SPECIMEN
RECOGNISING ACHIEVEMENT

GENERAL CERTIFICATE OF SECONDARY EDUCATION MATHEMATICS B Higher Tier

MODULAR PAPER - SECTION B

## Specimen

Candidates answer on the question paper.
Time: 45 minutes
Additional Materials:
Scientific calculator Geometric instruments Tracing paper (optional)

##  <br> H



Candidate Name $\square$

Centre Number


Candidate Number


## INSTRUCTIONS TO CANDIDATES

- Write your name, centre number and candidate number in the boxes above.
- Answer all the questions.
- Write your answers, in blue or black ink, in the spaces provided on the question paper. Pencil may be used for graphs and diagrams only.
- Read each question carefully and make sure you know what you have to do before starting your answer.
- Show all your working. Marks may be given for working which shows that you know how to solve the problem, even if you get the answer wrong.
- Do not write in the bar code.
- Do not write outside the box bordering each page.
- WRITE YOUR ANSWER TO EACH QUESTION IN THE SPACE PROVIDED. ANSWERS WRITTEN ELSEWHERE WILL NOT BE MARKED.


## INFORMATION FOR CANDIDATES

- You are expected to use a calculator in Section B of this paper.
- The number of marks is given in brackets [ ] at the end of each question or part question.
- The total number of marks in this section is 36 .
- This section starts at question 10 .
- Unless otherwise instructed take $\pi$ to be 3.142 or use the $\pi$ button on your calculator.


## FORMULAE SHEET

Volume of prism $=($ area of cross-section $) \times$ length


## In any triangle $A B C$

Sine rule $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$

Cosine rule $a^{2}=b^{2}+c^{2}-2 b c \cos A$


Area of triangle $=\frac{1}{2} a b \sin C$

Volume of sphere $\frac{4}{3} \pi r^{3}$

Surface area of sphere $=4 \pi r^{2}$


Volume of cone $=\frac{1}{3} \pi r^{2} h$

Curved surface area of cone $=\pi r l$


The Quadratic Equation

The solutions of $a x^{2}+b x+c=0$, where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{\left(b^{2}-4 a c\right)}}{2 a}$

10 Twenty people took a reaction time test.
Their times, in seconds, are shown below.

| 4.1 | 3.2 | 3.0 | 5.7 | 6.2 | 5.3 | 5.4 | 3.6 | 4.6 | 4.7 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 3.4 | 5.0 | 5.1 | 4.5 | 3.4 | 4.4 | 4.2 | 5.9 | 5.3 | 4.2 |

(a) Construct an ordered stem and leaf diagram to represent these data.


Key:
(b) Find the median time.
(b)

11 (a) Solve the following equation.
$2(3 x-1)=5$
(a)
(b) Factorise the following completely.

$$
4 x^{2}+12 x y
$$

(b)

12 The diagram shows the cross-section of a garden shed.

(a) Calculate the area of the cross-section.
(a) $\qquad$ $\mathrm{m}^{2}[2]$
(b) The volume of the shed is $5.55 \mathrm{~m}^{3}$.

Calculate the length of the shed.
(b)
m [2]
(c) Use Pythagoras' theorem to calculate $h$.
(c)

13 The table shows the distribution of the weekly wages earned by 200 students working part-time.

| Weekly wage (£w) | Frequency | Mid-point |
| :---: | :---: | :---: |
| $20 \leq w<40$ | 61 | 30 |
| $40 \leq w<50$ | 52 |  |
| $50 \leq w<60$ | 43 |  |
| $60 \leq w<70$ | 27 |  |
| $70 \leq w<100$ | 17 |  |

(a) (i) Calculate an estimate of the mean weekly wage.
(a)(i) $£$ $\qquad$
(ii) Explain why the answer to part (i) is only an estimate of the mean.
$\qquad$
$\qquad$
(b) Draw a histogram to illustrate these data.


## 6

(c) David says that $£ 40-£ 50$ is the modal class.

Give a reason in support of his choice.
$\qquad$
$\qquad$

14 The graph shows the cost of printing personal business cards.

(a) (i) Calculate the gradient of the line.
(a) (i)
[2]
(ii) Explain briefly what this gradient represents.
$\qquad$
$\qquad$
(b) Find the equation in the form $y=m x+c$, where $£ y$ is the cost of printing $x$ business cards.
(b)

15 From a point 14 metres from the base of a tree the angle of elevation of the top of the tree is $25^{\circ}$.


Calculate the height of the tree.

16 The population of a town is 217600 correct to the nearest hundred. The area of the town is $140 \mathrm{~km}^{2}$, correct to the nearest $10 \mathrm{~km}^{2}$.

Calculate the upper bound for the population density.

