Rewarding Learning

General Certificate of Secondary Education January 2014


Candidate Number


## Mathematics

## Unit T3


[GMT31]

## *GMT31*

FRIDAY 10 JANUARY, 9.15am-11.15am

## TIME

2 hours.

## INSTRUCTIONS TO CANDIDATES

Write your Centre Number and Candidate Number in the spaces provided at the top of this page.
You must answer the questions in the spaces provided. Do not write outside the box, around each page, on blank pages or tracing paper.
Complete in blue or black ink only. Do not write with a gel pen.
Answer all twenty-nine questions.
Any working should be clearly shown in the spaces provided since marks
may be awarded for partially correct solutions.
You may use a calculator for this paper.

## INFORMATION FOR CANDIDATES

The total mark for this paper is 100 .
Figures in brackets printed down the right-hand side of pages indicate the marks awarded to each question or part question.
Functional Elements will be assessed in this paper.
Quality of written communication will be assessed in questions 6(b) and 24(b).
You should have a calculator, ruler, compasses and a protractor.
The Formula Sheet is on page 2.


## Formula Sheet

Volume of prism $=$ area of cross section $\times$ length


$$
\text { Area of trapezium }=\frac{1}{2}(a+b) h
$$



Volume of cone $=\frac{1}{3} \pi r^{2} h$
Curved surface area of cone $=\pi r l$
Volume of sphere $=\frac{4}{3} \pi r^{3}$
Surface area of sphere $=4 \pi r^{2}$


## Quadratic Equation

The solutions of $a x^{2}+b x+c=0$ where $a \neq 0$ ，are given by

$$
x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}
$$



In any triangle $A B C$


Sine Rule：$\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$

Cosine Rule：$a^{2}=b^{2}+c^{2}-2 b c \cos A$

Area of triangle $=\frac{1}{2} a b \sin C$

1 Without using a calculator, show how to find the answer to

2 Hugh is a travelling salesman. He claims 24.6p for each km he travels and $£ 27.60$ for meals on each day he is travelling.

If he travels more than 700 km in any week he adds $12.5 \%$ to his total claim.

Last week Hugh travelled 915 km in 5 days.
How much did Hugh claim for last week?
Show clearly how you arrived at your answer.

Answer £ $\qquad$ [5]

3 (a) Write down two numbers which are square roots of 49

Answer $\qquad$ and $\qquad$
(b) Explain the meaning of $0.10 \dot{3}$

Answer $\qquad$ [1]

4 The table shows the temperature of some liquids as they cool in a freezer.

| Time (minutes) | 5 | 10 | 15 | 18 | 25 | 30 | 30 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Temperature $\left({ }^{\circ} \mathrm{C}\right)$ | 35 | 31 | 24 | 22 | 12 | 7 | 6 |

(a) Draw a scatter graph for this data.
[2]


(b) Draw a line of best fit.
(c) Estimate the time taken for a liquid to reach freezing point $\left(0^{\circ} \mathrm{C}\right)$.

Answer $\qquad$ minutes [1]

[Turn over

5 Twenty two pupils were asked to record the time (in minutes) they spent on their homework last Monday night.
Their responses are listed below.

| 40 | 55 | 80 | 60 | 50 | 55 | 65 | 40 | 120 | 100 | 90 |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 55 | 60 | 110 | 100 | 120 | 75 | 50 | 80 | 85 | 60 | 45 |

Construct a stem and leaf diagram to illustrate this data.


## Quality of written communication will be assessed in part (b) of this

 question.6 (a) Calculate the size of the interior angle of a regular pentagon.

Answer $\qquad$ ${ }^{\circ}$ [2]
(b) Three regular pentagons are placed together as shown below.

diagram not
drawn accurately

Explain why you cannot cover a floor with regular pentagonal tiles.
Answer $\qquad$
$\qquad$

7 (a) What mathematical name is given to the pair of acute angles $a$ and $b$ below?


Answer $\qquad$
(b) What mathematical name is given to the pair of acute angles $c$ and $d$ below?


| Examiner Only |  |
| :--- | :--- |
| Marks | Remark |
|  |  |
|  |  |

Answer $\qquad$ [1]

8692

8 (a) Factorise $c^{2}-5 c$

| Exa |  |
| :---: | :---: |
| Marks | Remark |

(b) Simplify $\frac{d}{4}-\frac{d}{5}$

Answer $\qquad$

Answer $\qquad$ Total Question 8

9 Solve $7 e+3=4 e+5$

Answer $e=$ $\qquad$ [3]
Total Question 9

10 The $n^{\text {th }}$ term of a sequence is given by $n^{2}-1$
(a) Write down the first 3 terms of this sequence.

Answer $\qquad$ , $\qquad$ -
(b) Explain why 101 cannot be a term in this sequence.

Answer $\qquad$

11 Angela buys 5 DVDs and 4 CDs.
Each DVD costs $d$ pounds.
Each CD costs $c$ pounds.
Write down an expression for the total cost.

Answer $\qquad$ [2]

Total Question 10
5 DVDs and
osts $d$ pound
ts $c$ pounds.
an expression

Answer
Total Question 11
$\square$
[Turn over


12 (a) Express 84 as a product of its prime factors in index form.

Answer $\qquad$
(b) Find the Lowest Common Multiple (LCM) of 63 and 84

Answer $\qquad$

| Examiner Only |  |
| :---: | :---: |
| Marks | Remark |
|  |  |
|  |  |
|  |  |

$13 £ 4000$ is invested in a bank for 3 years and earns $5 \%$ per annum compound interest.

