + 'walking time' = 60 minutes.
Runs for 50min AND Walks for 10min.	B1	OR 'Ten repeats of 5min running and 1min walking' is enough for S1B1
Use of Distance = Time \times Speed	M1	Allow this M1 even if time in minutes and speed per hr.
Runs $18 \times 50/60 \ (= 15 \text{km})$	m1	F.T. their 'running time' if less than 60minutes.
Walks $6 \times 10/60$ (= 1km)	m1	F.T. their 'walking time' if less than 60minutes and not equal to 'running time'.
(Distance =) $16 (km)$	A1	
	6	
7. $\frac{23970 - 23500}{23500}$	IVI I	Look out for those who incorrectly use 23970 as a denominator (giving an answer of 1.96 %) which is
× 100	m1	then approximated to 2%. M0m0A0.
= 2(%)	A1	
	3	
8. $\pi \times 50$	M1	
+ 100	M1	(Note for '+100' and not '100'.)
= 257(.07)	AI	F.1. for A1 and B1 only if at least one M1gained and lengths are dimensionally correct and π used
(nearest 10 metres =) 260	B1	E.T. for equivalent work to nearest 10 metres.
	21	SC2 for 130. SC1 for 128.5(0) [Using 50m as
		diameter]
0 (a) 15 × 1200	4 M1	
9. (a) $15 \times \frac{1200}{800}$	MII	Or equivalent e.g. \times 1.5 or \div 0.66(6).
$\times \frac{6}{5}$	M1	Or equivalent e.g. $\times 1.2$ or $\div 0.83(3)$.
= 27 (people)	A1	C.A.O.
		Alternate presentation.
		<u>Scarves Time People</u>
		800 6 15
		Award M1 for one correct step Award M1 for next correct steps
		$\frac{1200}{(Watch out for componenting organ)} = \frac{27}{(Watch out for componenting organ)}$
		(watch out for compensating errors)
(b) $800 \div (15 \times 6)$ OR $1200 \div (27 \times 5)$	B1	FT their 27
(which is less than 10) so 'NO'.		Also $15 \times 6 \times 10$ (required) (which is more than 800).
A correct conclusion must be unambiguously		OR $27 \times 5 \times 10$ (required) (which is more than 1200).
stated or implied.	4	
10. (a) $(60/4) \times 60 \times 60$		For converting 'per second' to 'per hour'
÷ 1000	M1	For converting metres to kilometres.
= 54(km/h)	A1	C.A.O.
(b) Recognising that time could be 4.5 (seconds)	B1	
$\frac{60 \times 3600}{1000}$	M1	F.T. their 'time' only if greater than 4(seconds).
$\overline{4.5 \times 1000}$		
=48(km/h)	A1	A0 if greater than 50(km/h) on F.T.
	0	

NOVEMBER 2011	Mark	FINAL MARK SCHEME (19/11/11)
UNIT 1 Higher		Comments (Page 3)
11. 2116 equivalent to 92(%) implied.	S 1	Allow 2116 = 92(%)
2116×100	M1	Or equivalent.
92		
= 2300(kg)	Al	
12 Dedicing that 24 and much be available the	3 D1	
12. Realising that 24 cards must be considered in	BI	Any use of 24 e.g. 24×8 or 24×0.1 or 24×1 .
solution.		CAO
(Expected length =) $24 \times 8 + 10$	M1	0.11.0.
= 202(cm)	A1	Accept 24mm only if units given.
		C.A.O.
(Maximum 'error' =) 24×0.1 (= 2.4)	M1	Alternate method
(Least length =) 199.6 AND (Greatest length =) 204.4	A1	24 overlaps B1
		Least length $= 250 - 24 \times 2 \cdot 1$ M1
		= 199.6(cm) A1 C.A.O.
		Greatest length $= 250 - 24 \times 1.9$ M1
		= 204.4(cm) A1 C.A.O.
