

Rewarding Learning

## General Certificate of Secondary Education

January 2009

## Mathematics



Module N4 Paper 1
(Non-calculator)
Higher Tier
[GMN41]
FRIDAY 9 JANUARY
9.15am-10.15 am

## TIME

1 hour.

## INSTRUCTIONS TO CANDIDATES

Write your Centre Number and Candidate Number in the spaces provided at the top of this page.
Write your answers in the spaces provided in this question paper.
Answer all twelve questions.
Any working should be clearly shown in the spaces provided since marks may be awarded for partially correct solutions.
You must not use a calculator for this paper.

## INFORMATION FOR CANDIDATES

The total mark for this paper is 44 .
Figures in brackets printed down the right-hand side of pages indicate the marks awarded to each question or part question.
You should have a ruler, compasses, set-square and protractor. The Formula Sheet is on page 2.

| For Examiner's <br> use only |  |
| :---: | :---: |
| Question <br> Number | Marks |
| 1 |  |
| 2 |  |
| 3 |  |
| 4 |  |
| 5 |  |
| 6 |  |
| 7 |  |
| 8 |  |
| 9 |  |
| 10 |  |
| 11 |  |
| 12 |  |
| Total <br> Marks |  |

## Formula Sheet

Area of trapezium $=\frac{1}{2}(a+b) h$


Volume of prism $=$ area of cross section $\times$ length


In any triangle $A B C$
Area of triangle $=\frac{1}{2} a b \sin C$
Sine rule: $\quad \frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$
Cosine rule: $a^{2}=b^{2}+c^{2}-2 b c \cos A$


Volume of sphere $=\frac{4}{3} \pi r^{3}$
Surface area of sphere $=4 \pi r^{2}$


Volume of cone $=\frac{1}{3} \pi r^{2} h$
Curved surface area of cone $=\pi r l$


## Quadratic equation:

The solutions of $a x^{2}+b x+c=0$, where $a \neq 0$, are given by
$x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$

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(Questions begin overleaf)

1 Eileen constructed a cumulative frequency table from her mobile phone bill to display her call times over the previous month. The results are shown in the table below.

| Time in minutes | Cumulative frequency |
| :---: | :---: |
| $<5$ | 29 |
| $<10$ | 62 |
| $<15$ | 114 |
| $<20$ | 153 |
| $<25$ | 179 |
| $<30$ | 195 |

(a) Draw a cumulative frequency graph, on the opposite page, to display the data.
(b) From your graph, estimate the median for Eileen's call times.

Answer $\qquad$ minutes [1]
(c) Eileen's pricing plan with the phone company allows her free calls provided that they last no more than 12 minutes.
From your graph, estimate the number of calls which will be charged to Eileen's account by the phone company.

Answer $\qquad$ calls [
(d) The shortest call took one minute and the longest took 29 minutes. Draw a box plot on the grid below the cumulative frequency graph to illustrate the data. to


2 Calculate $4 \frac{1}{4} \times 2 \frac{2}{3}$
Give your answer as a mixed number.
$\qquad$

3 Solve the equation $\frac{x+2}{2}-\frac{2 x-1}{3}=2$
Show your working.
A solution by trial and improvement will not be accepted.

Answer $x=$ $\qquad$ [4]

4 The graphs of the lines $y=x+1$ and $x+2 y=8$ are shown in the diagram.

(a) Identify with a letter $R$, the region which satisfies the inequalities

$$
\begin{equation*}
y \geq x+1 \quad x+2 y \leq 8 \quad x \geq 0 \tag{2}
\end{equation*}
$$

(b) What is the greatest value of $x$ in this region?

Answer $\qquad$
(c) What point $(x, y)$ in the region R maximises the value of the expression $y-x$ ?

Answer $x=$ $\qquad$ $y=$ $\qquad$

## reman

5536 pupils attend a secondary school. There are a total of 20 registration classes.

A random sample of 40 pupils is to be chosen to represent the school at a charity event.

The principal suggests that every 10th pupil in alphabetical order in each registration class should be chosen to attend the charity event.

Give two reasons why this selection process is flawed.

## Reason 1

$\qquad$
$\qquad$

## Reason 2

$\qquad$
$\qquad$

6 Calculate the length of the space diagonal JP in the cuboid shown.
Give your answer in the form $\sqrt{n}$.

Answer $\qquad$ cm [2]
$\square$


7 A wedding cake has two tiers, which are similar in shape.
The area to be iced on the small tier is 100 square inches.
The area to be iced on the large tier is 225 square inches.
The width of the larger tier is 12 inches.
What is the width of the smaller tier?

Answer $\qquad$ inches [

8 Evaluate
(a) $64^{0.5}$

Answer $\qquad$
(b) $27^{2 / 3}$

Answer $\qquad$ [2]
(c) $16^{-3 / 4}$

Answer $\qquad$


Use the graph to find solutions for the equation

## Examiner Only

(a) $\sin x=-0.95$

Answer $x=$ $\qquad$
(b) $5 \sin x=3$

Answer $x=$

11 State which one of the following equations has solutions which are rational. Explain why this is the case.
(a) $\frac{x^{3}}{3}=8$
(b) $\frac{8 x^{3}}{3}=9$
(c) $\frac{x^{3}}{4}=9$

Answer $\qquad$ because $\qquad$
$\qquad$
$12(x-a)^{2} \equiv x^{2}-12 x+b$
Find the values for $a$ and $b$

Answer $a=$ $\qquad$ $b=$ $\qquad$ [3]
$\square$

