

Rewarding Learning

## General Certificate of Secondary Education

January 2012

## Mathematics



## Module N6 Paper 1

(Non-calculator)

## Higher Tier

[GMN61]
MONDAY 16 JANUARY
$9.15 \mathrm{am}-10.30 \mathrm{am}$

## TIME

1 hour 15 minutes.

## INSTRUCTIONS TO CANDIDATES

Write your Centre Number and Candidate Number in the spaces provided at the top of this page.
Write your answers in the spaces provided in this question paper.
Answer all thirteen questions.
Any working should be clearly shown in the spaces provided since marks may be awarded for partially correct solutions.
You must not use a calculator for this paper.

## INFORMATION FOR CANDIDATES

The total mark for this paper is 56 .
Figures in brackets printed down the right-hand side of pages indicate the marks awarded to each question or part question.

You should have a ruler, compasses, set-square and protractor.
The Formula Sheet is on page 2.

| For Examiner's <br> use only |  |
| :---: | :---: |
| Question <br> Number | Marks |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |
| 5 |  |
| 6 |  |
| 7 |  |
| 8 |  |
| 9 |  |
| 10 |  |
| 11 |  |
| 12 |  |
| 13 |  |
| Total |  |
| Marks |  |

## Formula Sheet

Area of trapezium $=\frac{1}{2}(a+b) h$


Volume of prism $=$ area of cross section $\times$ length


In any triangle $A B C$
Area of triangle $=\frac{1}{2} a b \sin C$
Sine rule : $\quad \frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$
Cosine rule: $a^{2}=b^{2}+c^{2}-2 b c \cos A$


Volume of sphere $=\frac{4}{3} \pi r^{3}$
Surface area of sphere $=4 \pi r^{2}$


Volume of cone $=\frac{1}{3} \pi r^{2} h$
Curved surface area of cone $=\pi r l$


## Quadratic equation:

The solutions of $a x^{2}+b x+c=0$, where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$

1 (a) Given that $\frac{1560}{24}=65$ write down the answer to
(i) $\frac{1560}{240}$

Answer $\qquad$ [1]
(ii) $2.4 \times 6.5$

Answer $\qquad$
(b) Write $0.45555 \ldots$ as a recurring decimal.

Answer $\qquad$
(c) (i) Estimate $\frac{42 \times 596}{78}$

Show your working.

Answer
(ii) Estimate $\frac{213}{0.39}$

## Show your working.

Answer

2 A six-sided dice is biased.
(a) The table below gives the probability of some outcomes when the dice is rolled once.

| Outcome | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Probability | 0.1 |  | 0.15 |  | 0.22 | 0.25 |

(i) The probability of getting a 2 is the same as the probability of getting a 4. Complete the table above for the missing probabilities.
(ii) The dice is rolled 500 times. How many times would you expect to get a 5 ?

Answer $\qquad$ times
(b) Boris plays a game of chess with his friend Gary.

He states, "I can win, draw or lose, so the probability that I will win must be $\frac{1}{3}$ ".

Explain why Boris is wrong.
$\qquad$
$\qquad$
$3 \quad a=\frac{b-c}{d}$
Calculate the value of $a$ when $b=-6, c=10$ and $d=4$

$$
\text { Answer } a=
$$

$\qquad$

4 Ruth has a bag containing 27 white balls and some black balls.
If a ball is taken at random from the bag, the probability that it will be white is $\frac{3}{5}$
(a) Work out the number of black balls that are in the bag.

Answer $\qquad$ black balls

Ruth now puts some more black balls into the bag.
If a ball is now taken at random from the bag, then the probability that it will be black is $\frac{2}{3}$
(b) How many black balls did Ruth add to the bag?

Answer $\qquad$ black balls

5 (a) Reflect the shape in the line $x=3$.

(b) Rotate the triangle $\mathrm{PQR} 90^{\circ}$ anticlockwise about the point $(2,-1)$.

(c) (i) Describe fully the single transformation which maps triangle 1 onto triangle 2

Answer

(ii) Draw the image of triangle $\mathbf{1}$ after a translation 6 left and 1 up. [2]

6 (a) "If $a$ and $b$ are square numbers, then the product of $a$ and $b$ is always an even number." Is this statement true or false? Explain your answer.

Answer $\qquad$ because $\qquad$
$\qquad$
(b) Simplify
(i) $\frac{t^{3}}{t^{8}}$

Answer $\qquad$
(ii) $\frac{t^{2} \times t^{7}}{t^{3}}$

Answer $\qquad$
(c) Solve the inequality $-5<3 n \leq 9$ for integer values of $n$.

Answer $n=$ $\qquad$
(d) Complete the identity $x(x+4) \equiv x^{2}$

7 Calculate $\left(4 \times 10^{9}\right) \times\left(3 \times 10^{-6}\right)$ giving your answer in standard form.

Answer
(Calcule $\left(4 \times 10^{9}\right) \times\left(3 \times 10^{-6}\right)$ giving your
$\qquad$

8 A bag contains a number of coloured counters. Some of them are green.
A counter is taken at random from the bag.
Its colour is recorded and the counter is put back into the bag.
This is repeated 300 times.
The total number of green counters taken from the bag and replaced is recorded after 100 trials, 200 trials and 300 trials as shown in the table.

| Number of trials | Number of green counters | Relative Frequency |
| :---: | :---: | :---: |
| 100 | 45 |  |
| 200 | 105 |  |
| 300 | 144 |  |

(a) Complete the table to show the relative frequencies.
(b) If a counter is picked at random from the bag, estimate the probability of it being green.

Answer $\qquad$

9 (a) Expand and simplify $(n+3)^{2}-(n-3)^{2}$

Answer
(b) Rearrange $\quad P=\sqrt{Q R} \quad$ to make $R$ the subject.

Answer $R=$
$10 y$ is inversely proportional to the square of $x$ and $y=5$ when $x=3$
(a) Express $y$ in terms of $x$.

$$
\text { Answer } y=
$$

$\qquad$
(b) Hence find the value of $y$ when $x=\frac{1}{2}$

$$
\begin{equation*}
\text { Answer } y= \tag{1}
\end{equation*}
$$

$\qquad$

11 Write the recurring decimal $0.1 \dot{4} \dot{5}$ as a fraction.
$\qquad$

Simplify fully $\frac{w}{x y}$

Answer $\qquad$

## $12 w=\sqrt{40} \quad x=\sqrt{2} \quad y=\sqrt{5}$

13 In the square $\mathrm{ABCD}, \overrightarrow{\mathrm{AB}}$ represents the vector a and $\overrightarrow{\mathrm{BC}}$ represents the vector $\mathbf{b}$.
E is the midpoint of $\mathrm{CD} . \mathrm{F}$ is a point on AE such that $\mathrm{AF}: \mathrm{FE}=2: 1$


Express the following in terms of $\mathbf{a}$ and/or $\mathbf{b}$
(a) (i) $\overrightarrow{\mathrm{BD}}$

Answer
(ii) $\overrightarrow{\mathrm{AE}}$

Answer
(iii) $\overrightarrow{A F}$

Answer
(b) Using vectors find the ratio $\mathrm{BF}: \mathrm{FD}$

Show your working.

Answer $\qquad$

Permission to reproduce all copyright material has been applied for In some cases, efforts to contact copyright holders may have been unsuccessful and CCEA will be happy to rectify any omissions of acknowledgement in future if notified.