		If no marks gained, then SC2 for 197.5 <u>and</u> 202.5.
	5	SC1 jor euner 1975 <u>or</u> 2025.
13. Sight of $\frac{1}{4} \times \pi \times 8^2$ OR $\frac{1}{2} \times 8^2$	B1	Implied by 50.2 and 32 or $\frac{1}{2} \times 8 \times 8 \times \sin 90^{(\circ)}$
(Area segment =) $\frac{1}{4} \times \pi \times 8^2 - \frac{1}{2} \times 8^2$	M1	
$= 18 \cdot 2(65)(cm^2)$	A1	C.A.O. Accept 18.2 to 18.3 inclusive.
	3	
14. (Volume of hemisphere. =) $\frac{2}{3} \times \pi \times 9^3$	B1	Look for sight of $1526 \cdot 8()$ for this B1.
('Height' of cone =) $15(cm)$	B1	Both B marks may be implied from volume calculations.
(Volume of shape =) $\frac{2}{3} \times \pi \times 9^3 + \frac{1}{3} \times \pi \times 9^2 \times 15$	M1	F.T. 'their hemisphere volume' and 'their cone height'.
		(The formula $\frac{1}{3} \times \pi \times 9^2 \times$ 'their height' must be used
		for the M1 to be awarded)
3.		
= 2799(.15) (cm ³)	A1	Allow 2797 to2801.
		(Look out for those who multiply by 50000 at this stage)
(Volume of pyramid =) $\frac{1}{2} \times 60^2 \times 120$	B1	Look for sight of 144000 for this B1
(Volume of pyramid $=$) /3 × 00 × 120 (Height of 'small' pyramid $=$) 90(cm)	B1	Both B marks may be implied from volume calculations
(noight of shian pyrainia) so(oin)	DI	Dour D marks may be imprice from votanic calculations.
(Volume of shape =) $\frac{1}{3} \times 60^2 \times 120 - \frac{1}{3} \times 45^2 \times 90$	M1	F.T. 'their pyramid volume' and 'their height for the
		small pyramid'.
		(The formula $\frac{1}{3} \times 45^2 \times$ 'their height' must be used for
2		the M1 to be awarded)
$= 83250 (\text{cm}^3)$	Al	
(Number for re-cycling –) 50000×2799	M1	F T their two calculated volumes
83250	1,11	(The 50000 might have already been considered.)
05250		Must be given to the nearest whole number above.
= 1682	A1	6
	10	

UNIT 2 - HIGHER FOUNDATION

Unitised Unit 2 Nov 2011		Final 29/11/11
Higher Lier Markscheme	B2	B1 for either OR correct parallelogram shown OR the point
1. (17, 18) in answer space of annotated on the diagram.	2	(17,18) marked unambiguously on the grid
2. Table: Probabilities total 1 from the 4 boxes	B1	Evidence for the 1 st 3 marks may be elsewhere on the page
White is 0.2	B1	
P(Y) = 0.3 and $P(P) = 0.3Spinner P expective W and V expective P$	B1 P1	
Given that $P(Y) = P(P)$ and $P(R) = P(W)$ and $P(W) < P(Y)$ in	B1 B1	Must be from entries in the table. No entries in the table, B0
the table, Y & P in <u>larger sectors</u> and R & W in <u>smaller sectors</u>	21	
	5	
3.(a) Correct reflection	B2	B1 Any horizontal reflection or a reflection in x=4, OR line y=4 seen
(b) Correct translation	B1 3	
4.(a) Strategy for the idea of time difference, e.g. 16 hours	S1	For the idea of time difference, but there may be an error in the
different, 2 days + 8 $\frac{1}{2}$ (from NY time on clock)		actual time difference Sight of 16
Use of timeline or calculation, e.g. 15 00 + 16 hours, or 3pm +	M1	Sight of 31 or 56 $\frac{1}{2}$. Or M1 for an alternative complete method
9 hours to midnight +, or $0630 + 48 \text{ hrs} + 8 \frac{1}{2} \text{ hrs}$		that could lead to a correct answer
Thursday AND $0/(:)00$ or 7 am	Al	Needs day and time, time (0/00 or 7am) alone gets S1 M1 A0.
