

# General Certificate of Secondary Education 

## Mathematics 3301 Specification A

## Paper 2 Intermediate

## Mark Scheme

2007 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

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## Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

M Method marks are awarded for a correct method which could lead to a correct answer.

A Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.

B Marks awarded independent of method.
Mdep A method mark dependent on a previous method mark being awarded.
B dep A mark that can only be awarded if a previous independent mark has been awarded.
ft Follow through marks. Marks awarded following a mistake in an earlier step.

SC Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.
oe Or equivalent. Accept answers that are equivalent. eg, accept 0.5 as well as $\frac{1}{2}$

## Paper 2I

| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| $\mathbf{1 ( a )}$ | $658 .(\ldots)$ | B1 |  |
| :---: | :--- | :---: | :---: |
| $\mathbf{1 ( b )}$ | $1.7(\ldots)$ | B1 |  |
| $\mathbf{1 ( c )}$ | $7.37(\ldots)$ | B1 | $\frac{258}{35}$ |


| $\mathbf{2}$ | $1.5 \times 98$ | M1 | $1.5 \times 0.98$ |
| :---: | :--- | :---: | :--- |
|  | $249-$ Their 147 | M1 | $2.49-$ Their $1.47,0.17$ or 17 gets M2 |
|  | Their $102 \div 85$ | M1dep | Only dependent on $2^{\text {nd }}$ M1 <br> Their $1.02 \div 0.85,1.02 \div 85$, not $2.49 \div 85$ |
|  | 1.2 | A1 | SC2 0.012 or other position of decimal point |


| 3 | Fully Correct | B3 | B2 for inner 8 correct (ignore extras) <br> B1 for outer 4 correct (ignore extras) <br> SC1 any other rational symmetry of order 4 |
| :---: | :---: | :---: | :---: |
| 4 | Method 1: Attempt to compare using equilateral triangles / rhombi <br> Method 2: Using formulae | B1 | Method 1: eg, 2 bottom halves equal <br> Need line drawn <br> Method 2: eg, $\mathrm{b} \times \mathrm{h}$ for rhombus or $\frac{1}{2} \mathrm{~b} \times \mathrm{h} \text { for triangle }$ <br> B2 Complete hexagon on diagram and show each is $\frac{1}{3}$ of the hexagon |
|  | Complete argument | B1 | Method 1: Show that both top halves are $\frac{1}{2}$ of a rhombus or are the same <br> Method 2: Using both formulae and triangle has double the height |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 5 | $\begin{array}{ccccc} 2 & 2 & 5 & 6 & 7 \\ 3 & 3 & 6 & 7 & 8 \\ 6 & 6 & 9 & 10 & 11 \\ 7 & 7 & 10 & 11 & 12 \\ 8 & 8 & 11 & 12 & 13 \end{array}$ | B2 | One or two errors in table B1 <br> If table not used full listing of totals B2 <br> 1 or 2 errors / omissions of totals B1 <br> Allow E, O or W, L or explained symbols |
|  | Counting up Their odds and evens eg, 13 Even, 12 Odd | M1 | $\text { eg, } \mathrm{P}(\text { even })=\frac{13}{25} \text { or } \mathrm{P}(\text { odd })=\frac{12}{25}$ <br> Must have numbers |
|  | eg, More evens than odds or Yes | A1ft |  |

Allow embedded solutions, but if contradicted M marks only

| $\mathbf{6 ( a ) ( i )}$ | 32 | B1 | $\frac{32}{1}$ is B0 |
| :---: | :--- | :--- | :--- |
| $\mathbf{6 ( a ) ( i i ) ~}$ | $4 w=13-3$ | M1 | $w+\frac{3}{4}=\frac{13}{4}$ |
|  | $2.5,2 \frac{1}{2}$ | A1 | $\frac{10}{4}$ oe |
|  | 14 | B2 | B1 for -6 or $\pm 6$ seen |
| $\mathbf{6 ( c )}$ | $4 x-12$ | B1 |  |
| $\mathbf{6 ( d ) ( i ) ~}$ | $3(2 a+3)$ | B1 |  |
| $\mathbf{6 ( d ) ( i i ) ~}$ | $(x+5) x$ | B1 | $(x+5)(x+0)$ |


| 7(a) | 1415 seen or marked on table | B1 | 2.15 |
| :---: | :---: | :---: | :---: |
|  | 1415-1040 must be times | M1 | eg, $20+3+15,64+26+74+51,215(\mathrm{mins})$ |
|  | 3 h 35 m | A1 |  |
| 7(b) | $1 \mathrm{~h} 30 \mathrm{~m}=1.5$ | B1 | $1 \mathrm{~h} 30 \mathrm{~m}=90$ |
|  | Distance / Time | M1 | $96 \div 1.5,96 \div 90 \times 60,96 \div 1.3,$ <br> Not $96 \div 90 \times 100$ |
|  | 64 | A1 | SC1 73.8 |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :--- | :---: | :--- |
| $\mathbf{8}$ Substituting for $\mathrm{t}=3$ in both terms M1 Even if algebra not correct <br>  9 from $3 \times 3$ or -18 A1  <br>  0 A1  |  |  |  | | ( |
| :--- |


