

Rewarding Learning

General Certificate of Secondary Education 2012

Candidate Number
$\square$

## Mathematics

## Unit T4

(With calculator)
Higher Tier

[GMT41]
*GMT41*
WEDNESDAY 6 JUNE $9.15 \mathrm{am}-11.15 \mathrm{am}$

## TIME

2 hours.

## INSTRUCTIONS TO CANDIDATES

Write your Centre Number and Candidate Number in the spaces provided at the top of this page.
Write your answers in the spaces provided in this question paper.
Complete in blue or black ink only. Do not write in pencil or with a gel pen.
Answer all fourteen questions.
Any working should be clearly shown in the spaces provided since marks may be awarded for partially correct solutions.
You may use a calculator for this paper.

## INFORMATION FOR CANDIDATES

The total mark for this paper is 100 .
Figures in brackets printed down the right-hand side of pages indicate the marks awarded to each question or part question.
Functional Elements will be assessed in this paper.
Quality of written communication will be assessed in questions 1 and 7.
You should have a calculator, ruler, compasses and a protractor.
The Formula Sheet is overleaf.
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## Formula Sheet

Volume of prism $=$ area of cross section $\times$ length


Area of trapezium $=\frac{1}{2}(a+b) h$


Volume of cone $=\frac{1}{3} \pi r^{2} h$
Curved surface area of cone $=\pi r l$


In any triangle $A B C$


Sine Rule: $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$
Cosine Rule: $a^{2}=b^{2}+c^{2}-2 b c \cos A$

Area of triangle $=\frac{1}{2} a b \sin C$
Quadratic Equation
The solutions of $a x^{2}+b x+c=0$ where $a \neq 0$, are given by

$$
x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}
$$

$\square$

Quality of written communication will be assessed in this question.
Show your working.
1 (a) In a housing estate $\frac{5}{6}$ of the houses have a garage.
In three out of every four garages there is a car parked.
There are 15 cars in total parked in a garage. Find the number of houses that have no garage.

Answer $\qquad$
(b) An empty tank is in the shape of a cuboid as shown with measurements $1.4 \mathrm{~m}, 1.2 \mathrm{~m}$ and 0.8 m all to the nearest 10 cm .

What is the smallest possible volume of the tank?


Answer $\qquad$ $\mathrm{m}^{3}$

2120 employees in a warehouse were asked how far they travelled to work each day. The table shows their responses.

| Distance (km) | Frequency <br> (number of <br> people) | Distance ( $\leqslant$ ) | Cumulative <br> frequency |
| :---: | :---: | :---: | :---: |
| $0<d \leqslant 5$ | 5 | 5 | 5 |
| $5<d \leqslant 10$ | 12 | 10 | 17 |
| $10<d \leqslant 15$ | 16 |  |  |
| $15<d \leqslant 20$ | 21 |  |  |
| $20<d \leqslant 25$ | 27 |  |  |
| $25<d \leqslant 30$ | 14 |  |  |
| $30<d \leqslant 35$ | 12 |  |  |
| $35<d \leqslant 40$ | 8 |  |  |
| $40<d \leqslant 45$ | 5 |  |  |

(a) Complete the cumulative frequency table above.
(b) Draw the cumulative frequency graph on the grid opposite.
(c) Use your graph to find
(i) the median,

Answer $\qquad$ km [1]
(ii) the percentage of employees who travel more than 18 km to work each day.
$\qquad$ \% [2]
(d) The minimum distance travelled by any employee was 2 km and the maximum distance travelled was 44 km .

Draw a box plot below to illustrate the data for all 120 employees.

(d)


Total Question 2
$\square$
[Turn over
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3 (a) Find the least common multiple (LCM) of 60 and 132.
$\qquad$
(b) M is the point $(-1,4) . \mathrm{N}$ is the point $(5,8)$.

Find the length of MN , correct to 2 decimal places.

Answer $\qquad$

4 (a) Solve the simultaneous equations

$$
\begin{aligned}
& 5 x+2 y=13 \\
& 2 x-3 y=9
\end{aligned}
$$

A solution by trial and improvement will not be accepted.

Answer $x=$ $\qquad$

$$
\begin{equation*}
y= \tag{4}
\end{equation*}
$$

$\qquad$
(b) Factorise fully
(i) $9 x y-12 y^{2}$

Answer $\qquad$
(ii) $g^{2}-9 h^{2}$

## Answer

$\qquad$ [2]

| Examiner Only |  |
| :---: | :---: |
| Marks | Remark |
|  |  |
|  |  |
|  |  |
|  |  |

5 (a) $\mathrm{P}, \mathrm{Q}, \mathrm{R}$ and S are points on the circumference of a circle, centre O . The angle PSR is $48^{\circ}$


Calculate
(i) the angle PQR ,

Answer $\qquad$ ${ }^{\circ}$ [1]
(ii) the reflex angle POR.

Answer

Examiner Only Marks $\quad$ Remark

## (b)



RT is a tangent to the circle, centre O .
Write down the size of angle SRT. Give a reason for your answer.
Answer $\qquad$ - because $\qquad$

| Examiner Only |  |
| :---: | :---: |
| Marks | Remark |
|  |  |

6 (a) (i) Find the equation of the line through the points $(0,1)$ and $(3,13)$.