		OWC
		An answer of '7(pm) Thurs' when S1 awarded gets M1 A0, but
		when S1 not awarded gets M0 A0.
QWC: Candidates would be expected to		Penalise-1 for going from London to Sydney (leading to 2am
• clearly show how they arrived at their solution	owe	Thursday)
• have few errors in spelling, punctuation and grammar	QWC	OWC2 Presents relevant material in a coherent and logical
• use capital letters appropriately	2	manner, using acceptable mathematical form, and with few if any
		errors in spelling, punctuation and grammar.
QWC2: Candidates will be expected to		OWC1 Presents relevant material in a scherent and lagical
• present work clearly, with words explaining process		manner but with some errors in use of mathematical form.
AND		spelling, punctuation or grammar
• make few if any mistakes in mathematical form,		OR
spelling, punctuation and grammar		evident weaknesses in organisation of material but using
OWC1: Candidates will be expected to		punctuation and grammar.
 present work clearly, with words explaining process 		
or steps		QWC0 Evident weaknesses in organisation of material, and errors
OR		in use of mathematical form, spenning, punctuation of grammar.
• make few if any mistakes in mathematical form, spelling, punctuation and grammar and include units		
in their final answer		A final statement only, e.g. 'Thursday 0700' gets QWC0
	MO	M1 for intention to multiply by 60 or
(b) $\frac{600 \times 60}{1000}$	1012	M1 for intention to divide by 1000 (may be shown by 0.6 km)
36 (km/h)	A1	CAO
5(p) 4 $7 > r$ OP $r > 7$ 4 OP $r > 3$	8 B1	
$\int \frac{1}{x^{-3}} = $	B1	FT from one error
		No marks for use of '=', unless replaced in correct final answer,
(b) $n + 2n - 84$ OD $4n - 84$	N./ 1	then B2
$(0) x + 5x = 64 \text{ OK } 4x = 64 \\ x = 2.1$	Al	SCI for $3x = 84$ with $x = 28$
		An answer $x = 21$ gets M0, A0
(c)(i) $n + 7 > 11$	B1	
n > 4 or $4 < n$	BI	F1 from one error (not from use of '=', but could be '<'). n > 4 alone gets B0 B1
(ii) 5	B1	FT only from the form $n > a$
	7	

6 (a) 5	B1	Accept embedded answer $\sqrt{5}$, 5, Mark final answer
(b) 4	B1	CAO Do not accent $4/1$
(c) Method that produces at least 2 correct prime factors	M1	Before 2 nd error
Sight of correct factors (2, 2, 2, 2, 7)	A1	Ignore 1s seen
Sign of concertacions (2, 2, 2, 2, 7) $2^4 \times 7$	B1	ET their factors (with at least 1 index >1 used). Do not ignore 1s
(d) E g^{25} not even power' or 'no whole number times	F1	Accept no number times itself gives 32 with 5×5 and 6×6
(d) E.g. 2 not even power of no whole number times itself gives 32' '32 is in between 5^2 and 6^2 '	6	riven
itself gives 52, 52 is in between 5 and 6	0	given: Accent $(5 \times 5 - 25 \text{ and } 6 \times 6 - 36)$ Do not accent $(25, 36)$
7(a) $4a + 7$	DO	Accept $5 \times 5 = 25$ and $6 \times 6 = 50$. Do not accept 25, 50
7.(a) 4n + 7	D2 D1	D 1 101 $4n \pm$ D 0 101 $4n$ atome, D 0 101 $n+4$. Allow D 2 101 $n-4n+7$