| 9(a) | Straight line, if extended, to pass <br> within $(0,13)$ to $(0,15)$ and <br> $(10,22)$ to $(10,24)$ inclusive | B1 | At least between $x=2$ and $x=8$ |
| :---: | :--- | :---: | :--- |
| $\mathbf{9 ( b ) ~}$ | Increase together | B1 | oe Positive correlation or Their equation of <br> line of best fit |


| $\mathbf{1 0 ( a )}$ | Reflection | B1 | Must be single transformation |
| :---: | :--- | :---: | :--- |
|  | In $y$ axis | B1 | oe in $y$, in $x=0$, in line $y$, in vertical axis |
| $\mathbf{1 0 ( b )}$ | Correct translation | B1 | $(-1,-2),(-1,0),(0,-2)$ |
| $\mathbf{1 0 ( c )}$ | Any enlargement | B1 | Any orientation. Not scale factor 1 |
|  | Scale factor 3 | B1 | Any orientation |
|  | Centre $(0,1)$ | B1 | $(3,1),(6,1),(3,7)$ |


| 11 | $\frac{40}{100} \times 65$ | M1 | 26 Build up method OK |
| :---: | :--- | :---: | :--- |
|  | $65-$ Their 26 | M1dep | $\frac{60}{100} \times 65$ gets M2 |
|  | 39 | A1 |  |


| $\mathbf{1 2}$ | $(80$ or 280 or 190$) \div 24 \times 36$ | M1 | $120 \pm 2,420 \pm 2,285 \pm 2$ for all 3 |
| :---: | :--- | :---: | :--- |
|  | $120,420,285$ | A2 | A1 for 1 or 2 correct. SC1 for 825 |


| 13(a) | Graph passing through $(0,10)$ | B1 | 1 correct point plotted or worked |
| :---: | :--- | :---: | :--- |
|  | Graph gradient -2 | B1 | 2 further points plotted or worked |
|  | Graph passing from $(0,10)$ to <br> $(5,0)$ with no errors to $\frac{1}{2}$ sq | B1 | If $>2$ lines (including $y=7)$ then B1 maximum |
| $\mathbf{1 3 ( b ) ~}$ | Correct horizontal line at least <br> 1 cm long | B1 | To $\frac{1}{2}$ sq accuracy. Must be a single line |


| Q | Answer | Mark | Comments |
| :---: | :--- | :---: | :--- |
| $\mathbf{1 4 ( a ) ( i ) ~}$ 36 B1  <br> $\mathbf{1 4 ( a ) ( i i ) ~}$ Goes up in 7's, add on 2 lots of 7 B1 oe $7 n+1,7 x+1$ <br> B0 for in 7 times table, B0 for add 7 <br> $\mathbf{1 4 ( b )}$ $7 n+1$ or $n=7 n+1$ or $x=7 n+1$ B2 oe B1 for $7 n+$ anything, $n 7+1,7 x+1$ <br> B2 for $n \times 7+1$ <br> $\mathbf{1 4 ( c ) ~}$ $358=7 n+1$ M1  <br>  51 A1 SC1 for 50 or 51 with wrong working |  |  |  |


| $\mathbf{1 5 ( a )}$ | Bearing $037^{\circ} \pm 2$ | B1 |  |
| :--- | :--- | :---: | :--- |
|  | $290^{\circ} \pm 2$ | B1 |  |
|  | Correct intersection of lines | B1 | Ignore any $x$. Within $\frac{1}{2}$ sq of grid intersection |
| $\mathbf{1 5 ( b )}$ | 6 to 6.2 cm | B1 |  |
|  | Their $6.1 \times 5$ | M1 |  |
|  | 30 to 31 | A1 |  |


| 16 | $\begin{aligned} & 35 \div 500 \times(100) \text { and } \\ & 28 \div 330(\times 100) \end{aligned}$ | M1 | $35 \div 500 \times 330 \text { or } 28 \div 330 \times 500$ <br> 500:35 and 330:28 and at least 1 attempt to cancel $500 \div 35$ and $330 \div 28$ |
| :---: | :---: | :---: | :---: |
|  | 0.07 (7) and 0.08... (8 or 8.5 ) | A1 | 23.(1) or 42.(42), 14.(3) and 11.(79) or 12 Ratio with same multiple of 7 eg, 100:7 and 82.5:7 or 200:14 and 165:14 |
|  | Kelly or Fizzy orange | A1 | Must have working with 1 of 2 values correct |
| 17 | $\begin{aligned} & 4 \times 142+5 \times 146+8 \times 150+7 \times \\ & 154+5 \times 158+1 \times 162 \end{aligned}$ | M1 | $\Sigma f x$ where $x$ is midpoint or end point or Values $\pm 0.5$ <br> For at least 2 multiplications and additions seen |
|  | Their $4528 \div 30$ | M1dep |  |
|  | 150.9(3...) | A1 | 151 with working |