How much will it earn in interest over the 3 years?
Show clearly all your working.

Answer $£$ $\qquad$


14 On every swing, a pendulum reaches $60 \%$ of the previous distance.

The pendulum swings 1.8 metres on its first swing.
How far does it swing during the third swing?

Answer $\qquad$ m [2]

Total Question 14

15 The table below shows the weights of fish caught in a competition.

| Weight (g) | Frequency |
| :---: | :---: |
| $0<w \leqslant 150$ | 10 |
| $150<w \leqslant 300$ | 25 |
| $300<w \leqslant 450$ | 18 |
| $450<w \leqslant 600$ | 12 |
| $600<w \leqslant 750$ | 10 |
| $750<w \leqslant 900$ | 5 |

(a) Write down the modal class interval.

Answer $\qquad$
(b) Write down the class interval which contains the median weight.

Answer $\qquad$
(c) Calculate an estimate for the mean weight of a fish caught in this competition.

16 A student wishes to carry out a survey relating to television viewing by the general public.
Her first question is
"What age are you?"
Answer

(a) Give one criticism of this question.
$\qquad$
(b) Design a more suitable question with appropriate response boxes for her to record the age of those being surveyed.

17 The radius of the base of a cylindrical oil tank is 60 cm .
(a) Calculate the area of the base of the oil tank.

Answer $\qquad$ $\mathrm{cm}^{2}$ [2]

The height of the oil tank is 70 cm .
(b) Calculate the volume of the oil tank. Give your answer in litres.

Answer $\qquad$ litres [3]

18 The sketch shows a field which is in the shape of a right-angled triangle. The side $\mathrm{PQ}=10 \mathrm{~m}$ and the side $\mathrm{QR}=26 \mathrm{~m}$.

| Examiner Only |  |
| :---: | :---: |
| Marks | Remark |
|  |  |

19 A glass window is in the shape of a semi-circle with diameter 40 cm .
Calculate the perimeter of the semi-circle.

diagram not drawn accurately


Answer $\qquad$ cm [3]
Answer $\qquad$ m [3]

Total Question 18
$\qquad$

20 Use the method of trial and improvement to find the solution of the equation $x^{3}+3 x=47$
Give your answer correct to 1 decimal place. Show all your working.

Answer $x=$ $\qquad$ [4]

Examiner Only
Marks $\quad$ Remark

|  |  |
| :---: | :---: |
|  |  |

21 Expand and simplify $3(2 w-1)-2(w-4)$

22 The first five terms of a sequence are $9,13,17,21,25$.
Find an expression, in terms of $n$, for the $n^{\text {th }}$ term of this sequence.

Answer $\qquad$ [2]

Total Question 22


23 During a very cold winter a glacier increased in volume by $32 \%$.
At the end of the winter its volume was found to be $6864 \mathrm{~km}^{3}$
What was its volume at the start of that winter?

| Examiner Only |  |  |
| :---: | :---: | :---: |
| Marks | Remark |  |
|  |  |  |
|  |  |  |
|  |  |  |
| Total Question 22 |  |  |
|  |  |  |

## Quality of written communication will be assessed in part (b) of this question.

24 The information given below relates to the ages (in years) of members of a badminton club.

Lower Quartile $=28$
Median = 32
Upper Quartile = 54
Youngest $=12$
Range $=58$
(a) Draw a box plot to show this information.

(b) The box plot below shows the age distribution of members of a bowls club.


Compare the age distributions of the members of the badminton club and the bowls club.
$\qquad$
$\qquad$
$\qquad$
$\qquad$ [2]

[Turn over

25 The cumulative frequency curve represents the times taken to run 1500 m by each of the members of a running club.

(a) Use the graph to estimate the median time.

Answer $\qquad$ minutes
(b) Any member taking more than $5 \frac{1}{2}$ minutes has to do extra training. Use the graph to estimate the percentage of runners who have to undertake extra training.

| Examiner Only |  |
| :---: | :---: |
| Marks | Remark |
|  |  |

Answer $\qquad$ \%

26 PQRS represents a rectangular gate. $\mathrm{PS}=200 \mathrm{~cm}$ and $\mathrm{SR}=300 \mathrm{~cm}$.
200 cm

diagram not drawn accurately
(a) Calculate the size of angle PRS.

Answer $\qquad$ ${ }^{\circ}$ [3]
(b) The measurements of the gate are all to the nearest centimetre. What is the smallest possible perimeter of the gate?

Answer $\qquad$ cm [2]

diagram not drawn accurately

A large circular pizza has radius 22 cm ．
Josh cuts a sector with angle $40^{\circ}$ from the pizza．
Calculate the area of this sector．

Answer $\qquad$ $\mathrm{cm}^{2}$［3］

| Examiner Only |  |
| :---: | :---: |
| Marks | Remark |
|  |  |

28 Solve the simultaneous equations Show your working．
A solution by trial and improvement will not be accepted．
$3 x+2 y=10$
$2 x-6 y=3$

Total Question 27
$\qquad$ ，$y=$ $\qquad$ ［3］

29 The breadth of a cuboid is 1 cm less than the length $y \mathrm{~cm}$. The height is 6 cm .
The volume of the cuboid is $72 \mathrm{~cm}^{3}$.
(a) Show that $y^{2}-y-12=0$
(b) Solve the equation $y^{2}-y-12=0$ by factorising.

Explain why only one answer makes sense in the question.

Answer $\qquad$
$\qquad$ [3]

THIS IS THE END OF THE QUESTION PAPER


## DO NOT WRITE ON THIS PAGE




