

Rewarding Learning

## General Certificate of Secondary Education

 January 2010Mathematics


Module N4 Paper 2
(With calculator)
Higher Tier
[GMN42]
TUESDAY 12 JANUARY

### 10.30 am-11.30 am

## TIME

1 hour.

## INSTRUCTIONS TO CANDIDATES

Write your Centre Number and Candidate Number in the spaces provided at the top of this page.
Write your answers in the spaces provided in this question paper.
Answer all eleven questions.
Any working should be clearly shown in the spaces provided since marks may be awarded for partially correct solutions.

## INFORMATION FOR CANDIDATES

The total mark for this paper is 44 .
Figures in brackets printed down the right-hand side of pages indicate the marks awarded to each question or part question.
You should have a calculator, ruler, compasses, set-square and protractor.
The Formula Sheet is on page 2.

| For Examiner's <br> use only |  |
| :---: | :---: |
| Question <br> Number | Marks |
| 1 |  |
| 2 |  |
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| Total <br> Marks |  |

## Formula Sheet

Area of trapezium $=\frac{1}{2}(a+b) h$


Volume of prism $=$ area of cross section $\times$ length


## In any triangle $A B C$

Area of triangle $=\frac{1}{2} a b \sin C$
Sine rule: $\quad \frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$
Cosine rule: $a^{2}=b^{2}+c^{2}-2 b c \cos A$


Volume of sphere $=\frac{4}{3} \pi r^{3}$
Surface area of sphere $=4 \pi r^{2}$


Volume of cone $=\frac{1}{3} \pi r^{2} h$
Curved surface area of cone $=\pi r l$


## Quadratic equation:

The solutions of $a x^{2}+b x+c=0$, where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$

1 A tennis club holds a Junior Tournament.
The time taken to complete each match is recorded.
(a) The statistical data for the girls' matches is:

Minimum time
42 minutes
Maximum time
104 minutes
Lower quartile
68 minutes
Upper quartile 90 minutes
Median time 84 minutes
Draw a box plot to illustrate this data.

[2]
(b) Similar data is recorded for the boys' matches and a box plot drawn.


Give two comments on the times taken to complete the girls' matches compared to the times taken to complete the boys' matches.
$\qquad$
$\qquad$

2 St Elsewhere High School had an 8\% absence rate on a particular day.
If there were 989 pupils present, how many pupils were absent?

Answer $\qquad$

3

Diagram not drawn accurately

The angle of elevation from $A$ to the top of the tree C is $35^{\circ}$ The distance $\mathrm{AB}=20 \mathrm{~m}$.

Calculate the height BC of the tree.

Answer $\qquad$ m [3]


4 Find the volume of a spherical ball of radius 10 cm .

5 (a) Expand and simplify $(3 x+5)(4 x-2)$
(b) Factorise $x^{2}-3 x-40$

Answer

6 Write down the equation of the straight line which passes through the point $(0,-3)$ and is perpendicular to the line $y=4 x+1$
$\qquad$

7 Calculate the distance between the points with coordinates (3, 1, -4) and (7, 4, 8).

8 (a) Solve the equation $6 m^{2}+7 m+2=0$

Answer $\qquad$
(b) Solve the following equation, giving your answers correct to two decimal places.

$$
x^{2}-5 x-3=0
$$

Answer $\qquad$ [3]

9 The table shows the distribution of the heights of all sixth formers in a school.

| Height $(\boldsymbol{h} \mathbf{~ c m})$ | Number of students |
| :---: | :---: |
| $150 \leqslant h<165$ | 45 |
| $165 \leqslant h<175$ | 75 |
| $175 \leqslant h<180$ | 36 |
| $180 \leqslant h<185$ | 66 |
| $185 \leqslant h<195$ | 18 |

(a) Show this information on a histogram on the graph paper below.

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(b) Students at least $H \mathrm{~cm}$ tall are considered for the basketball team.

A stratified sample of 40 students is selected from this group. Six of the stratified sample are at least 185 cm tall.

Calculate the value of $H$.

Answer $H=$ $\qquad$ [3]


ABD is an isosceles triangle with angle $\mathrm{A}=80^{\circ}$ and $\mathrm{AB}=\mathrm{BD}$.
$\mathrm{AB}=15 \mathrm{~cm}$ and $\mathrm{BC}=7 \mathrm{~cm}$. Angle $\mathrm{ABC}=115^{\circ}$
Calculate the length of CD.
$\qquad$ cm [4]

11 Solve $\frac{1}{2 x-3}+\frac{4}{x+1}=1$

A solution by trial and improvement will not be accepted.

Answer $\qquad$ [7]

