CO
Rewarding Learning

## General Certificate of Secondary Education

 January 2010
## Mathematics



Module N6 Paper 1
(Non-calculator)
Higher Tier
[GMN61]
FRIDAY 15 JANUARY
9.15 am - 10.30 am

## TIME

1 hour 15 minutes.

## INSTRUCTIONS TO CANDIDATES

Write your Centre Number and Candidate Number in the spaces provided at the top of this page.
Write your answers in the spaces provided in this question paper.
Answer all seventeen questions.
Any working should be clearly shown in the spaces provided since marks may be awarded for partially correct solutions.
You must not use a calculator for this paper.

## INFORMATION FOR CANDIDATES

The total mark for this paper is 56 .
Figures in brackets printed down the right-hand side of pages indicate the marks awarded to each question or part question.
You should have a ruler, compasses, set-square and protractor.
The Formula Sheet is on page 2.

| For Examiner's <br> use only |  |
| :---: | :---: |
| Question <br> Number | Marks |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |
| 5 |  |
| 6 |  |
| 7 |  |
| 8 |  |
| 9 |  |
| 10 |  |
| 11 |  |
| 12 |  |
| 13 |  |
| 14 |  |
| 15 |  |
| 16 |  |
| 17 |  |
| Total |  |
| Marks |  |

## Formula Sheet

Area of trapezium $=\frac{1}{2}(a+b) h$


Volume of prism $=$ area of cross section $\times$ length


## In any triangle $A B C$

Area of triangle $=\frac{1}{2} a b \sin C$
Sine rule: $\quad \frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$
Cosine rule: $a^{2}=b^{2}+c^{2}-2 b c \cos A$


Volume of sphere $=\frac{4}{3} \pi r^{3}$
Surface area of sphere $=4 \pi r^{2}$


Volume of cone $=\frac{1}{3} \pi r^{2} h$
Curved surface area of cone $=\pi r l$


## Quadratic equation:

The solutions of $a x^{2}+b x+c=0$, where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$

1 (a) Jill takes 120 steps to cover 72 metres.
What distance will she cover in taking 90 similar sized steps?

Answer $\qquad$ m [2]
(b) A recipe for 2 medium glasses of Apple and blackcurrant smoothie uses

| 250 ml | Apple and blackcurrant juice |
| :--- | :--- |
| 2 tablespoons | Natural yoghurt |
| 180 ml | Milk |
| 3 scoops | Vanilla ice cream |

Complete the recipe for 5 medium glasses.

| Answer |  |
| ---: | :--- |
| $\ldots \mathrm{ml}$ | Apple and blackcurrant juice |
| 5 tablespoons | Natural yoghurt |
| $\ldots \mathrm{ml}$ | Milk |
| $\ldots$ scoops | Vanilla ice cream |

2 Complete the identities
(a) $\frac{x}{4} \equiv \underline{3 x}$
(b) $3(y+2)-2 y \equiv y$

3 In a fairground game of chance, 120 people buy one ticket each.
The cost of a ticket is 50 p .
The probability that a person wins a prize is $\frac{1}{12}$
Each winning ticket gets a prize of $£ 1.50$
What profit is made by the fairground?

Answer $£$ $\qquad$ [2]

4 Given that $49 \times 123=6027$

Find
(a) $4.9 \times 12.3$

Answer $\qquad$
(b) $602.7 \div 4.9$

Answer $\qquad$ [1]

5 (a) Use the formula $P=3 R-4(Q-2)$ to find the value of $P$ when $Q=-8$ and $R=-6$

Answer $P=$ $\qquad$ [3]
(b) Use the formula $L=\frac{M(N+8)}{6}$ to find the value of $L$ when $M=9$ and
$N=-30$
$\qquad$

6 (a) Rearrange $2 p-3=6-q$ to make $q$ the subject.
Simplify your answer.

Answer $q=$ $\qquad$
(b) Simplify
(i) $d^{3} \times d^{4}$

Answer $\qquad$
(ii) $\frac{e^{8}}{e^{4}}$

Answer $\qquad$
(iii) $\frac{f \times f^{3}}{f^{9}}$

Answer $\qquad$ [1]
(c) "If $a$ and $b$ are prime numbers, then $a \times b$ is always an odd number." Is this statement true or false? Explain your answer.

Answer $\qquad$ because $\qquad$
$\qquad$

7 Jill and Joan both work in the same office.
The probability that Jill is late for work on a given day is 0.15
The probability that Joan is late for work on a given day is 0.2
(a) What is the probability that both of them are late for work on the same day?

Answer $\qquad$ [2]
(b) What assumption did you make in answering part (a)?

Answer $\qquad$

8 (a) Reflect the shape below in the line $y=1$


(i) Draw the image of triangle A after a translation $\binom{6}{-2}$
(ii) Describe fully the single transformation which maps triangle A onto triangle B .

Answer $\qquad$
$\qquad$

9 Opposite faces of a dice add up to give seven.
As shown, the total of the numbers on the front faces is $3+2+5=10$
In one move, each dice below is rotated in the direction shown one face at a time (a quarter turn).
After two moves, what will be the total of the numbers on the front faces?
Show your working.


Answer Total =

10 In a survey of 200 cars crossing a bridge, 45 had no passengers.
On a day when 4000 cars cross the bridge, how many cars would you expect to have no passengers?

Answer $\qquad$

11 Brenda knows that one of the following formulae can be used to find the correct area of a shape. Each letter $a, b, c, d$ represents a length.

Which is the correct formula? Give a reason for your answer.
A $\pi a c^{2}+a b^{2}$
B $\pi a^{2} b+b c^{2}$
C $\frac{1}{3} b+\pi c$
D $\quad \frac{1}{4} c d+a^{2}$

Answer $\qquad$
because
$\qquad$
$\qquad$

12 Show that $(n+2)^{2}-(n-2)^{2} \equiv 8 n$

13 (a) Which of the following is closest to $\sqrt{0.91}$ ?
Circle your answer.
0.45
0.3
0.9
[1]
(b) Write $0.1 \dot{7}$ correct to 3 decimal places.

Answer $\qquad$
(c) Write the recurring decimal 0.215 in fraction form.

Answer $\qquad$ [2]

14 Simplify $\left(3 x^{2} y^{3}\right)^{4}$
Answer

$O P Q R$ is a parallelogram. $M$ is the mid-point of $R Q$.
$\overrightarrow{\mathrm{OP}}=\mathbf{a}$ and $\overrightarrow{\mathrm{OR}}=\mathbf{b}$

Express in terms of $\mathbf{a}$ and/or $\mathbf{b}$
(a) $\overrightarrow{\mathrm{QP}}$,
Answer $\qquad$
(b) $\overrightarrow{\mathrm{OM}}$,
Answer $\qquad$
(c) $\overrightarrow{\mathrm{PM}}$.
Answer $\qquad$ [1]
$16(x-4)^{2}+e \equiv x^{2}-d x+21$
(a) Find values for $d$ and $e$.

Answer $d=$ $\qquad$ $e=$ $\qquad$
(b) Hence write down the minimum value of the expression $x^{2}-d x+21$ from part (a).

Answer $\qquad$

17 At a party each child is given a balloon at random.
There are 20 red balloons and 40 yellow balloons.
What is the probability that the first two children receive the same colour of balloon?
Answer $\qquad$ [4]

