

Rewarding Learning

General Certificate of Secondary Education 2011

## Mathematics

Unit T4
(With calculator)
Higher Tier

TUESDAY 31 MAY
$9.15 \mathrm{am}-11.15 \mathrm{am}$

## TIME

2 hours.

## INSTRUCTIONS TO CANDIDATES

Write your Centre Number and Candidate Number in the spaces provided at the top of this page.
Write your answers in the spaces provided in this question paper.
Answer all nineteen questions.
Any working should be clearly shown in the spaces provided since marks may be awarded for partially correct solutions.
You may use a calculator for this paper.

## INFORMATION FOR CANDIDATES

The total mark for this paper is 100 .
Figures in brackets printed down the right-hand side of pages indicate the marks awarded to each question or part question.

Functional Elements will be assessed in this paper.
||| |||||||||||||||||||||||||
Quality of written communication will be assessed in question 11. You should have a calculator, ruler, compasses and a protractor. The Formula Sheet is overleaf.

| For Examiner's <br> use only |  |
| :---: | :---: |
| Question <br> Number | Marks |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |
| 5 |  |
| 6 |  |
| 7 |  |
| 8 |  |
| 9 |  |
| 10 |  |
| 11 |  |
| 12 |  |
| 13 |  |
| 14 |  |
| 15 |  |
| 16 |  |
| 17 |  |
| 18 |  |
| 19 |  |
| Total |  |
| Marks |  |

## Formula Sheet

Volume of prism $=$ area of cross section $\times$ length


In any triangle $A B C$


Sine Rule: $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$
Cosine Rule: $a^{2}=b^{2}+c^{2}-2 b c \cos A$

Area of triangle $=\frac{1}{2} a b \sin C$

## Quadratic Equation

The solutions of $a x^{2}+b x+c=0$ where $a \neq 0$, are given by

$$
x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}
$$

Area of trapezium $=\frac{1}{2}(a+b) h$


Volume of cone $=\frac{1}{3} \pi r^{2} h$
Curved surface area of cone $=\pi r l$


Volume of sphere $=\frac{4}{3} \pi r^{3}$
Surface area of sphere $=4 \pi r^{2}$


1 The angle of elevation of the top of a telephone mast is $23^{\circ}$ from a point 60 metres from the base of the mast on horizontal ground. Calculate the height of the mast.

Answer $\qquad$ m [4]

2 (a) Solve the equation $\frac{2 x-4}{5}+\frac{x+11}{2}=2$

## Show your working.

A solution by trial and improvement will not be accepted.

Answer $x=$ $\qquad$
(b)


Write down the equation of this line in the form $y=m x+c$.
Answer $\qquad$
$\square$

3 The box plots show the distribution of test results for two different classes.

## Class P



Class Q


Comment on two differences between the classes.

1. $\qquad$
2. $\qquad$

4 Bags of coal weigh 12 kg , to the nearest kg .
Find the least and greatest total weight of 9 of these bags.

Answer least $\qquad$ kg
greatest $\qquad$ kg

5 (a) In the diagram O is the centre of the circle.
SOQ is a straight line.

Angle $\mathrm{ORQ}=41^{\circ}$ and angle $\mathrm{PQS}=24^{\circ}$


Find the size of the following angles:
(i) $\mathrm{OQR}=$ $\qquad$ ${ }^{\circ}$ [1]
(ii) $\mathrm{PSQ}=$ $\qquad$ - [1]
(iii) $\operatorname{PSR}=$ - [1]
(b) Show that the exterior angle of the cyclic quadrilateral equals the interior opposite angle (i.e. $x=y$ ).

6 A tea set has a sale price of $£ 63.36$ which is a saving of $12 \%$ on the original price.

What was the original price of the tea set?

Answer £ $\qquad$ [3]

7 The graph opposite shows the cumulative frequency of scores obtained in a darts tournament.
(a) Use the graph to estimate
(i) the median,

Answer $\qquad$
(ii) how many scores were more than 150

Answer $\qquad$

(b) From the graph draw a box plot.


8 (a) Factorise $9 a^{2}-3 a y$
(b) (i) Factorise $x^{2}+x-6$

Answer $\qquad$
(ii) Hence solve the equation $x^{2}+x-6=0$

Answer $\qquad$

Show your working.
A solution by trial and improvement will not be accepted.

Answer $\qquad$
(c) Solve the simultaneous equations $4 x+3 y=1$

$$
2 x-y=-2
$$

Ans

9 Each year a car lost $20 \%$ of its value at the beginning of the year. After how many whole years was it worth less than half of its original value?