(b) $05, 02$ (c) Strategy a.g. $1\times 2, 2\times 4, 2\times 5$		Looking at the number of squares with differences
(c) Strategy, e.g. $1 \land 5$, $2 \land 4$, $5 \land 5$, OP (2.8) 15, 24 with an attempt to look at differences	51	Looking at the number of squares with differences
OR (3, 8,) 13, 24 with an attempt to look at unreferences, OP n^2		
$n \times (n)$ OP second difference of 2 OP n^2	M1	If M1 awarded then also award S1
$n \wedge (n \dots)$ OK second difference of 2 OK $n \pm \dots$		II WIT awalded then also awald 51
$n \wedge (n+2)$ OK $n+2n$	A1 6	
8 Three reasonable skatches	D2	B1 for each skatch
8. Three reasonable sketches	D 5	N.P. The 2nd needs to show two disjoint survey $1^{st} e^{2^{rd}}$ intention
	3	to pass through Q
0 Any 3 of the lines $y=5$ $x+y=4$ $x=3$ $x+y=0$ drawn	B3	Award B2 for any 2 lines OP B1 for any 1 line drawn
9. Any 5 of the lines $y = 5$, $x + y = 4$, $x = 5$, $x + y = 0$ that in Correct region indicated	D.3 R1	CAO
Correct region mulcated		CAU
10 Method to find the first variable	4 M1	Allow 1 slip, but not in the aqual coefficient
Correct first variable		Anow 1 ship, but not in the equal coefficient $x = 8$ or $y = 2$
Mothed to find the second variable	AI M1	x = 0 OI $y = -3$
Correct second variable		F1 Hom then first variable
Confect second variable		
11 Transformation horizontally to the right	4 R1	
9 indicated correctly on the x-axis with the correct	B1	SC1 for left shift with 3 indicated on the x-axis
transformation	2	Set for left shift with 5 indicated on the x-axis
	2	E marks depend on B marks being awarded
$\begin{array}{c} 12. \\ (a) CO \text{ or } OC \end{array}$	D1	E marks depend on D marks being awarded
Tangents equal in length	E1	Or equivalent description in words
(b) 110°	B1	or equivalent description in words
Angle centre twice angle circumference AND cyclic	F1	OR angles at a point (or centre) AND angle centre twice angle
anadrilateral		circumference
13 (a) Attempt to subtract $100r - 76464$ and $r - 0.76464$	- - M1	Or equivalent for $1000r = 10r$
757/990		Final answer of 75 $7/99 \text{ M1}$ only
(b) $25 - 15\sqrt{2} - 15\sqrt{2} + 18$	M1	With at least 3 of the terms correct OR $25 \pm 3\sqrt{2} \pm 18$ with $3\neq 0$
$(0) 25 = 15 \sqrt{2} = 15 \sqrt{2} + 10$ = $-43 - 30\sqrt{2}$		CAO
= 45 -50 VZ	R1	ET provided at least M1 awarded
matolia	5	1 1 provided at least will awarded
14 (a) $50/100 \times 50/00$ (- 2500/0000)	B1	
14. (a) $50/100 \times 50/00 = 50/100 \times 50/00$		OB 2. 50/100 x 50/00
$50/100 \times 50/99 + 50/100 \times 50/99$		UK 2× 50/100 × 50/99
5000/9900 (=50/99)	AI	Ignore incorrect cancelling
		FT from (a) if $P(OE)$ and $P(EO)$ and $P(OO)$ used
(b) $1 - P(odd, odd)$	M1	OR P(OE) + P(EO) + P(EE) OR FT (a) + P(EE)
$= 1 - \frac{50}{100} \times \frac{49}{99}$	M1	50/100×50/99+50/100×50/99+50/100×49/99
		OR (a) + $50/100 \times 49/99$
= 7450/9900 (=149/198)	A1	CAO. Ignore incorrect cancelling
	6	
	U	

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