| Q | Answer | Mark | Comments |
| :---: | :--- | :---: | :--- |
| $\mathbf{1 8}$ | Sight of 0.12 | B1 | $12 \%=£ 15 \mathrm{M} 1$ |
|  | $15 \div 0.12$ | M1 | $(1 \%)=15 \div 12(=1.25)$ |
|  | $125(.00)$ | A1 | -1 for incorrect money notation <br> Penalise for further contradictory working <br> eg, $125+15=140$ |


| $\mathbf{1 9 ( a )}$ | F, I, E, X | B3 | -1 eeoo |
| :--- | :--- | :---: | :--- |
| $\mathbf{1 9 ( b )}$ | $a^{2}+a b-b a-b^{2}$ | M1 | Must have 4 terms <br> Condone 1 sign error |
|  | $a^{2}-b^{2}$ | A1 | Must show cancellation, either by 'crossing out' <br> or stating $a b-a b=0$ |


| $\mathbf{2 0}$ | $100 \times 0.7 \div 5.5$ | M1 | Ratio weight biscuit: $100=0.7: 5.5$ |
| :---: | :--- | :---: | :--- |
|  | $12.72 \ldots$ | A1 |  |
|  | 12.7 or 13 | B1ft | Award for any value to at least 4 sf or <br> calculation that is correctly rounded to 2 or 3 sf |


| 21(a)(i) | 59 to 61 | B1 |  |
| :---: | :--- | :---: | :--- |
| $\mathbf{2 1 ( a ) ( i i ) ~}$ | Reading at $15(.25)$ and $45(.75)$ | M1 | $44-46,70-71$ |
|  | 24 to 27 | A1 |  |
| $\mathbf{2 1 ( b )}$ | $60-$ Their reading at a mark of 55 | M1 |  |
|  | 34 to 36 | A1 | SC1 24 to 26 identified by lines or mark on <br> graph |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 22 | Valid method | M1 | Method 1: Two triangles base 15 , height 7.5 <br> Method 2: 4 triangles base and height 7.5 <br> Method 3: $x^{2}+x^{2}=225$ <br> Method 4: 2 squares side 7.5 and 7.5 <br> Method 5: 1 rectangle sides 7.5 and 15 <br> Method 6: $7.5^{2}+7.5^{2}=x^{2}$ <br> Method 7: Use of trig, eg, $15 \sin 45^{\circ}$ <br> Method 8: Kite or rhombus |
| :---: | :---: | :---: | :---: |
|  | Correct values in method | A1 | $x=10.6(\ldots), 15 \sqrt{ } 2 / 2,2 x^{2}=225, \frac{1}{2} \times 15 \times 15$ |
|  | 112.5 | A1 | Must be exact but allow rounding to 112.5 after 112.49, say |


| 23 | True or T for $y=x+3$ | B 1 |  |
| :---: | :--- | :---: | :--- |
|  | False or F | B 1 |  |


| 24(a) | $x^{2}=35^{2}-22^{2}(=741)$ | M1 | $x^{2}+22^{2}=35^{2}$ |
| :---: | :--- | :---: | :--- |
|  | $(x=) \sqrt{ } 741$ | M1dep | For squaring, subtracting and evidence of <br> square rooting <br> M2 for full method using trig |
| $\mathbf{2 4 ( b )}$ | Sight of tangent | A1 | 27 with working |
|  | $27.2(\ldots .)$. | M1 | M2 for full method using sin/cos and pythag |
|  | $20 \div \tan 38$ | M1dep | $20 \tan 52$ |
|  | $25.6,25.5988 \ldots$ | A1 | $25.599,26$ with working |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 25 | Breaks down problem into areas of rectangles and areas of (quarter) circles | M1 | Any combination of rectangles and circles $\pi r^{2}$ or 12.56 or $4 \times \pi$ is enough evidence for area of circles <br> NB 12.56 from $2 \times \pi \times 2$, if seen is M0 <br> NB 3.14 on its own is not evidence of the area of a quarter circle as it is $\pi$ |
| :---: | :---: | :---: | :---: |
|  | Uses an 'addition' method (method 1) and finds <br> Area of one (or 5) 'external' quadrants $\begin{aligned} & (5 \times) 2 \times 2-\frac{1}{4} \pi \times 2^{2} \\ & \text { or }(5 \times) 4-\pi \\ & \text { or }(5 \times) \frac{1}{4}\left(16-\pi \times 2^{2}\right) \end{aligned}$ | M1 | Uses a 'subtraction' method (methods 2 and 3) and finds <br> $5 \times$ area of one 'internal' quadrant $5 \times \frac{1}{4} \pi \times 2^{2}$ <br> or $5 \times \pi$ |
|  | $\begin{aligned} & =0.8584 \ldots,(0.9,0.86,0.858) \\ & \text { or }(\times 5)=4.3,4.29,4.292 \ldots \end{aligned}$ | A1 | 15.71, 15.7 |
|  | 52.3 or $52.29(\ldots), 68-5 \pi$ | A1 | Allow 52 if full method seen |