Show your working.

Answer $\qquad$ years [3]

10 The diagram shows the intersection of the line $y=x-6$ with the circle with equation $x^{2}+y^{2}=26$

(a) Show that the $x$ co-ordinates of the points of intersection of the line with the circle can be found from the solutions to the equation $x^{2}-6 x+5=0$
(b) Hence find the co-ordinates of the points of intersection of the line and the circle.
$\qquad$ , $\qquad$ ) ( $\qquad$ , $\qquad$ ) [3]

Quality of written communication will be assessed in this question.
11 The table shows information about 600 workers in a factory.

| Age, $\boldsymbol{a}$ years | Number of Males | Number of Females |
| :---: | :---: | :---: |
| $20 \leq a<30$ | 99 | 26 |
| $30 \leq a<40$ | 142 | 48 |
| $40 \leq a<50$ | 124 | 64 |
| $50 \leq a<60$ | 55 | 22 |
| $60 \leq a<70$ | 20 | 0 |

The manager wants to carry out a survey of the workers' views on the workplace. He decides to choose a sample of 80 workers to take part in the survey.
(a) From an alphabetical list of workers' names, he selects every 5th name until he has 80 names.

Explain why this may not produce a fair sample.
Answer $\qquad$
(b) Explain how to take a stratified sample of 80 workers for this data.

12 (a) $y$ is inversely proportional to the square of $x$ and $y=10$ when $x=2$
Express $y$ in terms of $x$.

Answer $\qquad$
(b) Calculate the value of $y$ when $x=5$

13 A small aircraft, located at position A in the sketch diagram, develops an engine fault while flying between two landing strips located at positions
 X and Y in the diagram.
The angles from X and Y to the aircraft are $50^{\circ}$ and $35^{\circ}$ respectively. The aircraft must land as quickly as possible. How much closer is X than Y from A?

Show all working.


Answer $\qquad$ km [4]

14 (a) Simplify

$$
\frac{x^{2}+3 x y-5 x-15 y}{2 x^{2}-10 x}
$$

Answer $\qquad$
(b) Hence write down a negative value of $x$ and the corresponding positive value of $y$ for which

$$
\frac{x^{2}+3 x y-5 x-15 y}{2 x^{2}-10 x}=0
$$

Answer $x=$ $\qquad$ , $y=$ $\qquad$

15 The table gives information about the weights of 100 children.

| Weight, $\boldsymbol{w}$ kg | Number of children |
| :---: | :---: |
| $20 \leq w<30$ | 16 |
| $30 \leq w<35$ | 28 |
| $35 \leq w<40$ | 36 |
| $40 \leq w<60$ | 18 |
| $60 \leq w<65$ | 2 |

(a) Illustrate the data by drawing a histogram, $\mathbf{A}$, on the graph paper opposite.
(b) A stratified sample of 20 children was taken from those whose weight was less than 40 kg .

How many of the sample were taken from the interval $35 \leq w<40$ ?

Answer $\qquad$
(c) The histogram $\mathbf{B}$, already drawn, illustrates the weights of a different group of 100 children. Compare this histogram with the one you have drawn. Give two comparisons.

1. $\qquad$
$\qquad$
2. $\qquad$
$\qquad$
(d) Suggest a reason for the difference in the two histograms.

Answer $\qquad$
$\qquad$
(e) Calculate an estimate for the mean weight of the children in histogram B.

Answer $\qquad$ kg


B


16 (a) Evaluate $289^{\frac{1}{2}}$
$\qquad$
(b) (i) $m, n$ are integers and $2^{m}=\frac{1}{4^{n}}$

Write $m$ in terms of $n$

Answer $m=$ $\qquad$
(ii) $m, n$ are integers and $2^{m}=\frac{1}{2}\left(\frac{1}{4^{n}}\right)$

Write $m$ in terms of $n$

17 Solve $\frac{10}{2 x-5}+\frac{7}{x+2}=3$
$\qquad$
$\square$


The square-based pyramid has four faces which are isosceles triangles.
Calculate the angle between AB and the base.

Answer $\qquad$ - [4]

$\mathrm{AB}=6.2 \mathrm{~cm}$, angle $\mathrm{BAC}=35^{\circ}$ and the area of triangle ABC is $9.2 \mathrm{~cm}^{2}$.
$\mathrm{AD}=10.5 \mathrm{~cm}$ and $\mathrm{CD}=6.4 \mathrm{~cm}$.
Calculate the area of the triangle ACD.

Answer $\qquad$ $\mathrm{cm}^{2}$

## THIS IS THE END OF THE QUESTION PAPER

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