OXFORD CAMBRIDGE AND RSA EXAMINATIONS
General Certificate of Secondary Education MATHEMATICS B

B293/B
MODULAR PAPER - SECTION B
Specimen Mark Scheme
The maximum mark for this paper is 36 .

| Section B |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 10 | (a) <br> (b) | $\left[\begin{array}{llllllllll}3 & 0 & 2 & 2 & 4 & 4 & 6 \\ 4 & 1 & 2 & 4 & 5 & 6 & 7 & \\ 5 & 0 & 1 & 3 & 3 & 4 & 7 & 9 \\ 6 & 2 & & & & & & \\ \\ 45.5 & & & & & & & & & \\ & & & & & & \end{array}\right.$ |  |  | Correct stem and leaves <br> Leaves in order and under each other <br> All correct <br> Attempt at a middle value accept 45 or 46 for M1 |
|  | (a) <br> (b) | $\begin{aligned} & 2(3 x-1)=5 \\ & \Rightarrow 6 x-2=5 \\ & \Rightarrow 6 x=7 \\ & \Rightarrow x=\frac{7}{6} \\ & 4 x^{2}+12 x y=4 x(x+3 y) \end{aligned}$ | $\begin{array}{\|c\|} \hline \mathbf{M 1} \\ \mathbf{A 1} \\ \mathbf{A 1} \\ \\ \mathbf{B 1} \\ \mathbf{B 1} \\ \hline \end{array}$ | 5 | Expand bracket Correctly <br> Accept $x=1 \frac{1}{6}$ <br> 1 for each factor taken out But -1 if answer given wrongly. |
| 12 | (a) <br> (b) <br> (c) | $\begin{aligned} & A=\frac{1}{2}(2.1+1.6) \times 1.2 \\ & =2.22 \\ & l=\frac{5.55}{\text { their area from }(i)}=\frac{5.55}{2.22}=2.5 \\ & h^{2}=1.2^{2}+(2.1-1.6)^{2} \\ & \\ & =1.2^{2}+0.5^{2} \\ & =1.44+0.25=1.69 \\ & \Rightarrow h=\sqrt{1.69}=1.3 \end{aligned}$ | $\begin{array}{\|l\|} \hline \mathbf{M 1} \\ \mathbf{A 1} \\ \mathbf{M 1} \\ \mathbf{A 1} \\ \mathbf{M 1} \\ \\ \mathbf{A 1} \\ \mathbf{A 1} \end{array}$ | 7 | Area of trapezium formula |
| 13 | (a)(i) <br> (ii) <br> (b) <br> (c) | Midpoints 45, 55, 65, 85 $\begin{aligned} & \text { Sum }=61 \times 30+52 \times 45+55 \times 43+65 \times 27+85 \times 17 \\ & \quad=9745 \\ & \Rightarrow \text { Mean }=\frac{9745}{200}=£ 48.68 \end{aligned}$ <br> Because we do not have the actual values and have assumed all in each group are at the midpoint. <br> Correct histogram <br> Modal group is frequency divided by width, so the larger frequency (20-40 group) is relatively only 30.5 | B1 <br> M1 <br> A1 <br> B1 <br>  <br> B1 <br> B1 <br> B1 <br> B1 |  | Midpoints <br> Multiply frequency by midpoint, add and divide by 200 <br> Widths correct Relative heights correct Frequency density correct |


| 14 | (a)(i) (ii) (b) | 20 divided by $1000=0.02$ Cost per card $y=0.02 x+20$ | M1 <br> A1 <br> B1 <br> B1 <br> B1 |  | $m$ correct c correct |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 15 |  | $\begin{aligned} & h=14 \tan 25 \\ & =6.528 \ldots . . \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \end{aligned}$ | 3 | Tan ratio Correct values Correct answer |
| 16 |  | $\begin{aligned} & \text { Population Density }=\frac{217650}{135} \\ & =1612.2 \ldots \ldots \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \end{aligned}$ |  | Correcting both numbers Both correctly Correct answer |

## Section B Total 36

## Assessment Objectives Grid

| Question | AO2 | AO3 | AO4 | Total |
| :---: | :---: | :---: | :---: | :---: |
| 10 | 0 | 0 | 5 | 5 |
| 11 | 5 | 0 | 0 | 5 |
| 12 | 0 | 7 | 0 | 7 |
| 13 | 0 | 0 | 8 | $\mathbf{8}$ |
| 14 | 5 | 0 | 0 | 5 |
| 15 | 0 | 3 | 0 | $\mathbf{3}$ |
| 16 | 3 | 0 | 0 | $\mathbf{3}$ |
| Totals | 13 | 10 | $\mathbf{1 3}$ | $\mathbf{3 6}$ |