Answer $\qquad$
(ii) Find the equation of the line which is perpendicular to the line $y=3 x-4$ and passes through the point $(0,7)$.

Answer $\qquad$
(b) Solve the equation

$$
\frac{3 x-5}{2}-\frac{2 x+7}{9}=\frac{11}{6}
$$

A solution by trial and improvement will not be accepted.

Answer $x=$ $\qquad$

| Examiner Only |  |
| :---: | :---: |
| Marks | Remark |
|  |  |

Quality of written communication will be assessed in this question.
7 (a) In a forest, the warden wishes to estimate the number of rabbits. He catches and marks 140 rabbits and releases them again.

The next day he catches 80 rabbits and finds 23 of the marked ones among these.

Estimate the number of rabbits in the forest.
Show your work clearly.

Answer $\qquad$
(b) "Lightup" claim that the lifetime of their light bulbs is over 1200 hours.
(i) Explain why it is necessary to use sampling to find the lifetime of the light bulbs.
$\qquad$
(ii) Describe a suitable sampling method for testing the lifetime of the light bulbs.
$\qquad$
$\qquad$
(c) In a hospital 840 patients were treated for tonsillitis during one year.

Some information on the gender and age groups of these patients is shown in the table below.

|  | Under 15 | $\mathbf{1 5 - 5 0}$ | Over 50 |
| :--- | :---: | :---: | :---: |
| Male | 62 | 260 | 25 |
| Female |  | 413 |  |

The hospital wishes to interview some of the patients.
They take a stratified sample of 80 patients.
(i) How many patients in the sample should be males under 15 ?

Answer $\qquad$
(ii) In the sample taken there were 5 females over 50. Estimate the number of females over 50 who were treated for tonsillitis in the hospital.
$\qquad$

| Examiner Only |  |
| :---: | :--- |
| Marks | Remark |
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|  |  |



Ship P is 62 km from a lighthouse L on a bearing of $072^{\circ}$
Ship Q is 45 km from L on a bearing of $124^{\circ}$
Calculate
(a) the distance between P and Q ,

Diagram not drawn accurately

(b) the area of triangle LPQ,
(c) the bearing of P from Q .


9 The force $F$ exerted by a magnet on a metal button is inversely proportional to the square of the distance $d$ of the magnet from the button.

When $d=8 \mathrm{~cm}, F=2.5$ newtons.
Calculate the distance from the magnet when the force on the button is 6.4 newtons.


10 (a) Expand and simplify $(2 a+3 b)(3 b-2 a)$

Answer $\qquad$
(b) Solve the quadratic equation $5 h^{2}-9 h+3=0$ giving your answer correct to 2 decimal places.

Answer $\qquad$ [3]

| Examiner Only |  |
| :---: | :---: |
| Marks | Remark |
|  |  |
|  |  |
|  |  |

11 (a) Factorise $6 a^{2} x-a b x-12 b^{2} x$

Answer $\qquad$
(b) Solve $\frac{7}{3 x-1}-\frac{5}{x+1}=4$

A solution by trial and improvement will not be accepted.

Answer $\qquad$ [7]


12 The table records the weight, in grams, of some of the 350 parcels which pass through a post office during 1 week.

| Weight ( $\boldsymbol{w}$ grams) | Frequency |
| :---: | :---: |
| $0<w \leqslant 250$ | 55 |
| $250<w \leqslant 500$ | 30 |
| $500<w \leqslant 1000$ |  |
| $1000<w \leqslant 2000$ | 60 |
| $2000<w \leqslant 2500$ | 35 |
| $2500<w \leqslant 4000$ |  |
| $4000<w \leqslant 5000$ | 40 |

(a) Complete the frequency density on the grid.
(b) Use the data in the table to complete the histogram.
(c) Use the data in the histogram to complete the table.
(d) Estimate the median weight of the 350 parcels.


Total Question 12
Answer $\qquad$ g [2]
[Turn over


A vertical telegraph pole TP stands at the corner P of a horizontal field PQRS.

PQRS is a rectangle of length 60 m and breadth 25 m .
The height of the pole is 10 m .
Calculate the angle of elevation of the top of the pole, T, from R.

Answer $\qquad$ [3]

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14 (a) Calculate, showing all your working, the value of $\left(\frac{1}{8}\right)^{-\frac{2}{3}}$

Answer $\qquad$
(b) Find the value of $n$ for which $9^{2 n}=\frac{1}{3}$

Answer $n=$ $\qquad$
(c) $\left(\frac{2^{a}}{3}\right)^{b}=3 \times 2^{a+c}$

Find possible values of $a, b, c$.

Answer $a=$ $\qquad$ $b=$ $\qquad$ $c=$ $\qquad$ [4]

THIS IS THE END OF THE QUESTION PAPER

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| For Examiner's <br> use only |  |
| :---: | :---: |
| Question <br> Number | Marks |
| 1 |  |
| 2 |  |
| 3 |  |
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| 14 |  |
| QWC |  |


| Total |  |
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Examiner Number $\qquad$

